

A New Approach to Regularized Iterative CT Image Reconstruction

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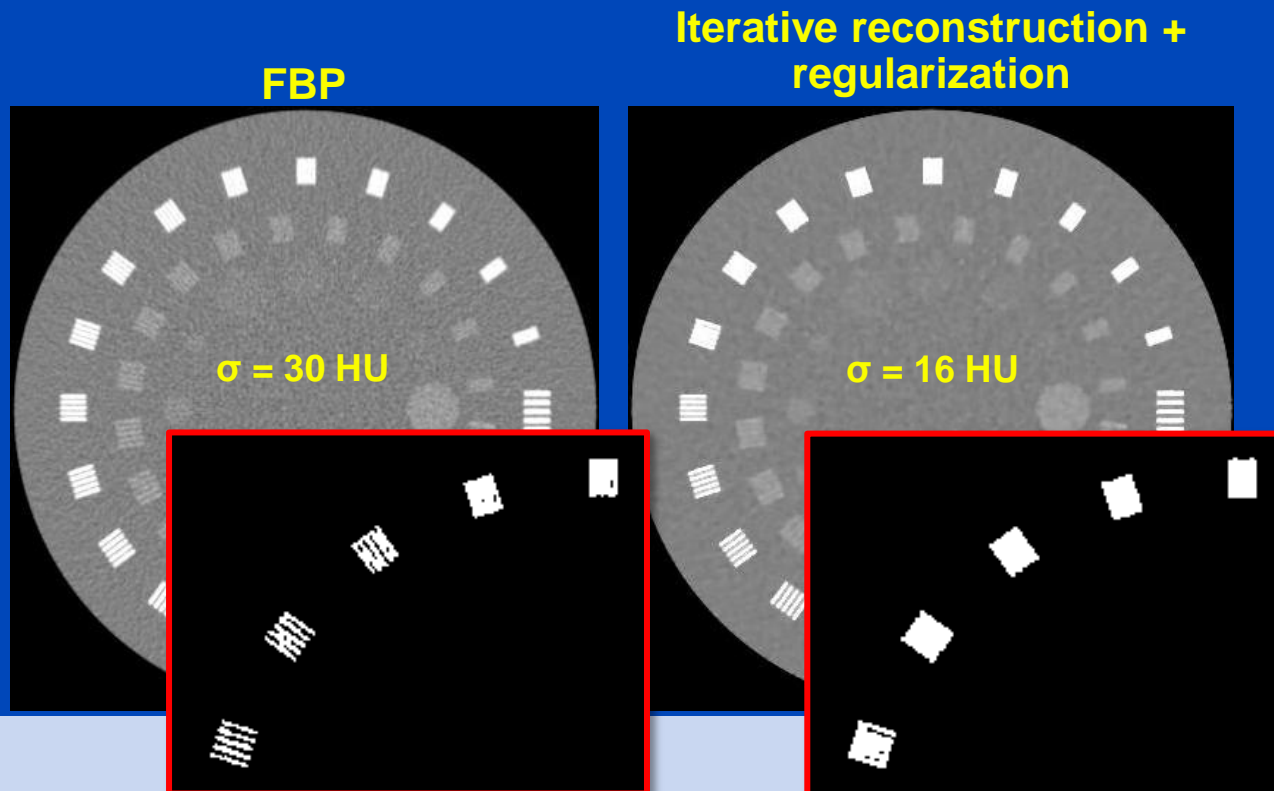
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Why Iterative Reconstruction?

- Iterative image reconstruction promises to reduce image noise (and thus patient dose), to reduce artifacts, or to improve spatial resolution.
- Works for all geometries with only small adaptations.
- Allows to model any effect of the rawdata acquisition process.
- Allows to incorporate prior knowledge like image properties such as smoothness and edges (regularization).

Motivation

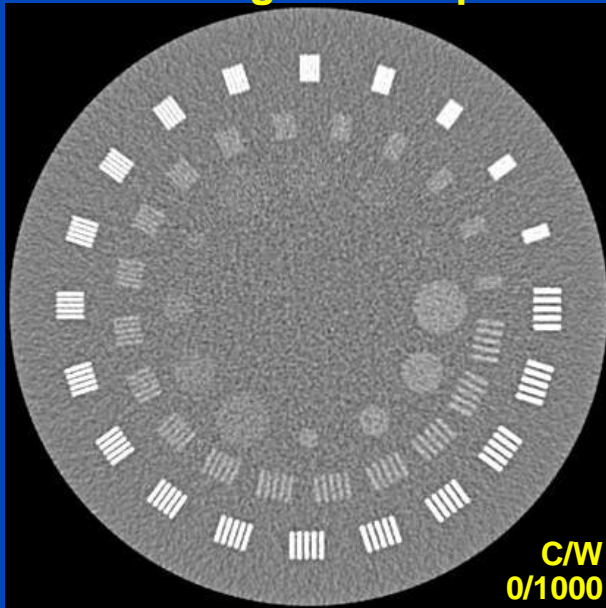
- Most common approach for regularization in iterative reconstruction:
Cost function = Rawdata fidelity + Penalty term (1) + Penalty term (2) ...
- In general the penalty terms penalize strong variations between neighboring voxels → the stronger the regularization the stronger the resolution-noise trade-off → problematic at the resolution limit or when the contrast of details is in the range of the noise level.
- Often many regularization parameters have to be chosen carefully to avoid an artificial image impression or not to alter anatomical information.



