

CT Calibration and Dose Minimization in Image-Based Material Decomposition With Energy-Selective Detectors

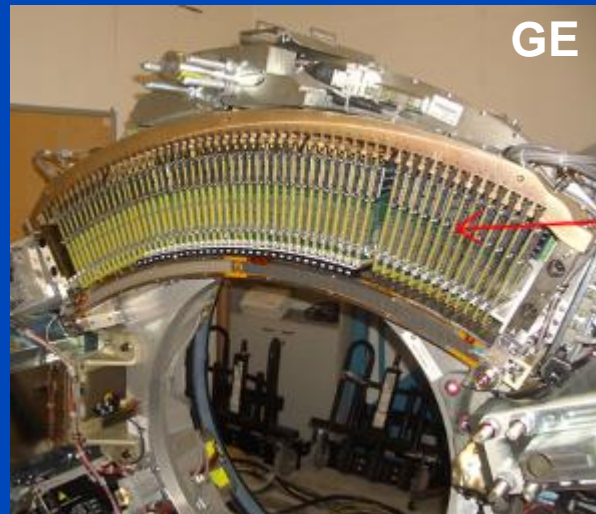
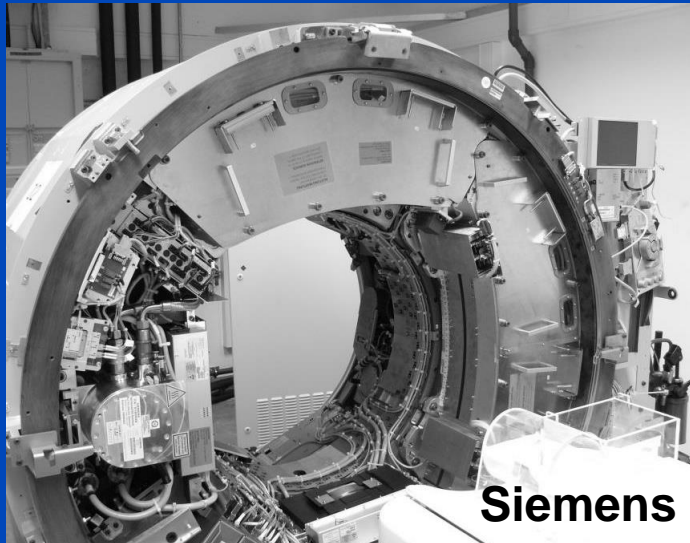
Sebastian Faby¹, Stefan Kuchenbecker^{1,2}, David Simons¹,
Heinz-Peter Schlemmer¹, Michael Lell²,
and Marc Kachelrieß^{1,2}

