

# Optimal Image-Based Material Decomposition With Energy-Selective Detectors in Spectral CT in Comparison to Dual Energy CT (DECT)

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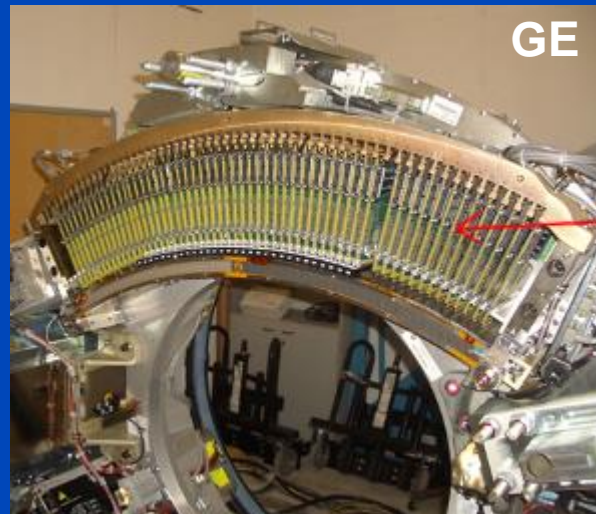
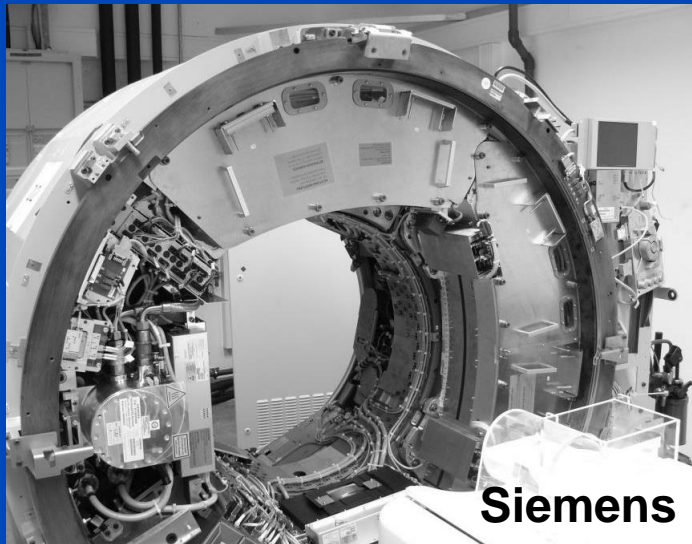
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# Aims

- Make use of energy data redundancies in spectral CT with photon counting (PC) detectors
- Minimize noise in material images, i.e. reduce patient dose
- Compare to today's dual energy CT (DECT)



# Motivation

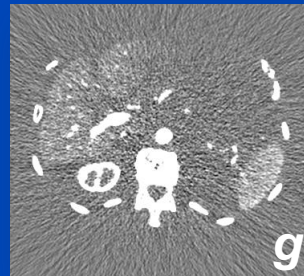
- Clinically only two independent basis materials exist:
  - 1 = water/soft tissue, 2 = bone/iodine
  - 1 = photoelectric effect, 2 = Compton scattering
  - 1 = virtual non-contrast (VNC) image, 2 = iodine map
- Two basis materials, but more than two energy bins  
→ Optimally use additional degrees of freedom!
- Image-based method for this task
  - Narrow energy bins, images show only little beam hardening.
  - Image-based methods are fast.
- Projection-based algorithms available
  - Maximum likelihood approach (Roessl and Proksa, PMB 2007)
  - EMEC + Dose Minimization (Maaß and Kachelrieß, MIC 2011)

