

Risk-Minimizing Tube Current Modulation (riskTCM) for CT – Potential Dose Reduction Across Different Tube Voltages

**Laura Klein^{1,2}, Chang Liu³, Jörg Steidel^{1,2}, Lucia Enzmann^{1,2}, Stefan Sawall^{1,2},
Joscha Maier¹, Andreas Maier³, Michael Lell⁴, and Marc Kachelrieß^{1,2}**

¹German Cancer Research Center (DKFZ), Heidelberg, Germany

²University of Heidelberg, Germany

³University of Erlangen-Nürnberg, Germany

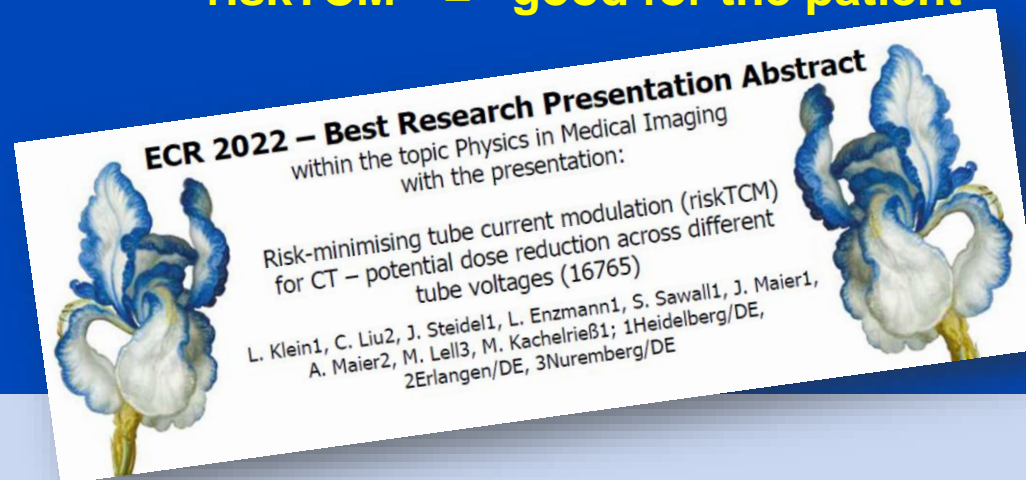
⁴Klinikum Nürnberg, Germany

Aim

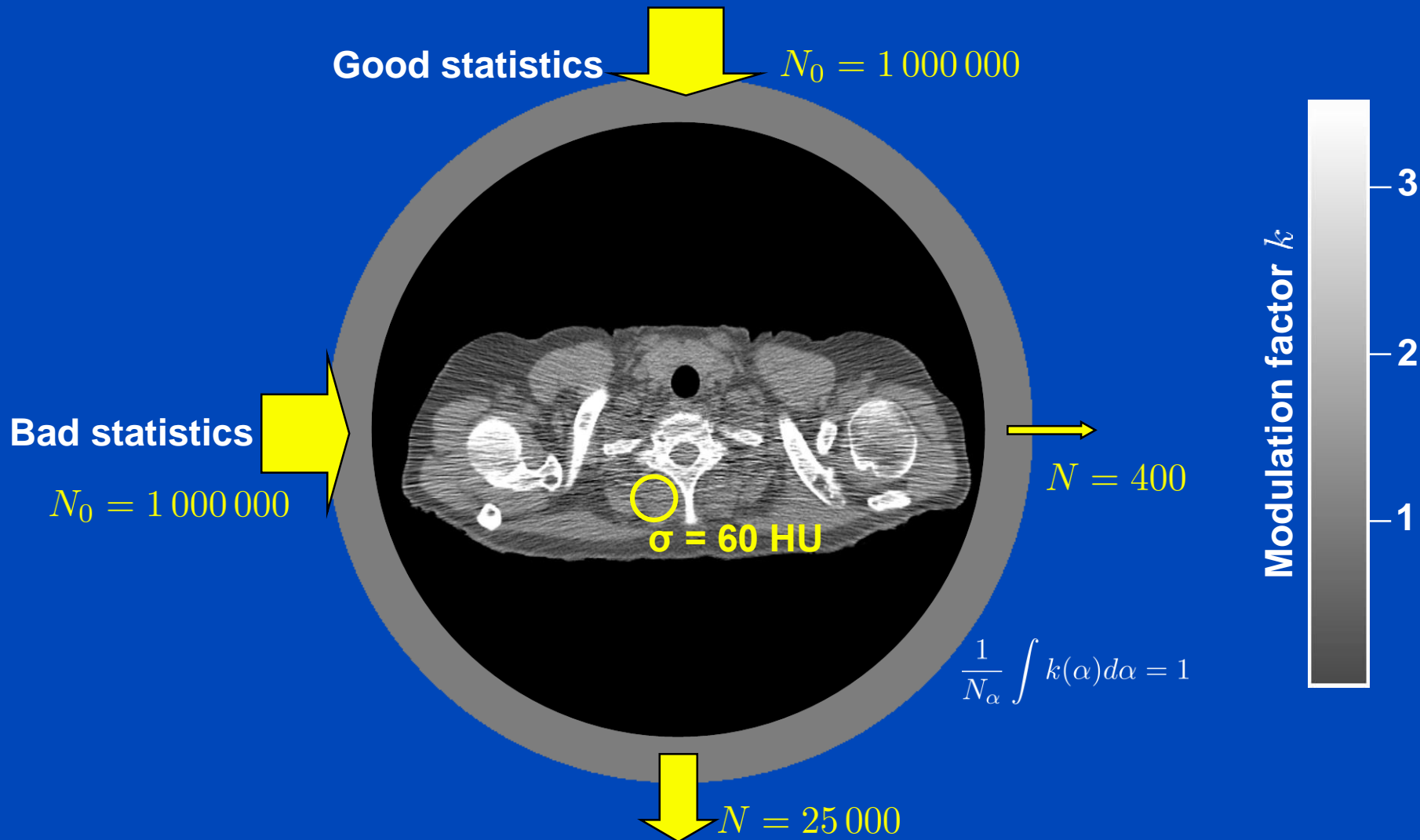
Today's state-of-art tube current modulation (**mAsTCM**) minimizes the mAs-product rather than the actual patient risk.