¹German Cancer Research Center (DKFZ), Heidelberg, Germany

²Friedrich-Alexander-University (FAU) Erlangen-Nürnberg, Germany

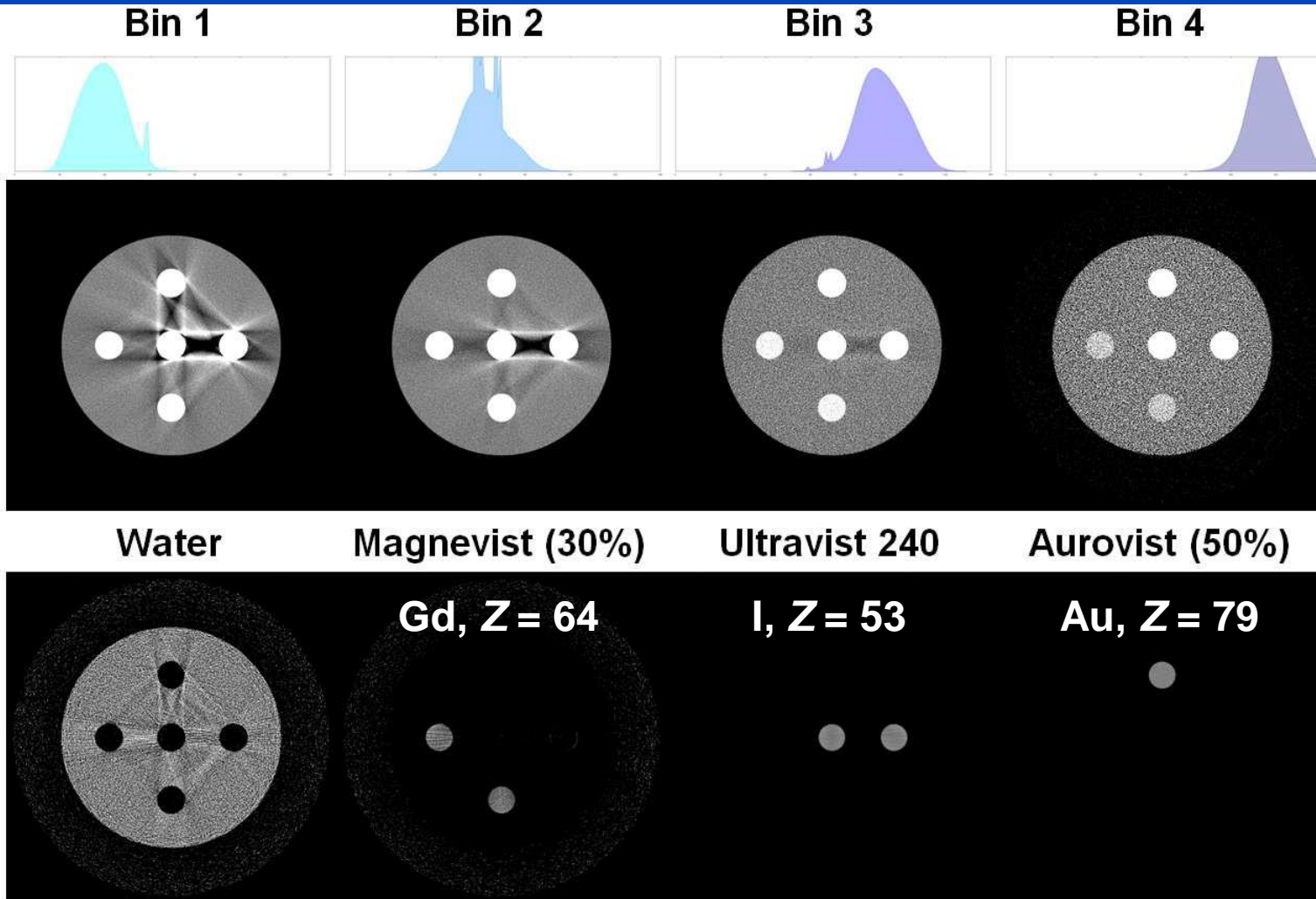
Aims

- Make use of energy data redundancies in multi energy CT
- Minimize noise in material images, i.e. reduce patient dose



Motivation

- Typical case: $B = 4$ energy bins, $M = 4$ basis materials



Motivation

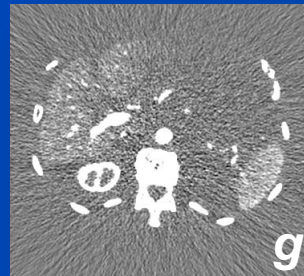
- **Without multiple high-Z contrast agents:**
- **Clinically interesting case only $M = 2$:**
 - Water/soft tissue and bone/iodine
 - Photoelectric effect and Compton scattering
- **Number energy bins $B >$ number basis materials M**
→ Gain in degrees of freedom, how to use it?
- **Image-based method for this task**
 - Narrow energy bins, images show only very little beam hardening
 - Linear image-based methods are fast.
- **Projection-based algorithms available**
 - Maximum likelihood approach (Roessl and Proksa, PMB 2007)
 - EMEC + Dose Minimization (Maaß *et al.*, MIC 2011)

Algorithm Concept

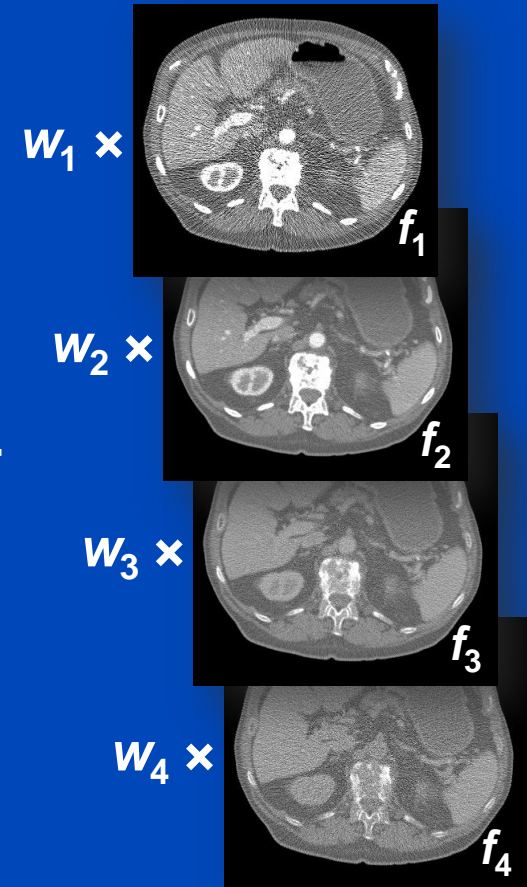
- Linear image weighting
 - Material image g
 - Weighting coefficients w
 - Energy bin images f

$$g = \begin{pmatrix} +16.5 \\ +81.8 \\ -79.7 \\ -44.9 \end{pmatrix} \cdot \begin{pmatrix} f_1 \\ f_2 \\ f_3 \\ f_4 \end{pmatrix}$$