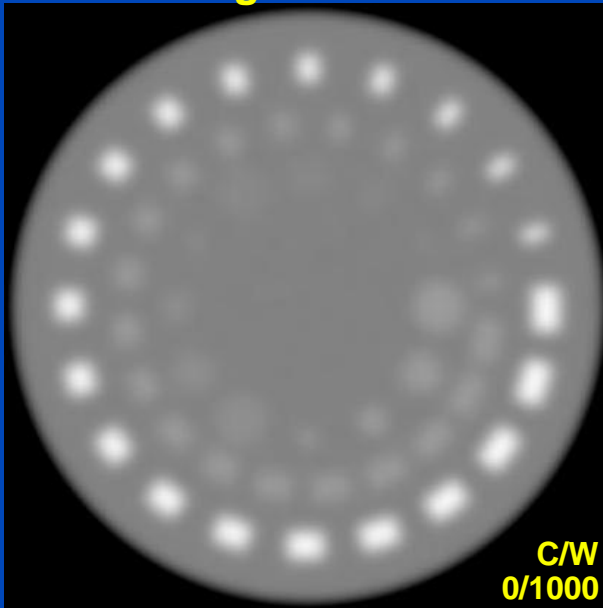
Aim

- To propose a different approach to regularization in iterative reconstruction which can improve the resolution noise trade-off.
- Basis images are generated which emphasize certain image properties like high resolution or low noise, etc. (regularization is incorporated by these basis images into the reconstruction process).
- We want to find the voxel-wise combination of the basis images to generate an image with superior resolution, and lower noise to improve the resolution noise trade-off.

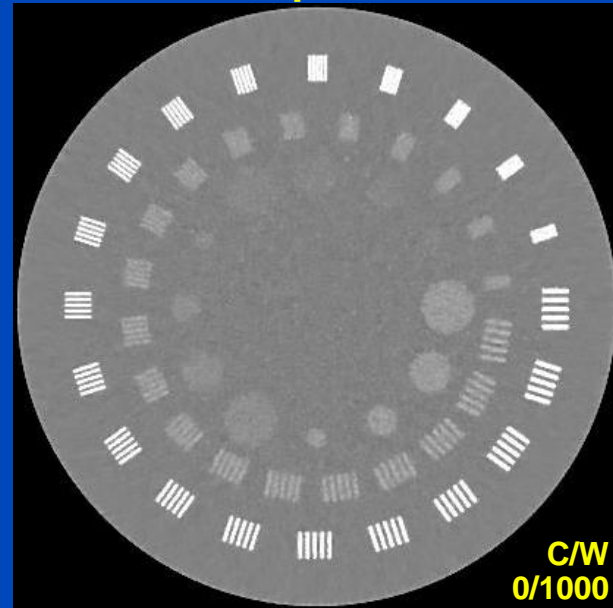
Basis image 1: Sharp FBP



Basis image 2: Smooth FBP



Proposed



Alpha Image Reconstruction (AIR)

- Generate basis images \rightarrow regularization is incorporated into the reconstruction by the basis images.
(e.g. regularized / filtered reconstructions, reference FBP reconstructions)
- Find the voxel-wise combination of these basis images best representing the real image by minimizing a cost function:

$$f_{\text{AIR}} = \sum_{b=1}^B \alpha_b \circ f_b, \quad \arg \min_{\alpha} \left\| R \cdot \left(\sum_{b=1}^B \alpha_b \circ f_b \right) - p \right\|_W^2 + U(\alpha)$$

- α_b = weighting images
- f_b = basis images
- $\alpha \circ f$ = Hadamard product
- B = Number of basis images
- R = Radon transform
- p = rawdata
- $U(\alpha)$ = regularization / constraints for α
- W = statistical weights

- Determine the α – images by minimizing the above cost function
 \rightarrow the minimum is reached when the weighting images α_b will have large contributions in regions of the corresponding f_b which highly correlate with the rawdata fidelity and low weighting otherwise.

Alpha Image Reconstruction (AIR)

- The regularization term is used to set certain constraints to the weighting images α_b such as continuity and smoothness:

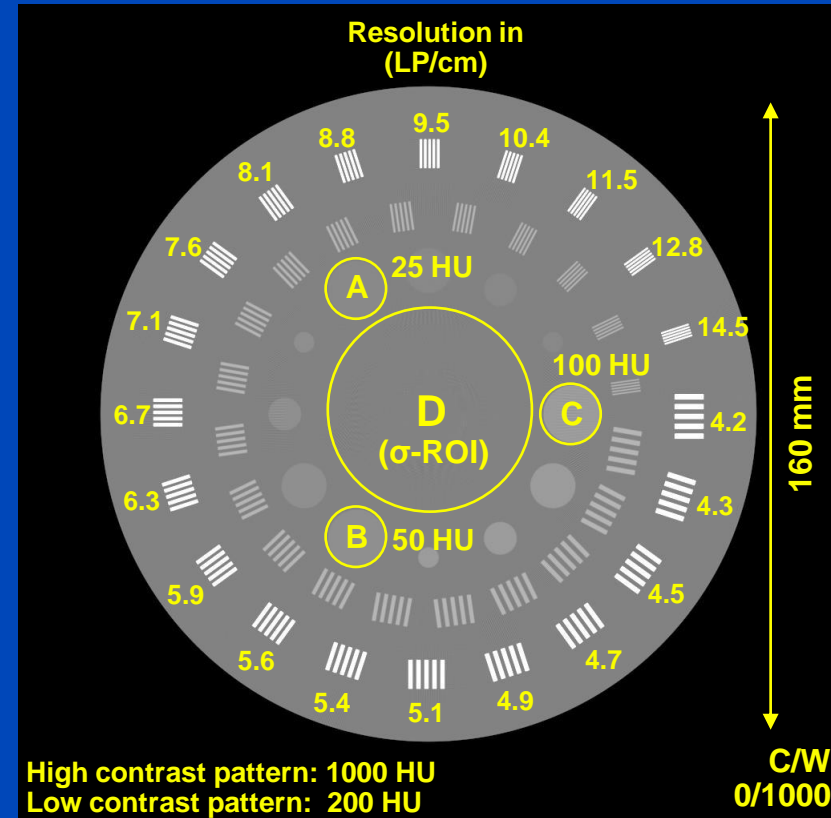
$$C(\alpha) = \underbrace{\|R \cdot \left(\sum_{b=1}^B \alpha_b \circ f_b \right) - p\|_{\mathbf{w}}^2}_{\text{convex}} + \underbrace{\beta \sum_{b=1}^B \text{TV}(\alpha_b)}_{\text{(1) convex}} + \underbrace{\gamma \sum_{b=1}^B \|\alpha_b - c_b\|_2^2}_{\text{(2) strictly convex}}$$

