

# Deep Learning in CT Image Formation



**Marc Kachelrieß**

**German Cancer Research Center (DKFZ)**

**Heidelberg, Germany**

**[www.dkfz.de/ct](http://www.dkfz.de/ct)**



**DEUTSCHES  
KREBSFORSCHUNGSZENTRUM  
IN DER HELMHOLTZ-GEMEINSCHAFT**

# Fully Connected Neural Network

- Each layer fully connects to previous layer
- Difficult to train (many parameters in  $W$  and  $b$ )
- Spatial relations not necessarily preserved

Input

Hidden

Hidden

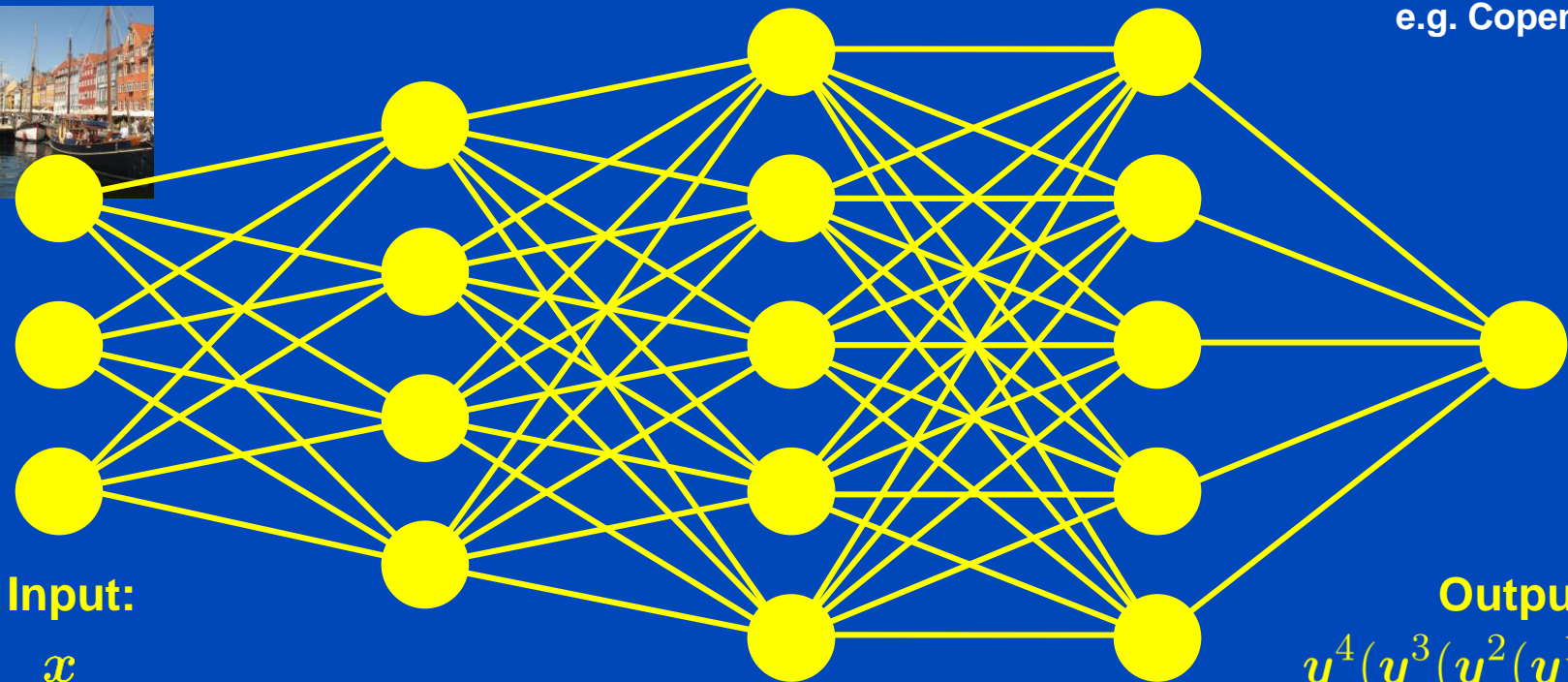
Hidden

Output

e.g. 512x512x3 pixels  
e.g.



e.g. 1 label  
e.g. Copenhagen

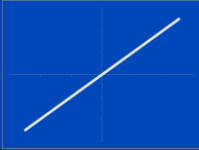

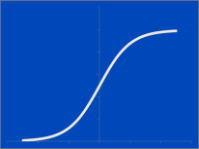
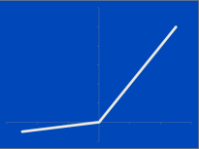