# Algorithm Concept

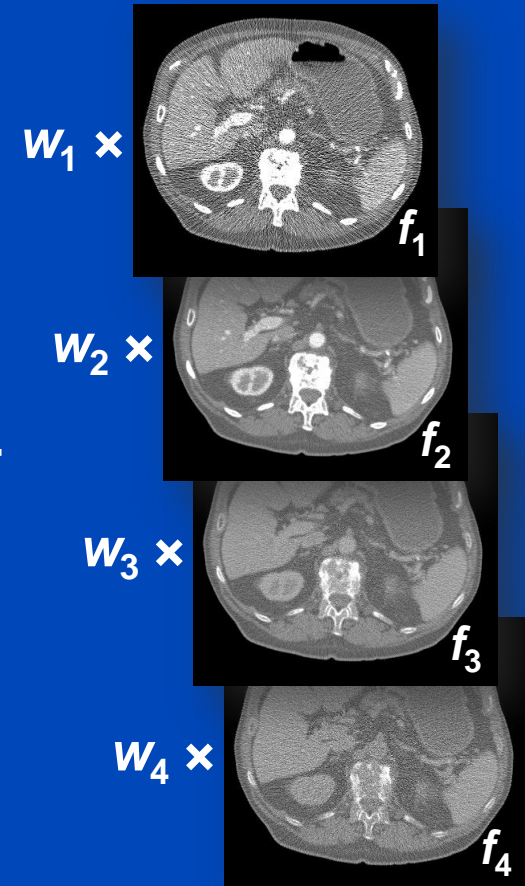
- Linear image weighting
  - Material image  $g$
  - Weighting coefficients  $w$
  - Energy bin images  $f$

$$g = \begin{pmatrix} w_1 \\ \vdots \\ w_B \end{pmatrix} \cdot \begin{pmatrix} f_1 \\ \vdots \\ f_B \end{pmatrix}$$

Material image  $g$



Bin images  $f$



- Two subsequent steps:
  - **Material decomposition** calibration
  - Image **noise minimization** using the additional degrees of freedom

# Algorithm

- Material images: E.g. VNC image and iodine map
- Two calibration measurements: water and iodine ROI
- Calibrate weighting coefficients  $w$ 
  - $B$  coefficients, but only  $M = 2$  calibration equations
  - We solve this in a least squares sense
- SVD finds the solution and the null space

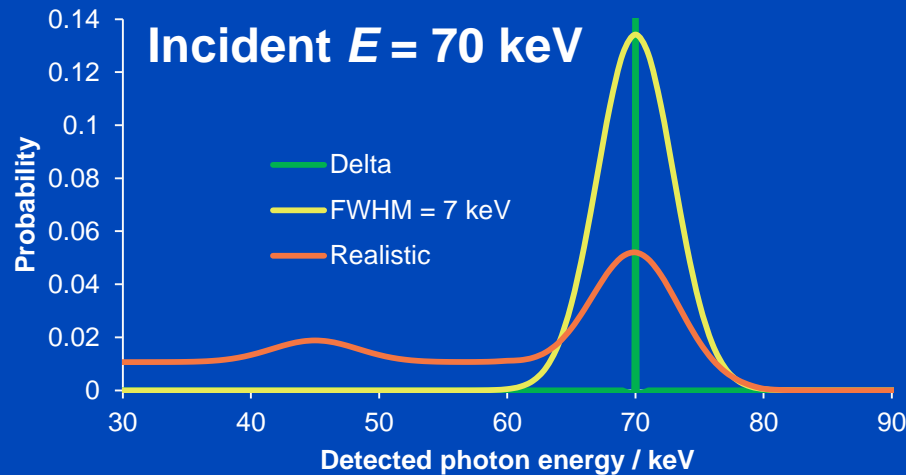
$$w(\alpha_k) = w_0 + \sum_{k=1}^{B-M} \alpha_k w_k, \quad \forall \alpha_k \in \mathbb{R}$$