$U(\alpha)$

- (1) Total variation¹: smoothness in α_b .
- (2) Penalty which controls the average contribution one basis image has to the final result. We use $c_b = 1/B \rightarrow$ homogeneous regions without differences with respect to the rawdata fidelity are averaged.
- β and γ are trade-off parameters (chosen as small as possible).
- Overall cost function is strictly convex \rightarrow a unique global minimum exists.

Phantom

- Analytical phantom
- Diameter of water cylinder = 160 mm
- High contrast (1000 HU) and low contrast (200 HU) resolution patterns (4.2 – 14.5 LP/cm)
- Low contrast disk (100, 50, 25 HU)
- D = ROI for noise measurements
- A, B, C = ROIs for CNR measurements



Assessment of Image Quality

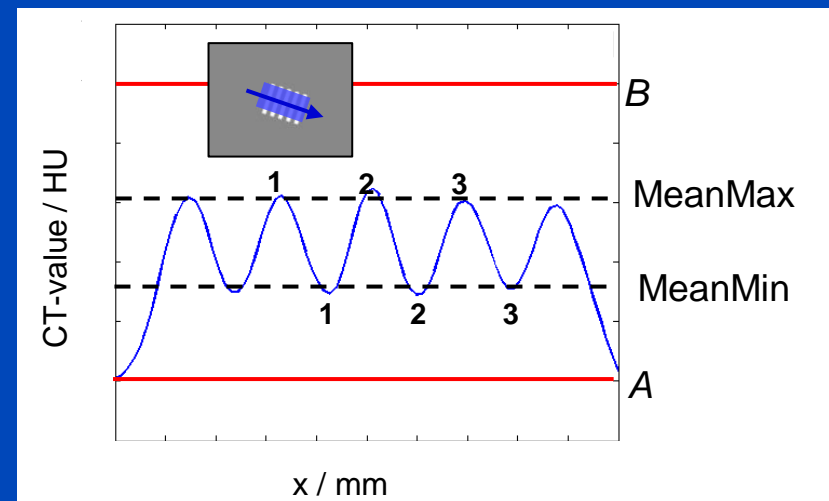
- Image quality was quantified by computing the normalized cross correlation with ground truth,

$$\text{NCC} = \frac{1}{L-1} \sum_{x,y \in \Omega} \frac{(f(x,y) - \bar{f})(g(x,y) - \bar{g})}{\sigma_f \sigma_g},$$

- f = reconstructed image, g = ground truth
 - σ_f, σ_g = corresponding standard deviations
 - Ω region for NCC analysis
- The resolution line patterns are analyzed using the contrast factor:

$$\text{CF} = \frac{\text{MeanMax}(i) - \text{MeanMin}(i)}{B - A},$$

- **MeanMax(i)** = mean of three inner maxima of resolution pattern i
- **MeanMin(i)** = mean of three inner minima of resolution pattern i
- **$B = 1000$ HU, $A = 0$ HU**



Compared Algorithms

- Ground truth:
 - noise-free ten-fold spatial resolution analytical reconstruction of our analytical phantom
- FBP:
 - Ram-Lak kernel (ramp filter till Nyquist frequency)
- PWLS with TV: $C_{\text{PWLS-TV}}(\mathbf{f}) = \|\mathbf{R} \cdot \mathbf{f} - \mathbf{p}\|_{\mathbf{W}}^2 + \eta \text{TV}(\mathbf{f})$
 - PWLS (Penalized weighted least squares): most attention in penalized CT literature
 - TV: also most attention in CT literature and only few parameters → results easy to comprehend etc.
- AIR: $C(\boldsymbol{\alpha}) = \|\mathbf{R} \cdot \left(\sum_{b=1}^B \alpha_b \circ \mathbf{f}_b \right) - \mathbf{p}\|_{\mathbf{W}}^2 + U(\boldsymbol{\alpha})$
 - Two basis images:
 - $\mathbf{f}_1 = \text{FBP}$, $\mathbf{f}_2 = \text{smooth FBP (FBP + Gaussian filtering)}$
 - Three basis images + anisotrop bilateral filtering¹:
 - $\mathbf{f}_1 = \text{FBP}$, $\mathbf{f}_2 = \text{FBP bilateral filtered}$, $\mathbf{f}_3 = \text{sharp FBP bilateral filtered}$

[1]C. Tomasi and R. Manduchi, “Bilateral filtering for gray and color images,” Proc. 6th Int. Conf. Computer Vision, pp. 839–846, 1998.