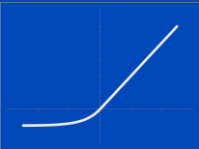

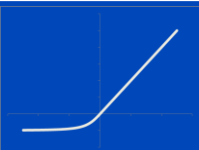
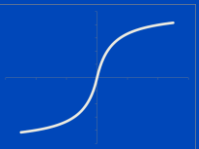
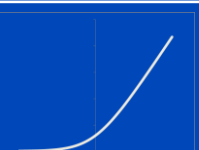


Input:  
 $x$

Output:  
 $y^4(y^3(y^2(y^1(x))))$

$y(x) = f(W \cdot x + b)$  with  $f(x) = (f(x_1), f(x_2), \dots)$  point-wise scalar, e.g.  $f(x) = x \vee 0 = \text{ReLU}$

# Activation Functions

Function	Equation	Plot	Function	Equation	Plot
Identity	$f(x) = x$		ReLU	$f(x) = \begin{cases} 0 & \text{for } x < 0 \\ x & \text{for } x \geq 0 \end{cases}$	
Sigmoid	$f(x) = \frac{1}{1 + e^{-x}}$		Leaky ReLU	$f(x) = \begin{cases} \alpha x & \text{for } x < 0 \\ x & \text{for } x \geq 0 \end{cases}$	
Hard sigmoid	$f(x) = \begin{cases} 0 & \text{for } x < -\alpha \\ \frac{\alpha+x}{2\alpha} & \text{for } -\alpha \leq x < \alpha \\ 1 & \text{for } x \geq \alpha \end{cases}$		ELU	$f(x) = \begin{cases} \alpha(e^x - 1) & \text{for } x < 0 \\ x & \text{for } x \geq 0 \end{cases}$	
Tanh	$f(x) = \frac{2}{1 + e^{-2x}} - 1$		Inverse square root LU	$f(x) = \begin{cases} \frac{x}{\sqrt{1+\alpha x^2}} & \text{for } x < 0 \\ x & \text{for } x \geq 0 \end{cases}$	
Softsign	$f(x) = \frac{x}{1 +  x }$		...	...	...
Softplus	$f(x) = \log(1 + \exp x)$				

# Gradient Descent

- Walk along the direction of the negative gradient
- Steepest descent
- Learning rate  $\eta$

$$w^{\text{new}} = w^{\text{old}} - \eta \nabla_w L(x_n, y_n, w)$$

- Easy to understand, but not optimal
- Methods in use
  - Batch gradient descent
  - Stochastic gradient descent
  - Mini-batch gradient descent
  - Conjugate gradient descent
  - Quasi Newton methods
  - Momentum methods
  - ...

# Convolutional Neural Network (CNN)

- Replace dense  $W$  in  $y(x) = f(W \cdot x + b)$  by a sparse matrix  $W$  with sparsity being of convolutional type.
- CNNs consist (mainly) of convolutional layers.
- Convolutional layers are not fully connected.
- Convolutional layers are connected by small, say  $3 \times 3$ , convolution kernels whose entries need to be found by training.
- CNNs preserve spatial relations to some extent.