- Covariance matrix  $C$  of all bin images required
- Use error propagation to find minimum noise solution based on null space:

$$\text{Var } g = w^T \cdot C \cdot w$$

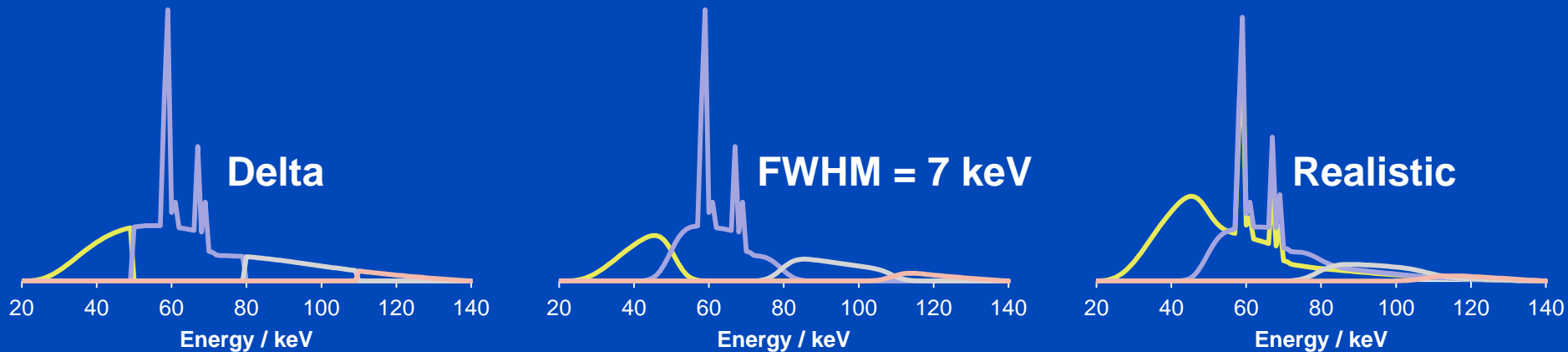
# Simulation Spectral CT

- Spectral response:



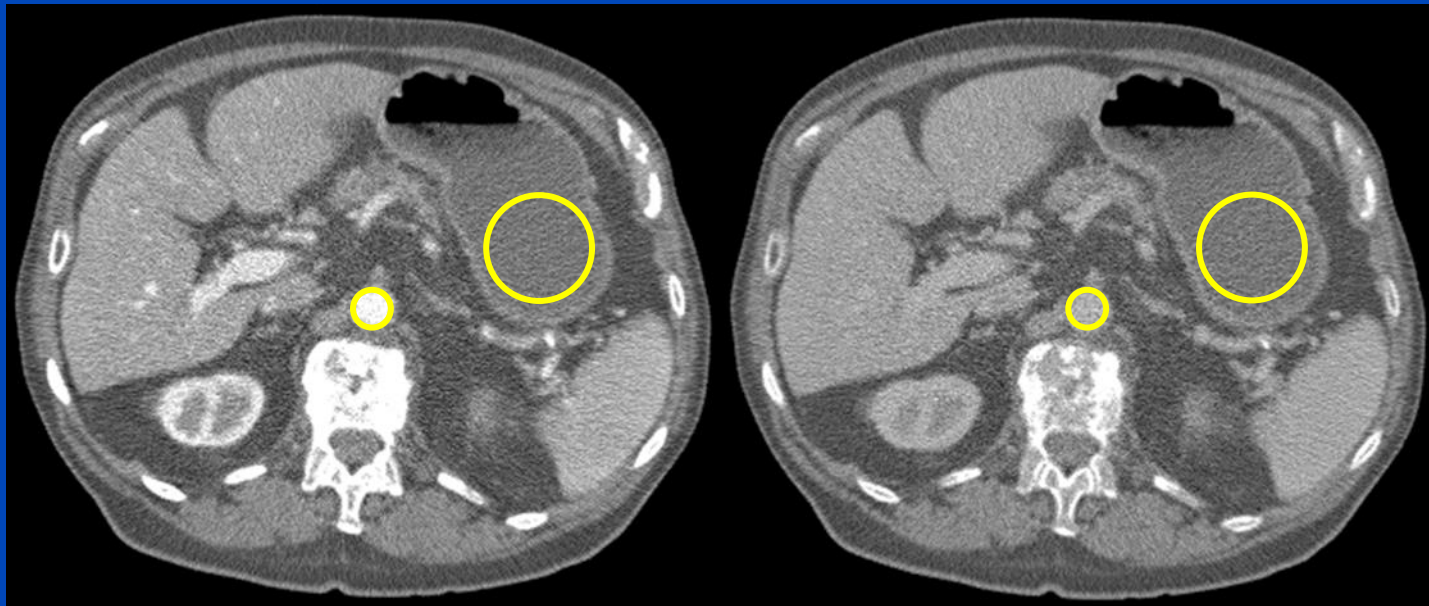
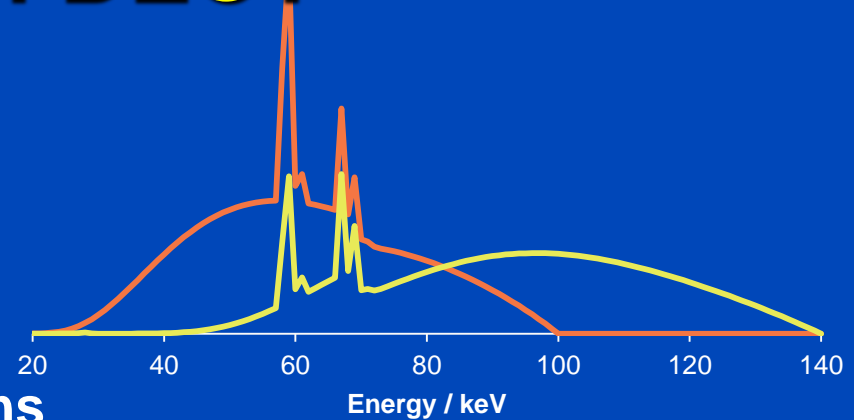
Energy bins placed equidistantly from 20 keV to 140 keV

- Energy bin spectra for four energy bins:



# Simulation DECT

- Dual source DECT:
  - 100 kV
  - 140 kV + 0.4 mm Sn
  - Corresponds to two energy bins