Simulation and Reconstruction Setting for Phantom Simulations

Rawdata:

- Siemens SOMATOM Definition Flash Geometry
- $N_{360} = 1160$
- Poisson noise was simulated resulting in 30 HU noise in the FBP reconstruction in water-equivalent tissue.
- Monochromatic rawdata at 80 keV

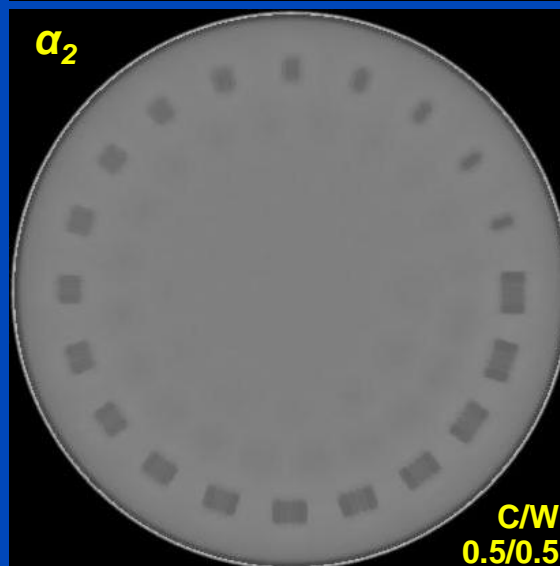
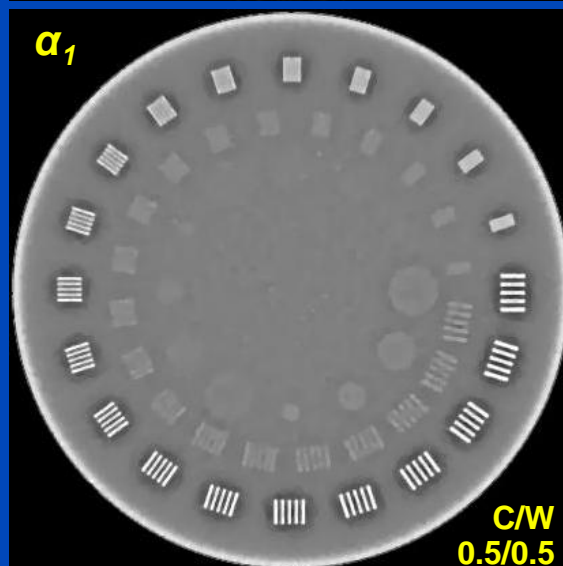
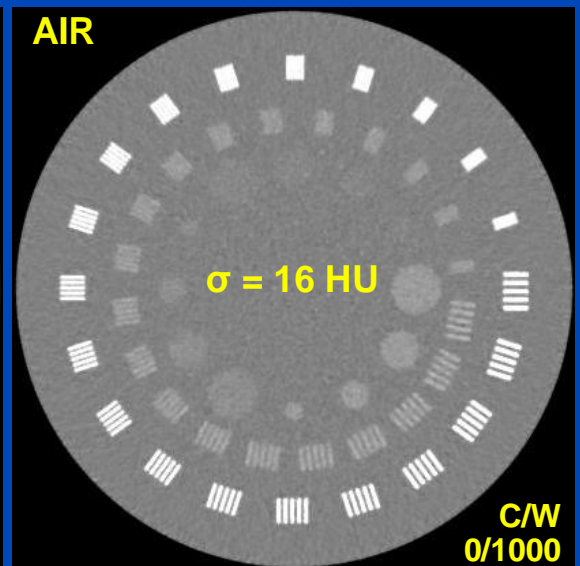
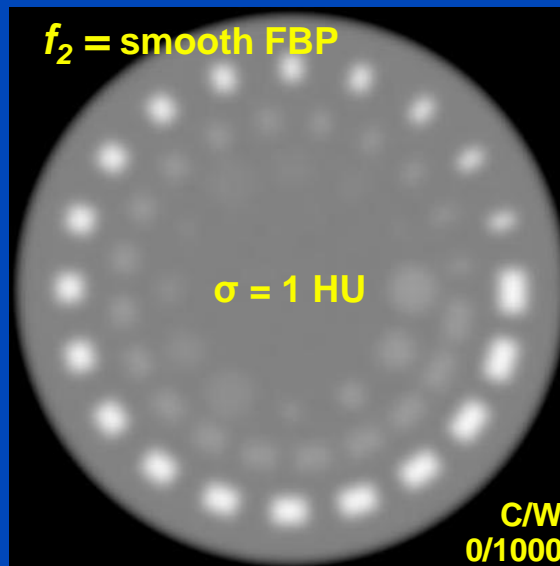
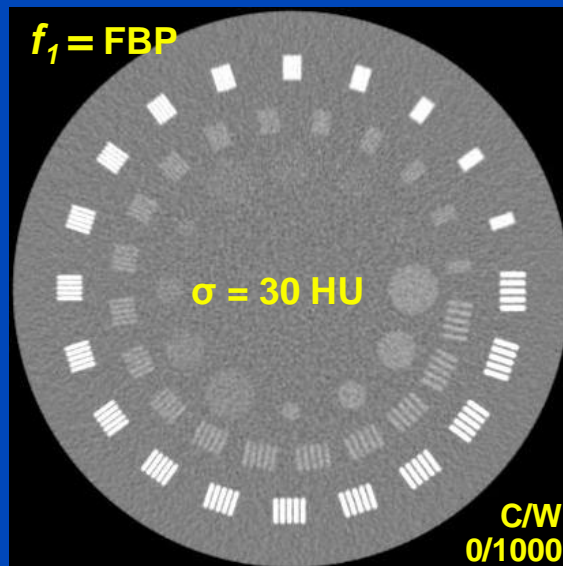
Reconstruction setting:

- Field of view = 200 mm
- $N_x = N_y = 512 \rightarrow \Delta x = \Delta y = 0.4$ mm

Algorithm parameters for the proposed method:

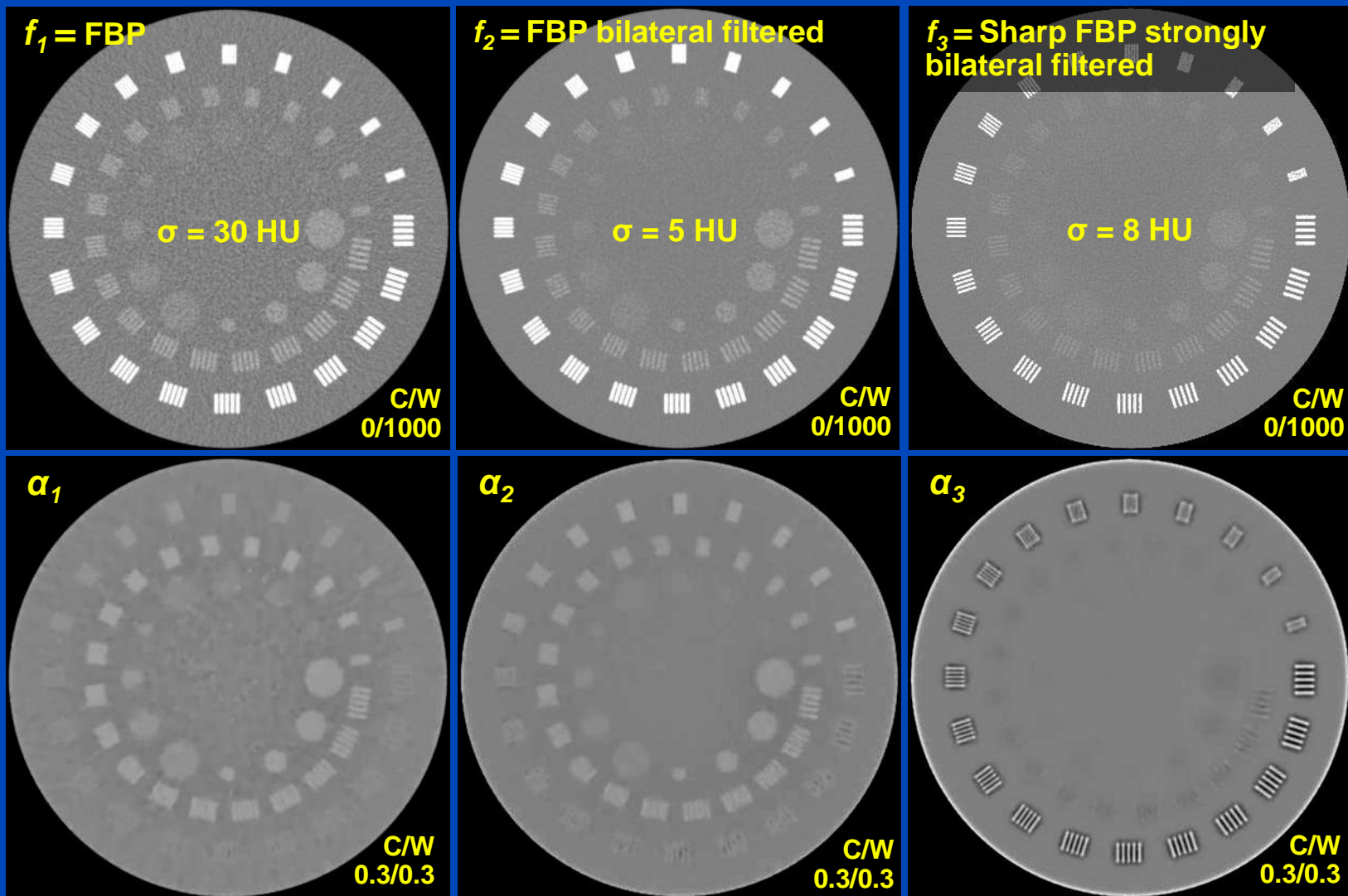
- $\beta = 0.001$, $\gamma = 0.02$, α initialized with zero
- Minimization of cost function: Gradient descent with backtracking line search
- $N_{\text{iter}} = 500$ (convergence: iterated until no significant changes during further iterations)