Material image g



Bin images f



- Two subsequent steps:
 - Material decomposition calibration
 - Image noise minimization using the $K = B - M$ degrees of freedom

Material Decomposition Calibration

- Example for $M = 2$: water and iodine
- $N = 2$ calibration measurements using ROIs
- Determine weighting coefficients w
 - $M \times B$ coefficients, but $M \times N$ equations

WATER

$$\begin{matrix} \text{Water} \\ \text{Iodine} \end{matrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} \stackrel{!}{=} \begin{pmatrix} w_{W,1} \dots w_{W,B} \\ w_{I,1} \dots w_{I,B} \end{pmatrix} \cdot \begin{pmatrix} f_{W,1} \\ \vdots \\ f_{W,B} \end{pmatrix} \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

Target values

ROI values

IODINE

$$\begin{matrix} \text{Water} \\ \text{Iodine} \end{matrix} \begin{pmatrix} 1 \\ 1 \end{pmatrix} \stackrel{!}{=} \begin{pmatrix} w_{W,1} \dots w_{W,B} \\ w_{I,1} \dots w_{I,B} \end{pmatrix} \cdot \begin{pmatrix} f_{I,1} \\ \vdots \\ f_{I,B} \end{pmatrix} \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$



- Case studied in the simulations

Material Decomposition Calibration

- Problem separable for the M basis materials
- $N \geq M$ calibration measurements to determine w :

$$g_n = \sum_b f_{nb} w_b \quad g = F \cdot w$$

- In general $N \neq B$, least squares approach:

$$w = \operatorname{argmin}_w (F \cdot w - g)^2$$

- Linear system for w :

$$\underbrace{F^T F}_{B \times B \text{ matrix, rank at most } M} \cdot w = \underbrace{F^T g}_{\text{Vector of dim. } B}$$

$B \times B$ matrix, rank at most M

Vector of dim. B

- Singular value decomposition:

$$w(\alpha_k) = w_0 + \sum_{k=1}^K \alpha_k w_k, \quad \forall \alpha_k \in \mathbb{R}$$

Rank M solution

Null space, dimension $K = B - M$

Image Noise Minimization

- Exploit free parameters α_k of the null space

$$w(\alpha_k) = w_0 + \sum_k \alpha_k w_k$$

- Noise minimization = maximizing CNR
- Covariance matrix C of all bin images:

$$C_{bb'} = \frac{1}{P-1} \sum_{p \in \text{ROI}} (f_b(p) - \bar{f}_b)(f_{b'}(p) - \bar{f}_{b'})$$

- Error propagation:

$$\text{Var } g = w^T(\alpha_k) \cdot C \cdot w(\alpha_k)$$

- Minimize variance: $\frac{\partial \text{Var } g}{\partial \alpha_j} = 0$

- Resulting linear system $A \cdot \alpha = b$ with:

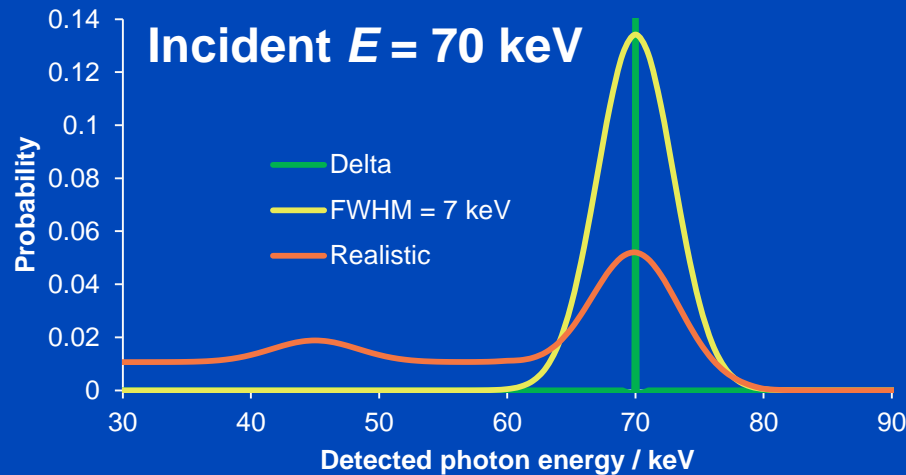
$$A_{jk} = \sum_b \sum_{b'} w_{jb} w_{kb'} C_{bb'} \quad \text{and} \quad b_j = - \sum_b \sum_{b'} w_{jb} w_{0b'} C_{bb'}$$