100 kV

140 kV Sn

C = 0 HU / W = 700 HU

# Results – Delta Model

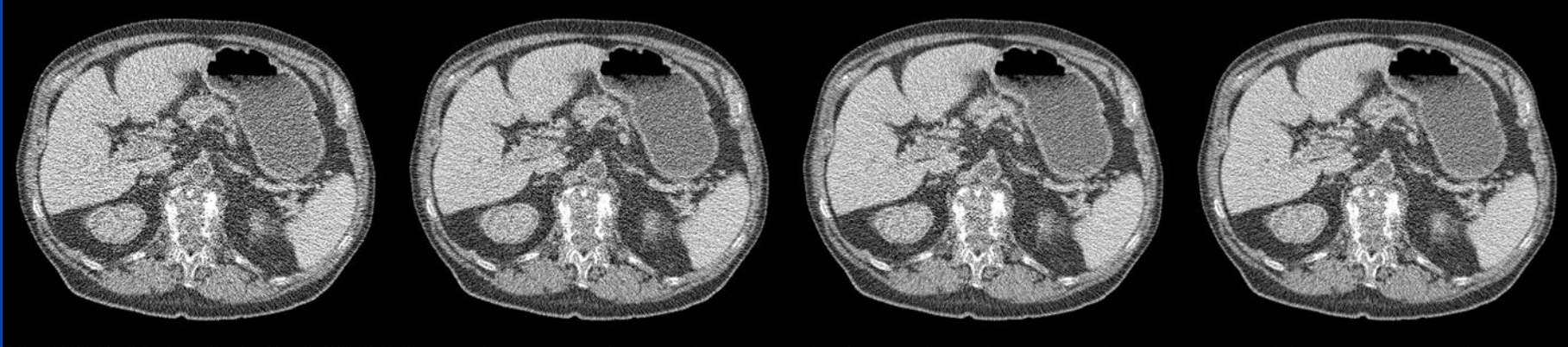
DECT

PC 2 bins

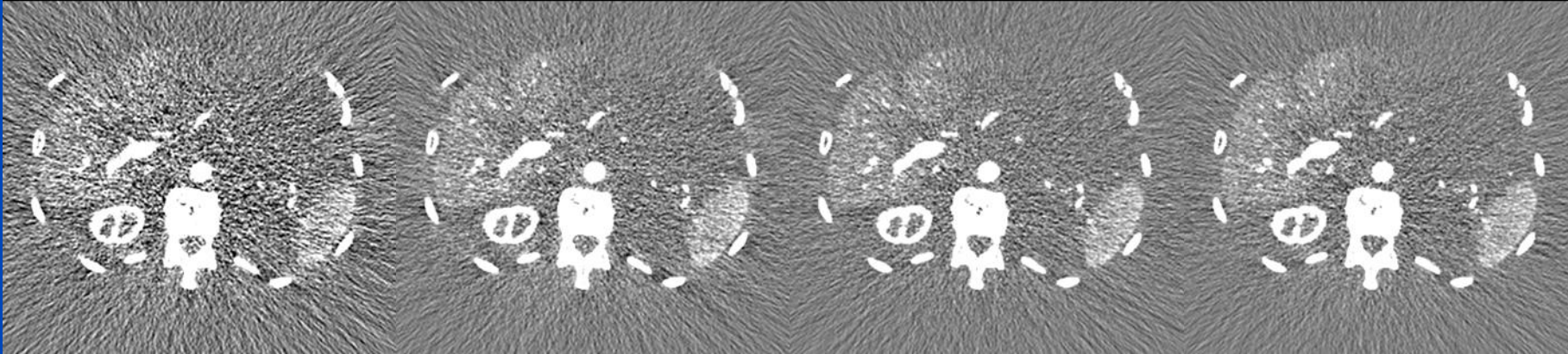
PC 4 bins

PC 8 bins

Water



Iodine



		2 bins	4 bins	8 bins	12 bins
Water	Noise rel. to DECT	-16%	-22%	-27%	-29%
Iodine	Noise rel. to DECT	-37%	-43%	-49%	-52%