TWO BASIS IMAGES

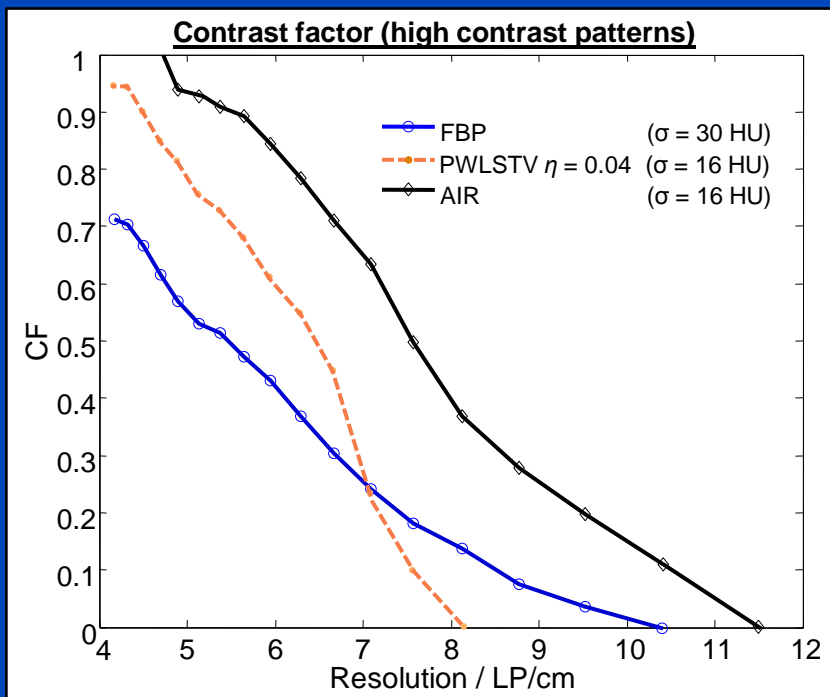
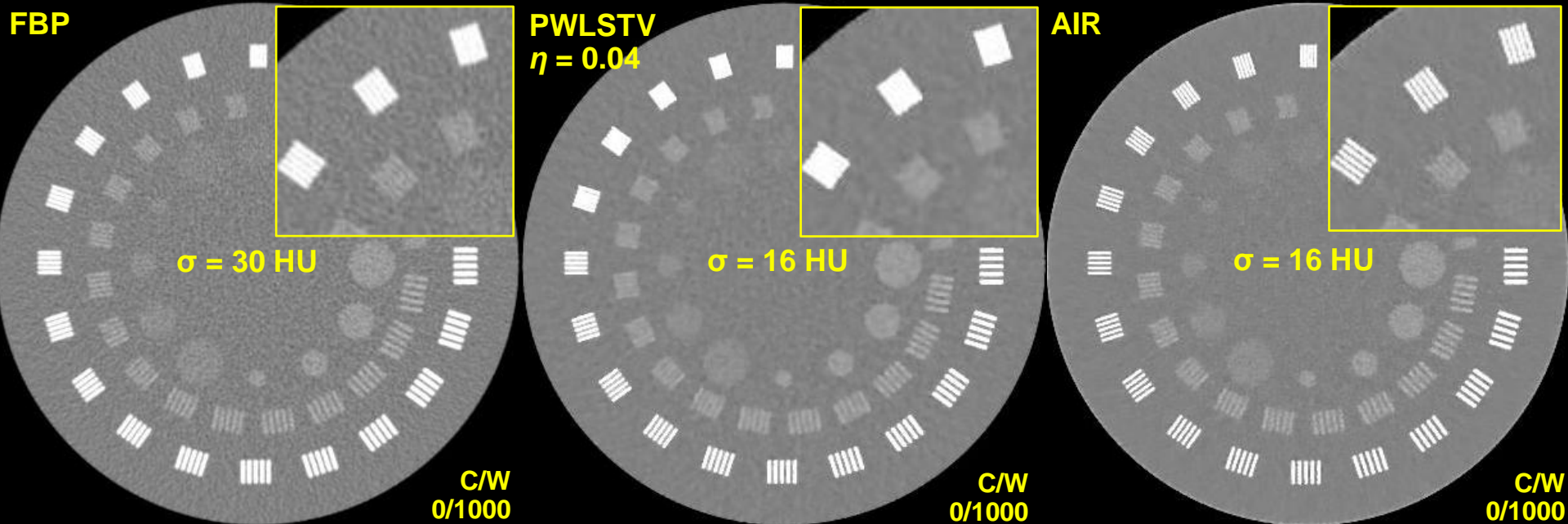


- High weights in regions which highly correlate with the rawdata fidelity
- Low weights in regions with low correlation
- Regions which have the same correlation with the rawdata are averaged

THREE BASIS IMAGES WITH BILATERAL FILTERING



- Low contrast detail information has the highest correlation with the ground truth in basis images f_1 and $f_2 \rightarrow$ weights are high in α_1 and α_2 .
- High contrast detail information has the highest correlation with the ground truth in basis images $f_3 \rightarrow$ weights are high in α_3 .

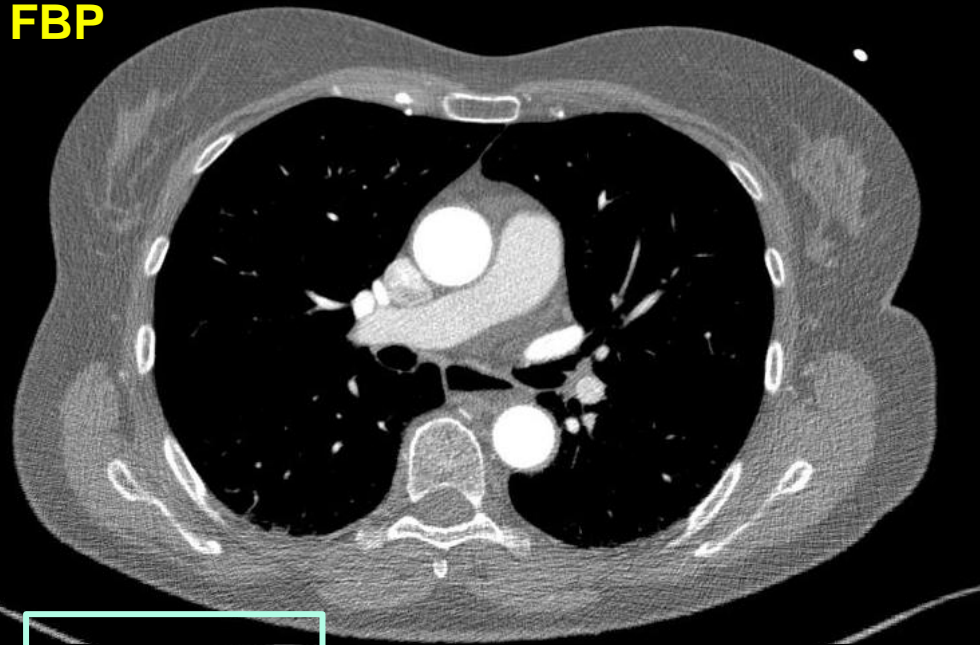


Proposed method has the highest correlation with the ground truth:

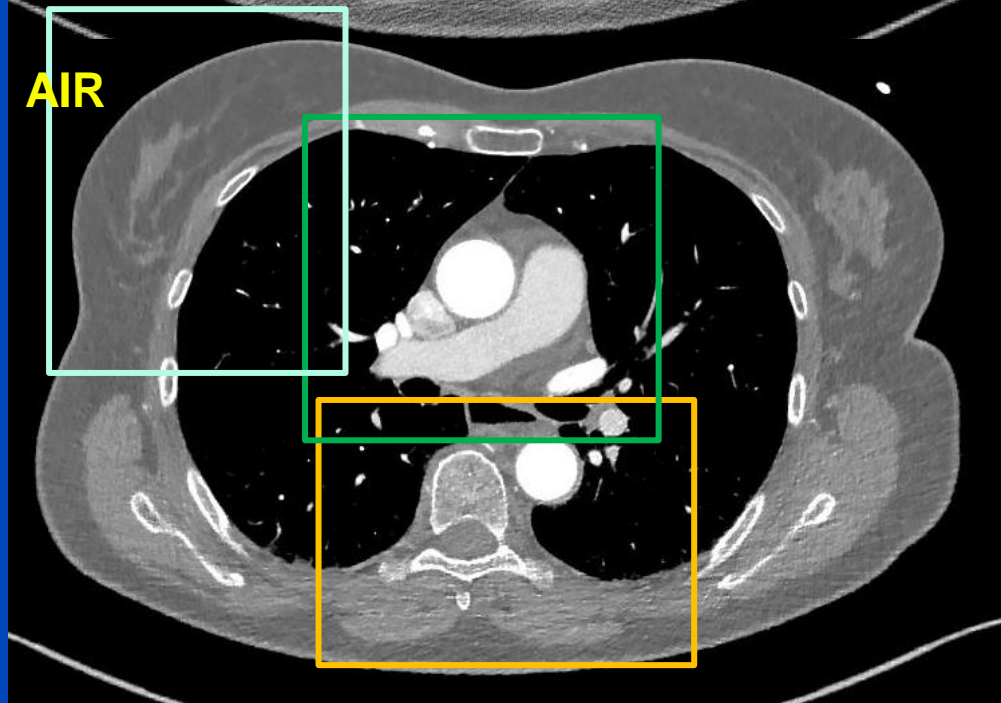
$$NCC_{\text{FBP}} \ 0.920 \ < \ NCC_{\text{PWLSTV}} \ 0.955 \ < \ NCC_{\text{AIR}} \ 0.971$$

PATIENT DATA

FBP



AIR



Rawdata:

- Siemens SOMATOM Definition Flash Scanner
- Sequence scan, single source
- Scan parameters: $N_{360} = 1160$, tube voltage = 100 kV

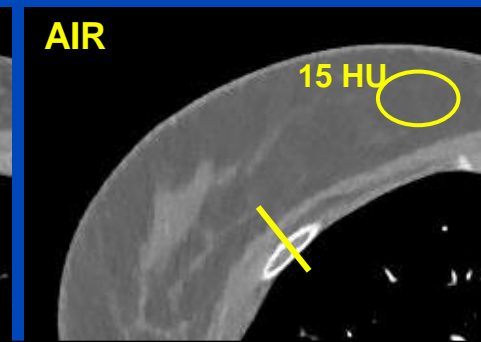
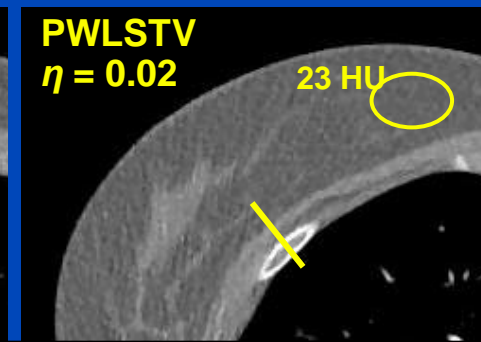
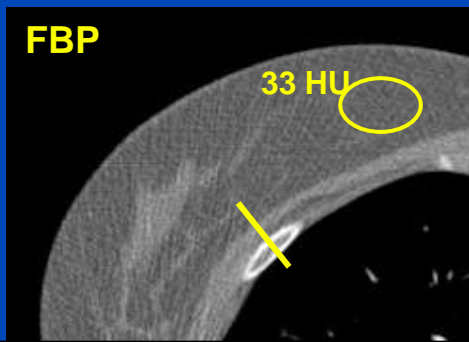
Reconstruction setting:

- Field of view = 500 mm
- $N_x = N_y = 1024$
→ $\Delta x = \Delta y = 0.5$ mm

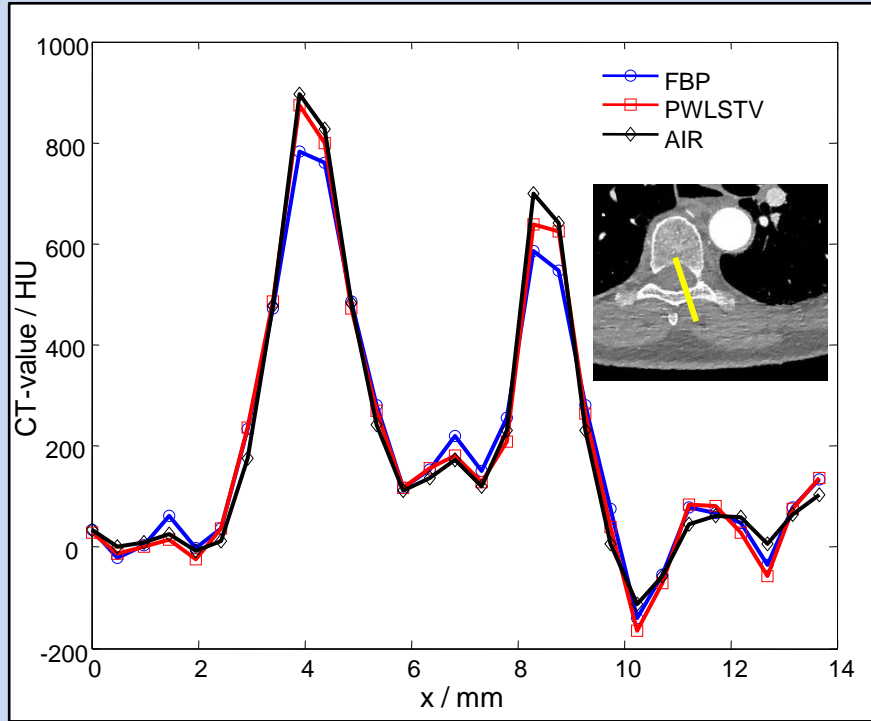
Parameters for proposed method:

- Same parameters as for the phantom
- AIR with three basis images and bilateral filtering

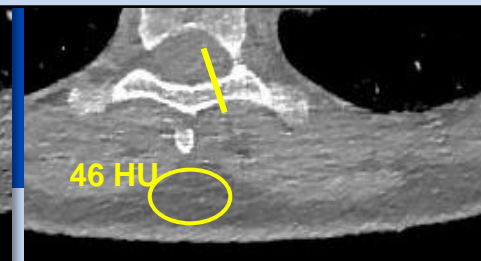
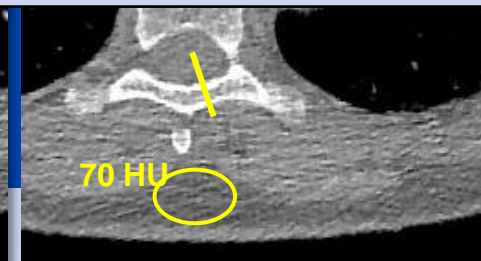
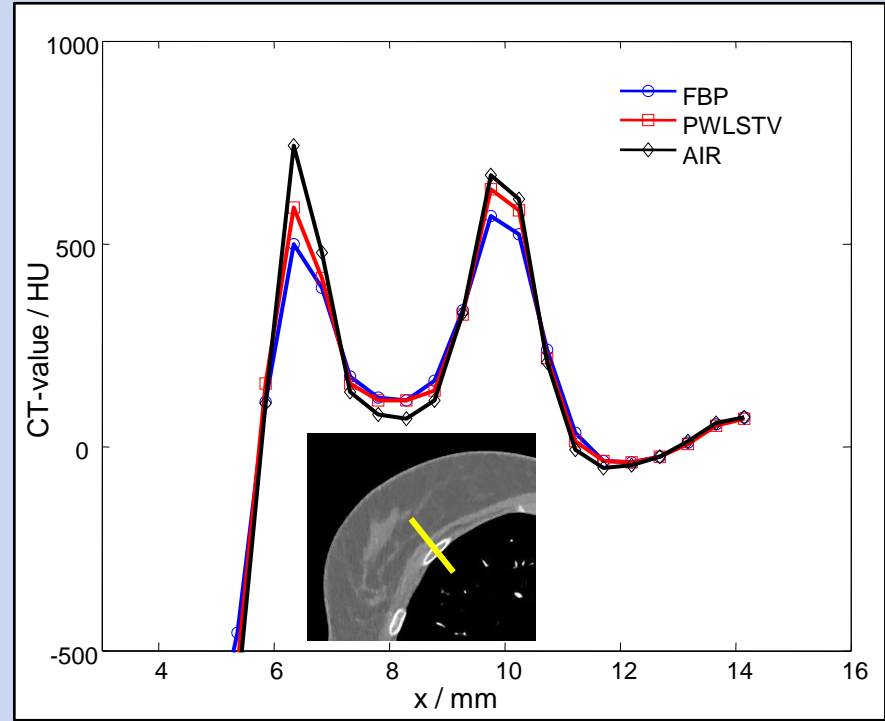
C = 0 HU, W = 1000 HU



Line profile through vertebra



Line profile through Rib



C = 0 HU
W = 1000 HU

Summary & Conclusion

- In our experiments the AIR algorithm reduces noise by up to 50% and at the same time has the potential to improve the resolution.
- Any image filter or regularization approach can be used to generate the basis images which makes the method very flexible.
- Future research will be concerned with finding optimal choices for the basis images.
- **Outlook – Special application cardiac CT**
Basis images:
 - Sharp FBP to avoid blooming
 - FBP with high temporal resolution and low CNR
 - FBP with low temporal resolution and high CNR

Thank You!

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This presentation will soon be available at www.dkfz.de/ct.