Simulations

- **Asses the proposed algorithm**
- **Study typical dual energy CT (DECT) application:**
 - Material decomposition into a water-equivalent and an iodine material image
- **Comparison of:**
 - Dual energy technique, energy integrating (EI) detectors
 - Energy-selective photon counting (PC) detectors
- **Based on patient data set with low noise**
 - Averaged over 8 thin slices
 - Separation into water and bone
 - Forward projection to obtain material-specific sinograms for polychromatic simulation

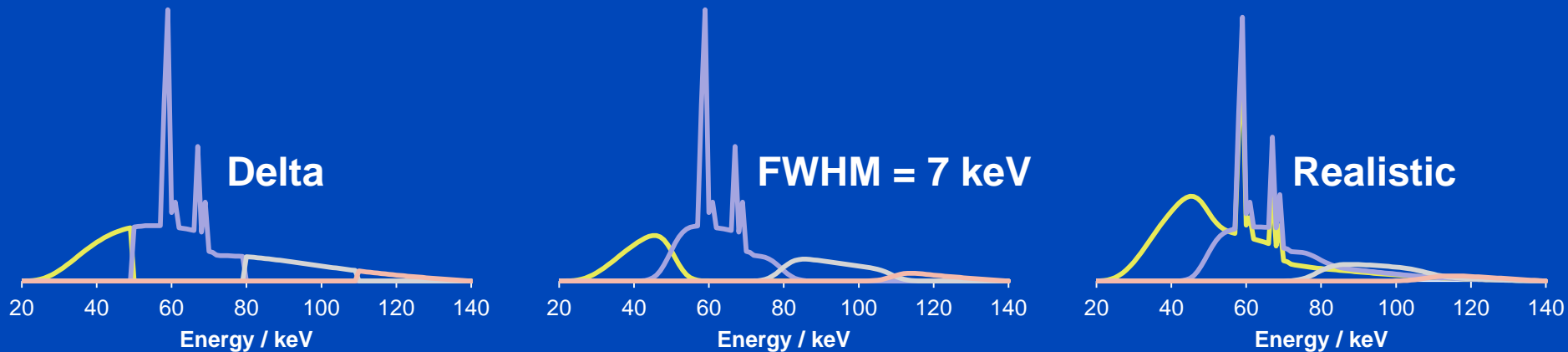
Simulations

- Spectral response:



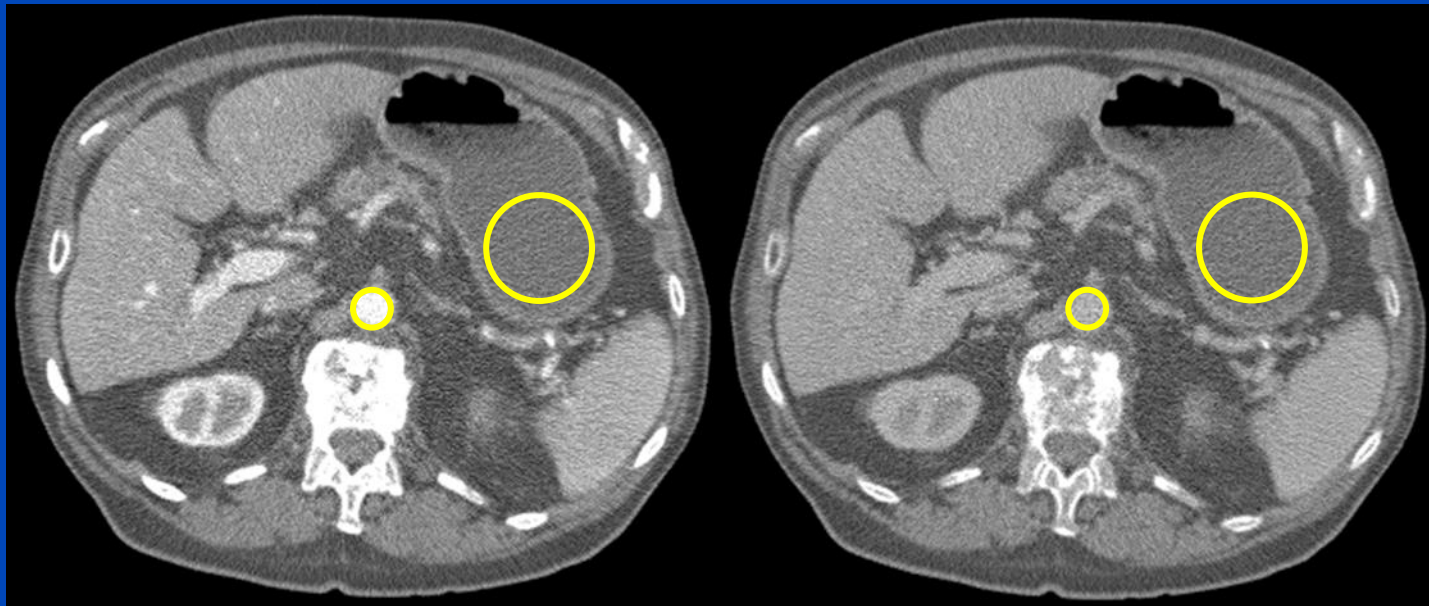
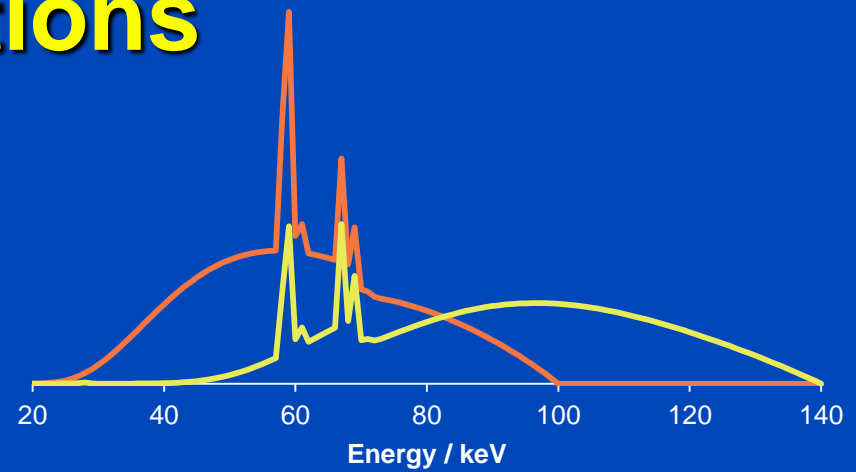
Energy bins placed equidistantly from 20 keV to 140 keV

- Energy bin spectra for $B = 4$:



Simulations

- Dual source DECT:
 - 100 kV
 - 140 kV + 0.4 mm Sn



100 kV

140 kV Sn

C = 0 HU / W = 700 HU

Results – Delta Model

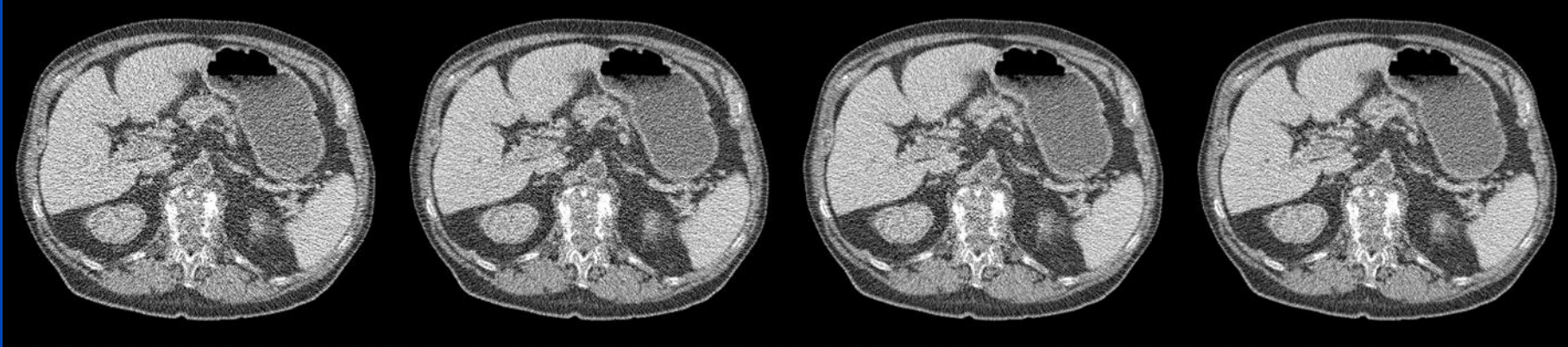
DECT

PC 2 Bins

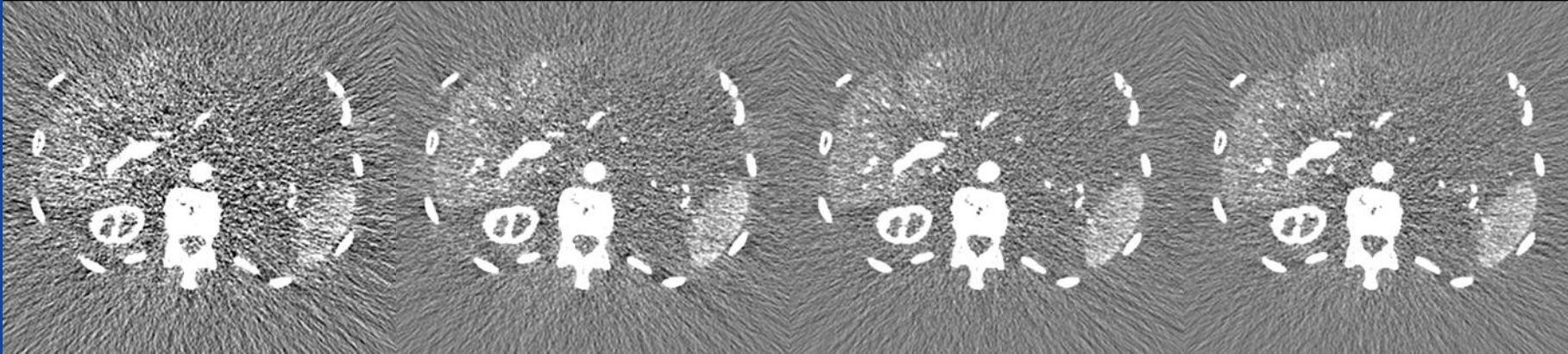
PC 4 Bins

PC 8 Bins

Water



Iodine

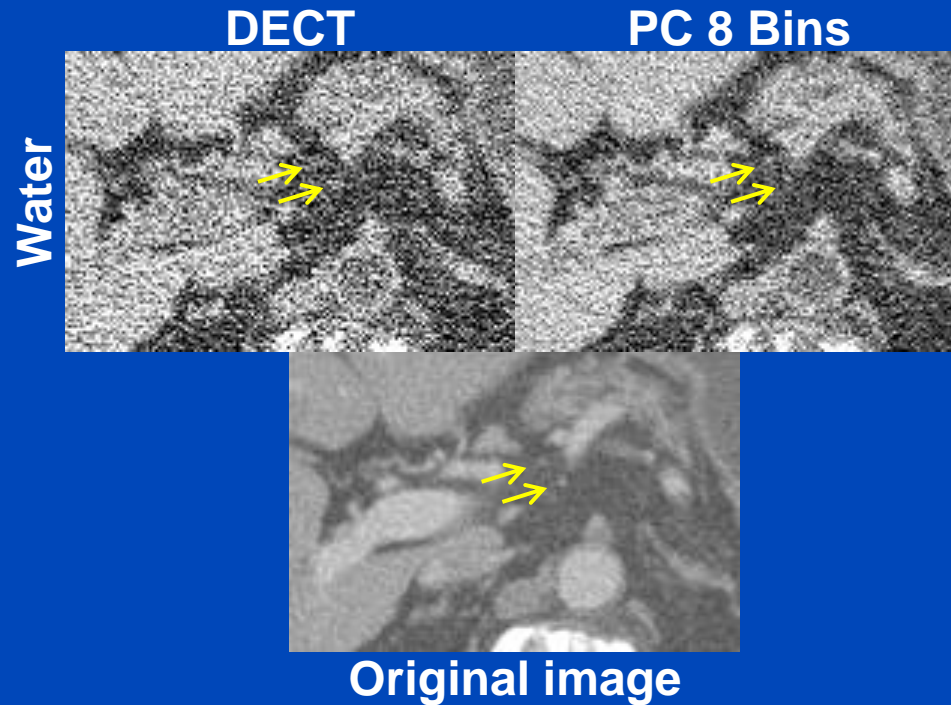


		2 bins	4 bins	8 bins	12 bins
Water	Noise rel. to DECT	-16%	-22%	-27%	-29%
Iodine	Noise rel. to DECT	-37%	-43%	-49%	-52%

$$\frac{\sigma_{PC}}{\sigma_{DECT}} - 1$$

Water: C = 1 / W = 0.4
Iodine: C = 0 / W = 0.4

Results – Delta Model



		2 bins	4 bins	8 bins	12 bins
Water	Noise rel. to DECT	-16%	-22%	-27%	-29%
Iodine	Noise rel. to DECT	-37%	-43%	-49%	-52%