Therefore, we propose a patient risk minimizing TCM (**riskTCM**) and estimate the potential dose reduction compared to mAsTCM as function of tube voltage.

mAsTCM = good for the x-ray tube
riskTCM = good for the patient

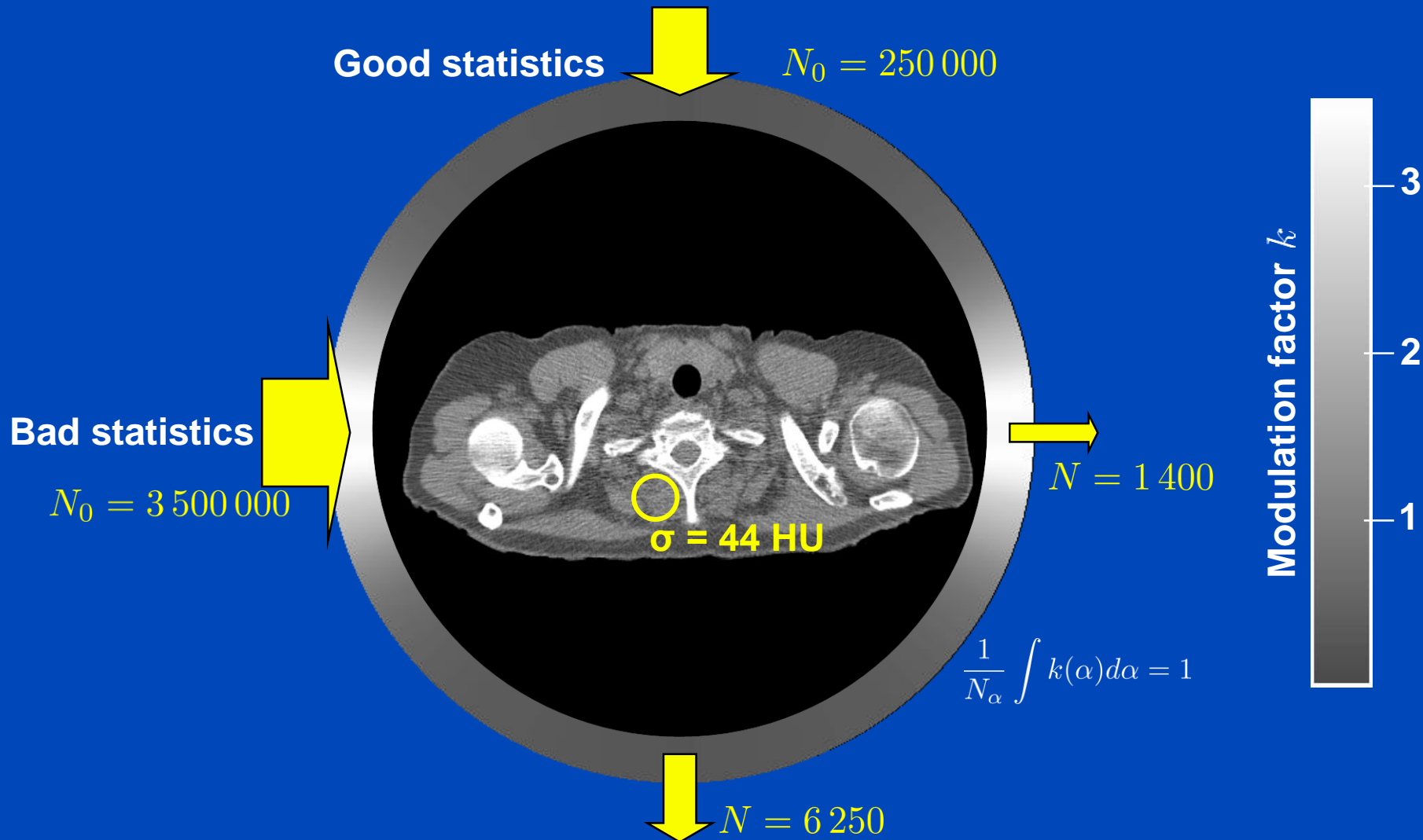


Tube Current Modulation



Constant tube current: High, inhomogeneous noise.

Tube Current Modulation



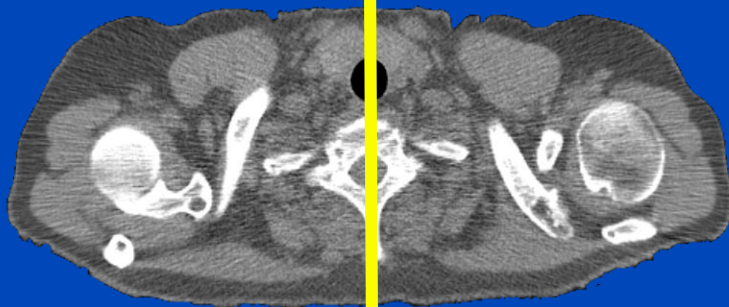
Modulated tube current: Lower, more homogeneous noise.

Tube Current Modulation

From a mathematical perspective

- The tube current modulation curve $I(\alpha)$ is chosen such that the variance in the CT reconstruction is minimal

$$N_0(\alpha) = c \cdot I(\alpha)$$



$$N(\alpha) = c \cdot I(\alpha) \cdot e^{-p(\alpha)}$$

- X-rays reaching the detector follow Poisson statistics:

$$\sigma_{N(\alpha)}^2 = N(\alpha) = c \cdot I(\alpha) \cdot e^{-p(\alpha)}$$

- Variance propagation to projection domain yields:

$$\sigma_{p(\alpha)}^2 = \frac{1}{c \cdot I(\alpha) \cdot e^{-p(\alpha)}}$$

- Variance propagation to image domain yields:

$$\sigma_f^2 = \sum_{\alpha} \frac{1}{c \cdot I(\alpha) \cdot e^{-p(\alpha)}}$$

- Cost function:

$$C = \sum_{\alpha} \frac{1}{c \cdot I(\alpha) \cdot e^{-p(\alpha)}} + \lambda \left(\sum_{\alpha} I(\alpha) - \text{const} \right)$$

For riskTCM, we also account for the effective dose $D_{\text{eff}}(\alpha)$ here.

- Minimization yields: $I(\alpha) \propto e^{\frac{1}{2} \cdot p(\alpha)}$

Cost Function

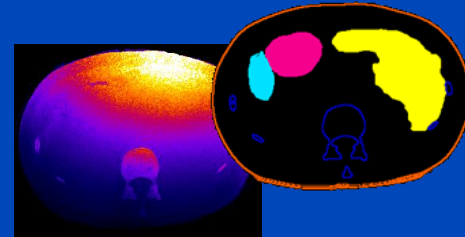


Table 3. Recommended tissue weighting factors.