$$\frac{\sigma_{PC}}{\sigma_{DECT}} - 1$$

Water: C = 1 / W = 0.4  
Iodine: C = 0 / W = 0.4



# Results – FWHM = 7 keV Model

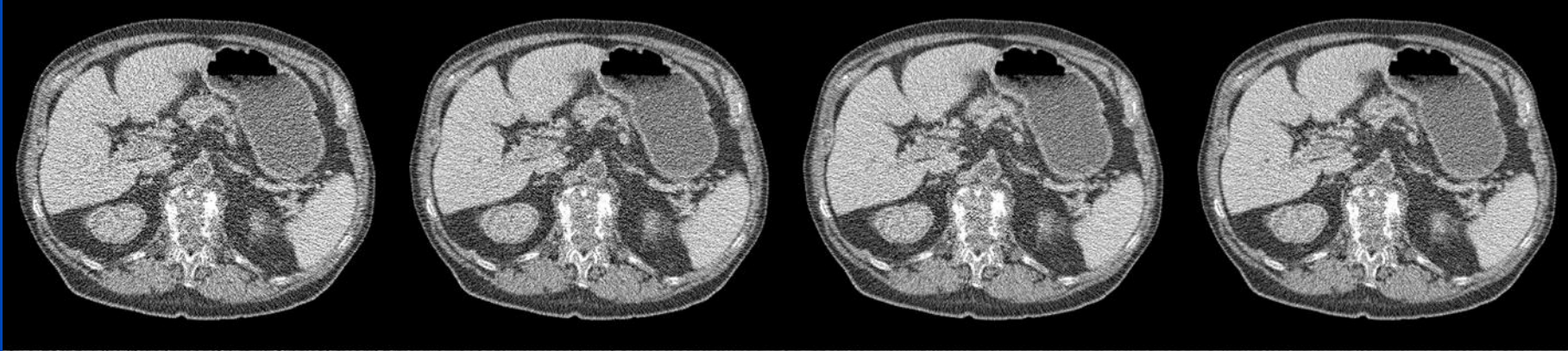
DECT

PC 2 bins

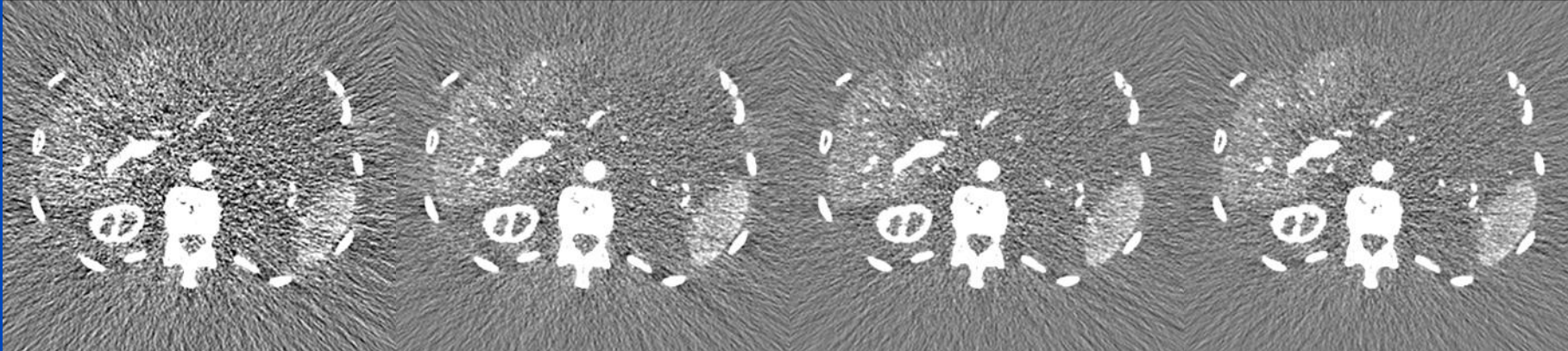
PC 4 bins

PC 8 bins

Water



Iodine



		2 bins	4 bins	8 bins	12 bins
Water	Noise rel. to DECT	-15%	-21%	-26%	-27%
Iodine	Noise rel. to DECT	-37%	-43%	-48%	-49%