$$\frac{\sigma_{PC}}{\sigma_{DECT}} - 1$$

Water: C = 1 / W = 0.4
Iodine: C = 0 / W = 0.4

Results – FWHM = 7 keV Model

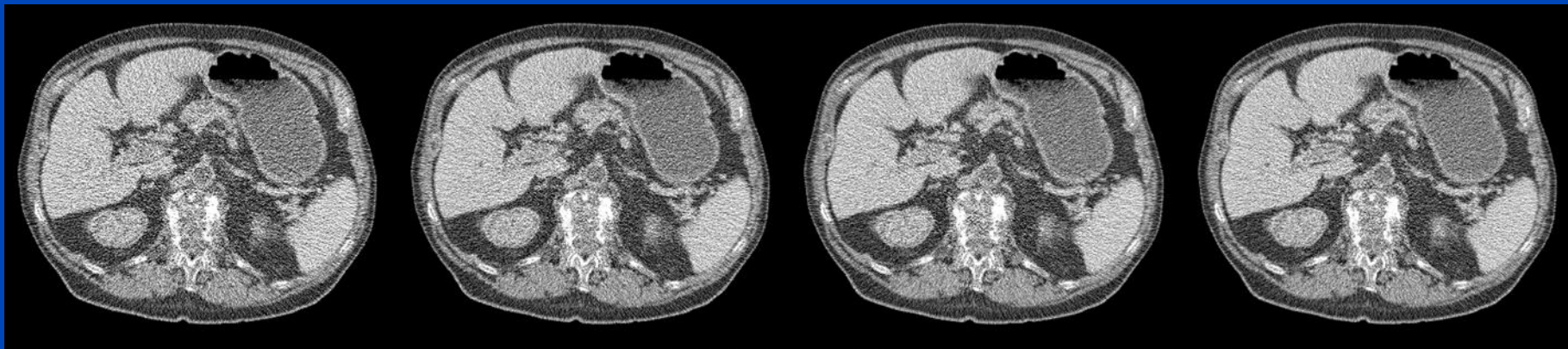
DECT

PC 2 Bins

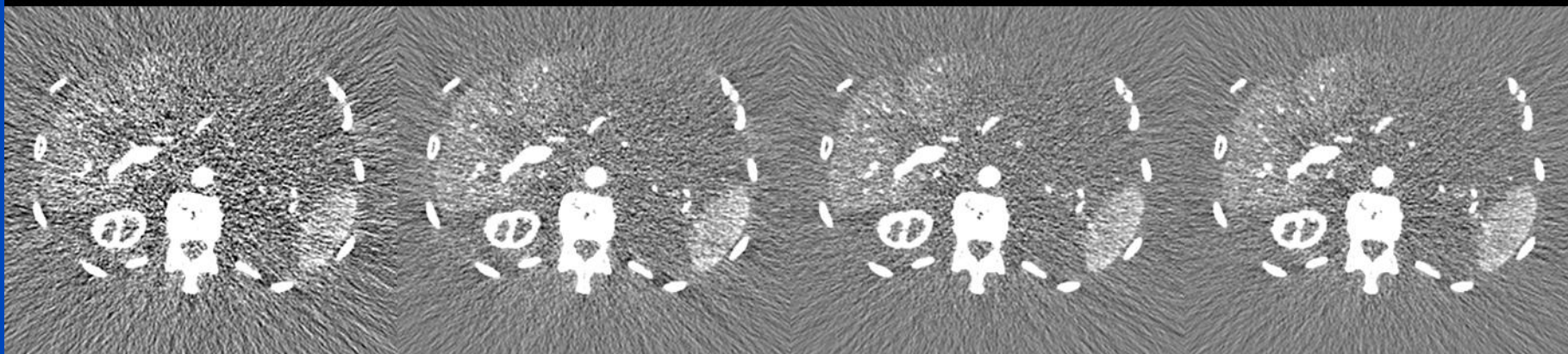
PC 4 Bins

PC 8 Bins

Water



Iodine



		2 bins	4 bins	8 bins	12 bins
Water	Noise rel. to DECT	-15%	-21%	-26%	-27%
Iodine	Noise rel. to DECT	-37%	-43%	-48%	-49%