Tissue	w_T	$\sum w_T$
Bone-marrow (red), Colon, Lung, Stomach,	0.12	0.72
Breast, Remainder tissues*		
Gonads	0.08	0.08
Bladder, Oesophagus, Liver, Thyroid	0.04	0.16
Bone surface, Brain, Salivary glands, Skin	0.01	0.04
Total		1.00

- For mAsTCM, the cost function is

$$C = \sum_{\alpha} \frac{1}{c \cdot \underbrace{I(\alpha)}_{\text{Image variance}} \cdot e^{-p(\alpha)}} + \lambda \left(\sum_{\alpha} I(\alpha) - \text{const} \right)$$

- For riskTCM, the equation is of the form

$$C = \sum_{\alpha} \text{Image variance}(\alpha) + \lambda \left(\sum_{\alpha} I(\alpha) \cdot D_{\text{eff}}(\alpha) - \text{const} \right)$$

$$D_{\text{eff}}(\alpha) = \sum_T w_T \cdot D_T(\alpha)$$

- The cost function for riskTCM also takes into account that the effective dose is dependent on the direction and is therefore not the same for two complementary (180°) rays, i.e. $D_{\text{eff}}(\alpha_D) \neq D_{\text{eff}}(\alpha_C)$.

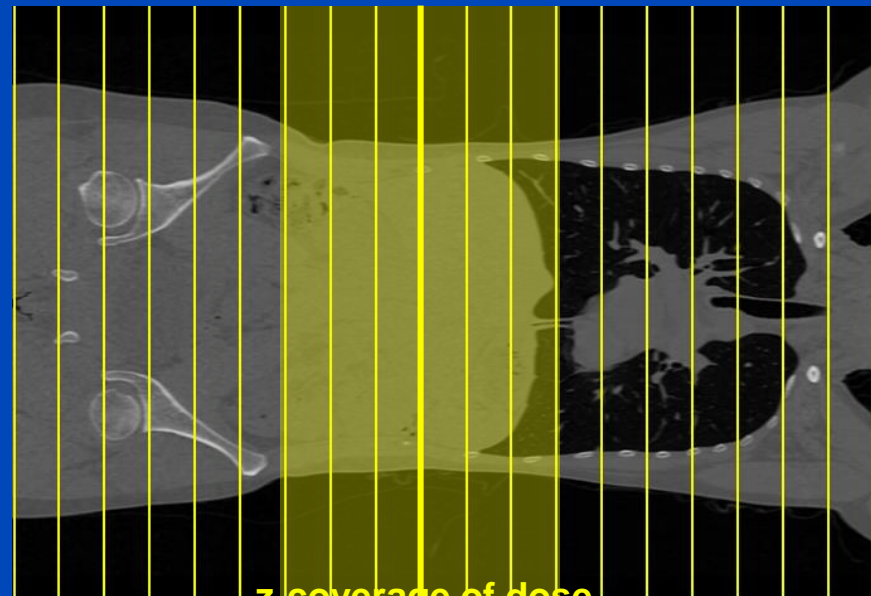
Retrospective Study

- Simulation of CT scans covering different anatomies at 70 kV, 100 kV, 120 kV, and 150 kV (6 mm Al prefiltration).
- Simulation of consecutive circle scans (38.4 mm apart), each with a z-collimation of 38.4 mm.

Axial view



Coronal view



$nz = 1$

z-coverage of dose
estimate at $nz = 10$

Effective Dose at Same Image Noise Relative to mAsTCM

Average over all patients

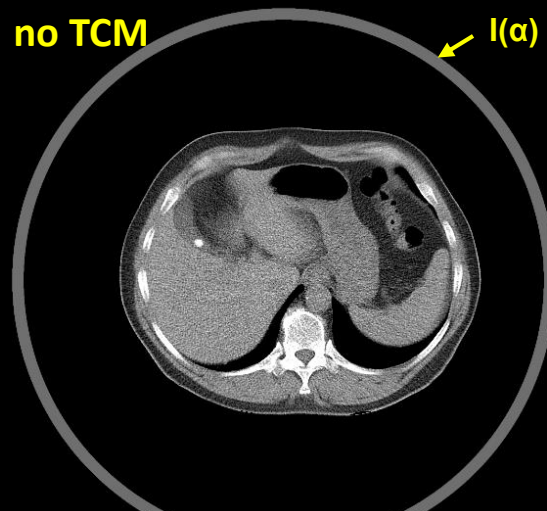
Abdomen

Tube Voltage	noTCM	mAsTCM	riskTCM
70 kV	113% from 105% to 135%	100%	69% from 57% to 76%
100 kV	113% from 103% to 137%	100%	71% from 62% to 79%
120 kV	114% from 106% to 135%	100%	72% from 64% to 79%
150 kV	115% from 106% to 136%	100%	73% from 66% to 80%