$$\frac{\sigma_{PC}}{\sigma_{DECT}} = 1$$

Water: C = 1 / W = 0.4

Iodine: C = 0 / W = 0.4

# Results – Realistic Model

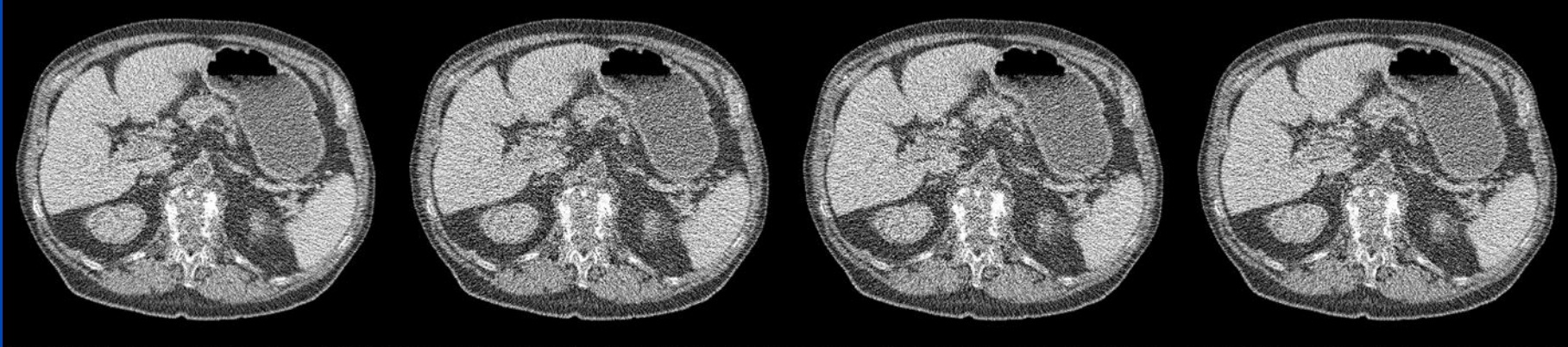
DECT

PC 2 bins

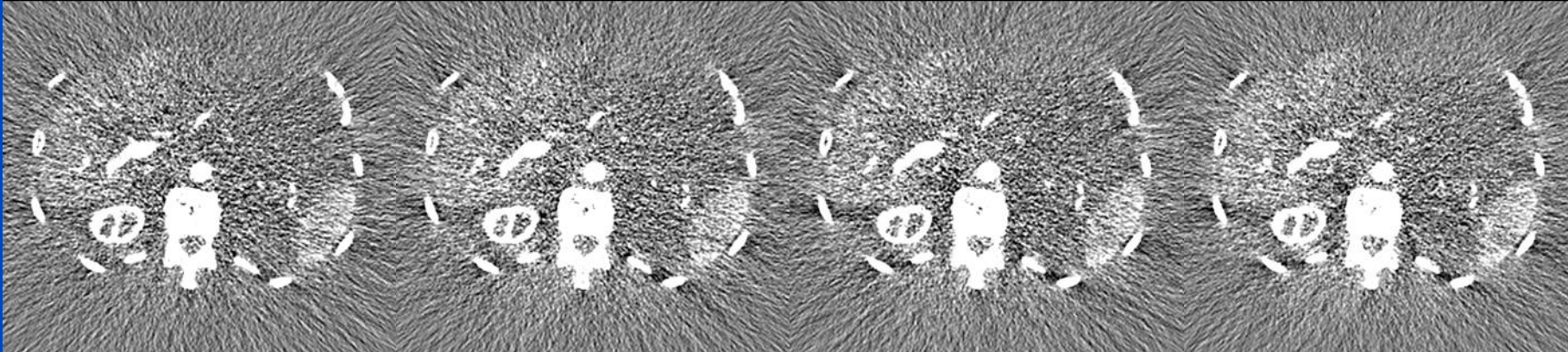
PC 4 bins

PC 8 bins

Water



Iodine



		2 bins	4 bins	8 bins	12 bins
Water	Noise rel. to DECT	<b>+27%</b>	<b>+23%</b>	<b>+15%</b>	<b>+15%</b>
Iodine	Noise rel. to DECT	<b>+6%</b>	<b>+2%</b>	<b>-6%</b>	<b>-6%</b>

$$\frac{\sigma_{PC}}{\sigma_{DECT}} - 1$$

Water: C = 1 / W = 0.4  
Iodine: C = 0 / W = 0.4

# Conclusions

- **Ideal energy response:**
  - PC detector with two bins is already better than DECT.
- **Realistic energy response:**
  - Low energy tail of realistic model impairs PC performance.
  - DECT is performing better than PC detector.
- **Good performance of image noise minimization step:**
  - More than 10% additional noise reduction (8 vs. 2 bins)
  - Corresponds to more than 18% dose reduction

# Thank You!

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This presentation will soon be available at [www.dkfz.de/ct](http://www.dkfz.de/ct).