$$\frac{\sigma_{PC}}{\sigma_{DECT}} = 1$$

Water: C = 1 / W = 0.4
 Iodine: C = 0 / W = 0.4

Results – Realistic Model

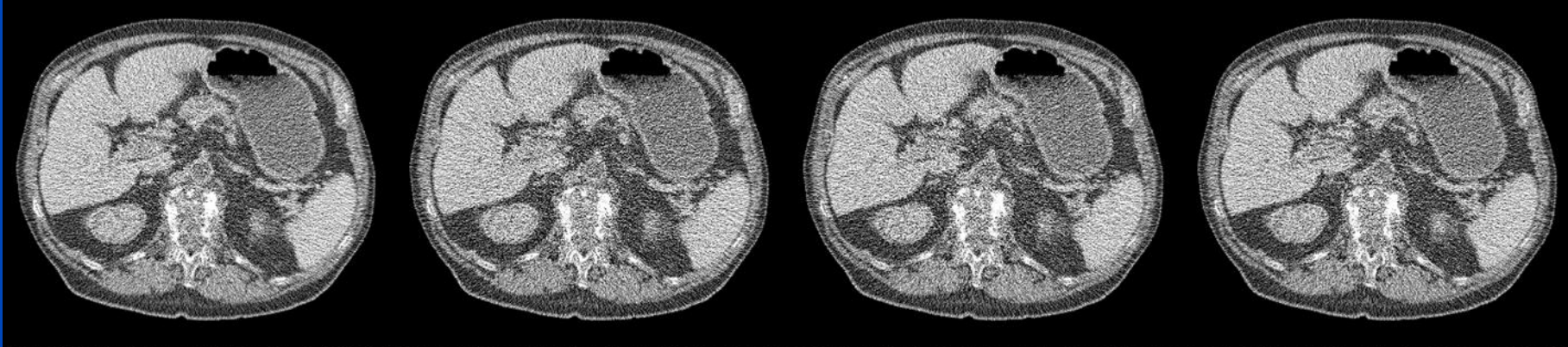
DECT

PC 2 Bins

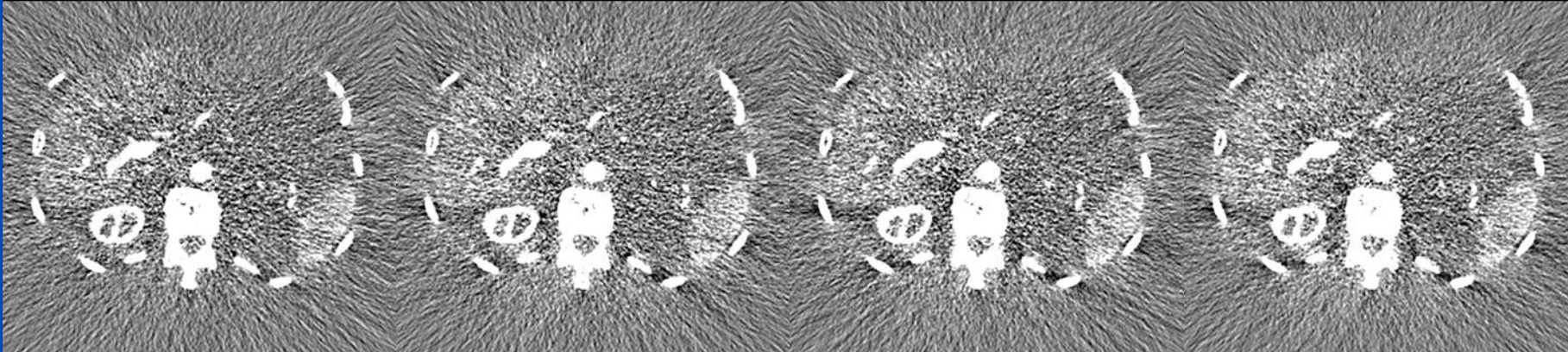
PC 4 Bins

PC 8 Bins

Water



Iodine



		2 bins	4 bins	8 bins	12 bins
Water	Noise rel. to DECT	+27%	+23%	+15%	+15%
Iodine	Noise rel. to DECT	+6%	+2%	-6%	-6%

$$\frac{\sigma_{PC}}{\sigma_{DECT}} - 1$$

Water: C = 1 / W = 0.4
Iodine: C = 0 / W = 0.4

Conclusions

- Good performance of image noise minimization step
- Ideal:
 - PC detector with $B = 2$ already better than DECT (no image noise minimization possible in this case)
 - Noise reduction significant with $B = 8$:
Water image -27%, iodine image -49%
- Realistic:
 - Finite energy resolution of PC detector not a problem
 - Low energy tail of realistic model vitiating all advantages of PC detector, DECT performing better than PC detector
- Shortcoming: Correlations not taken into account for realistic detector scenario, results will be presented in a later publication

Thank You!

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This presentation will soon be available at www.dkfz.de/ct.

Parts of the reconstruction software were provided by RayConStruct[®] GmbH, Nürnberg, Germany.