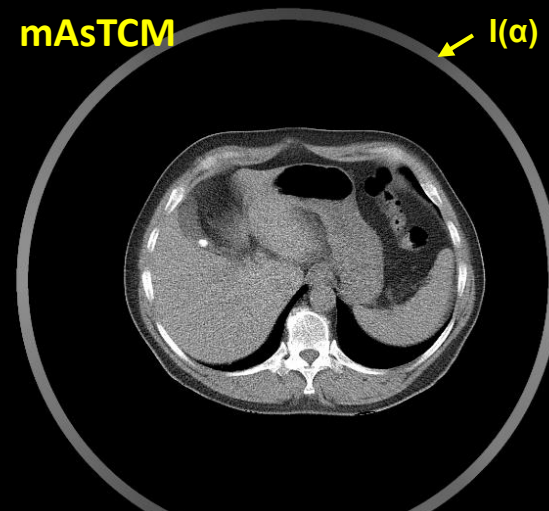
Head+Arms

Tube Voltage	noTCM	mAsTCM	riskTCM
70 kV	163% from 145% to 178%	100%	87% from 84% to 91%
100 kV	158% from 139% to 186%	100%	87% from 83% to 91%
120 kV	160% from 142% to 183%	100%	88% from 84% to 94%
150 kV	161% from 144% to 183%	100%	88% from 82% to 95%

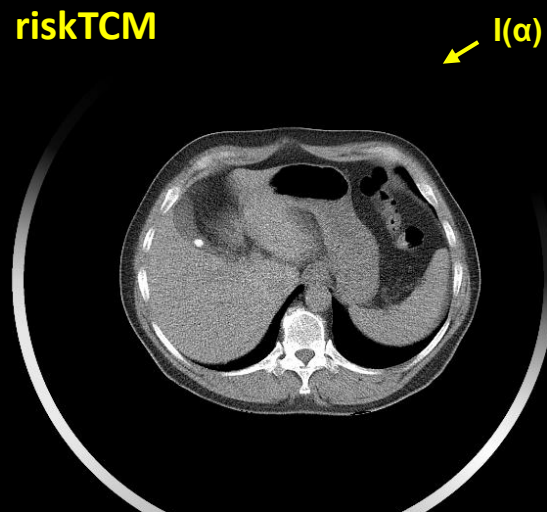
Modulation Curves for 70 kV



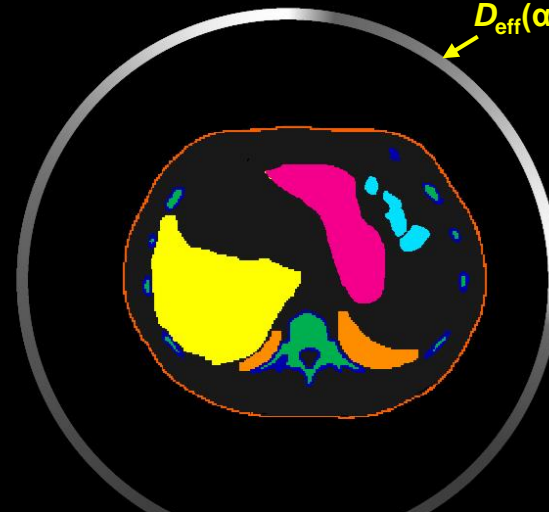
21 HU, 104% mAs, 109% D_{eff}



21 HU, 100% mAs, 100% D_{eff}



21 HU, 102% mAs, 63% D_{eff}



$C = 25 \text{ HU}$, $W = 400 \text{ HU}$

Conclusions

- All considered anatomical regions benefit from riskTCM.
- The highest potential D_{eff} reduction is seen for the abdomen, i.e. about 31% compared to mAsTCM, on average, for 70 kV.
- In case of head examinations, the proposed method achieves a D_{eff} reduction of about 13% compared to mAsTCM, for 70 kV.
- The proposed riskTCM method can be easily adapted to risk measures other than D_{eff} .
- This applies particular since other risk measures typically also account for organ doses.

Thank You!

This presentation will soon available at www.dkfz.de/ct.

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