Src  
 $512 \times 512 \times F$

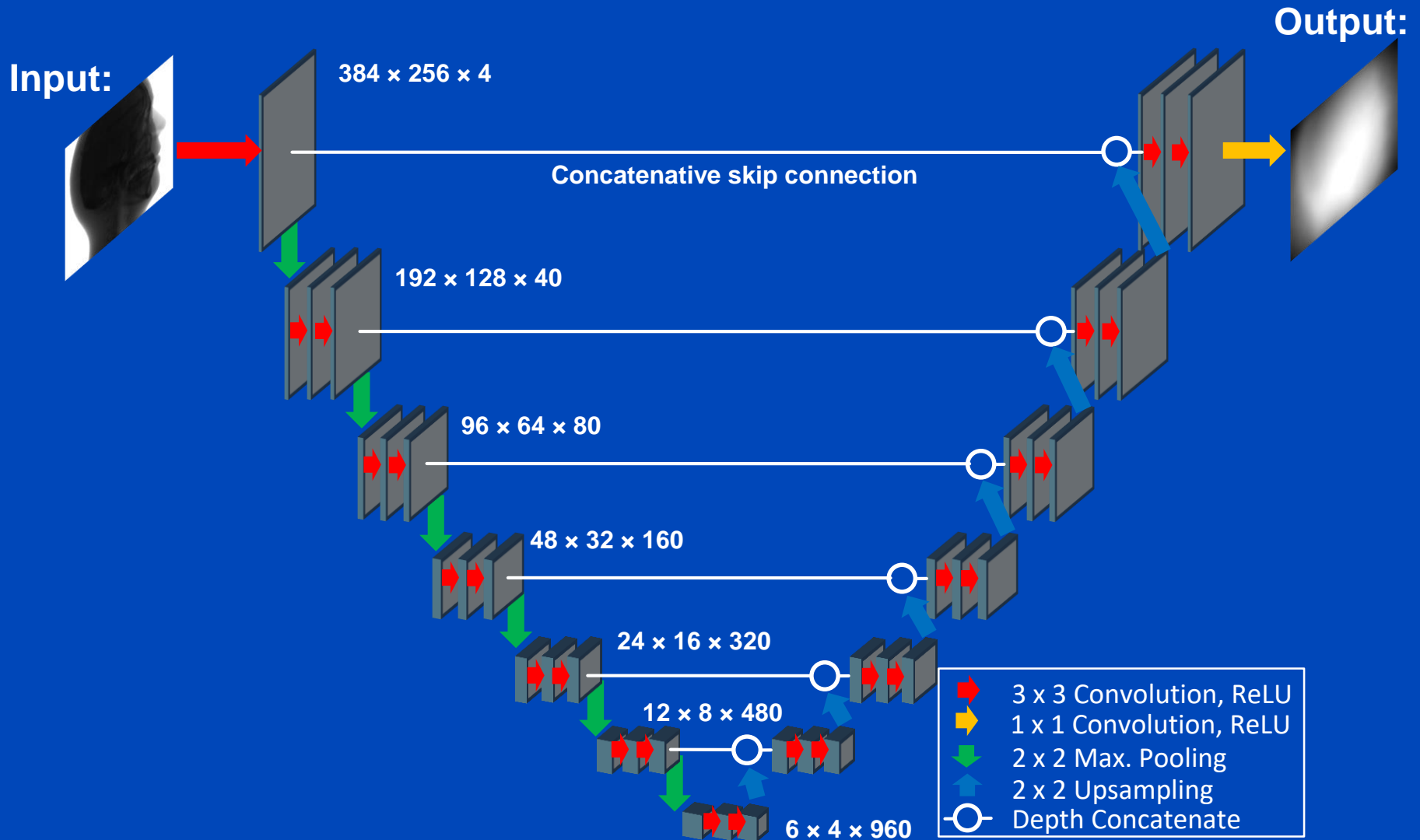
Dst  
 $512 \times 512 \times G$

$G$  kernels  
 $3 \times 3 \times F$

$$D_{i,j,g} = \sum_f S_{i,j,f} * K_{i,j,f}^g = \sum_{a,b,f} S_{i-a,j-b,f} K_{a,b,f}^g$$

Attention: No convolution in depth direction!

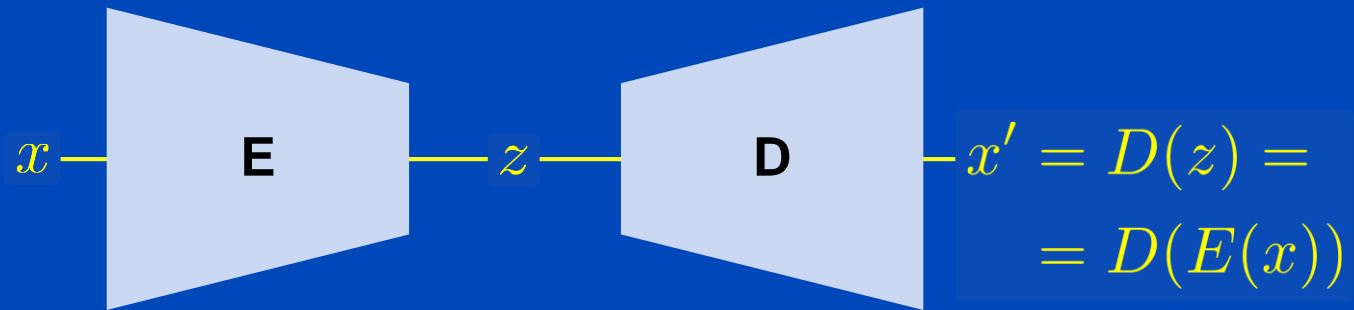
# U-Net<sup>1</sup>



<sup>1</sup>O. Ronneberger, P. Fischer, and T. Brox. U-net: Convolutional networks for biomedical image segmentation. Proc. MICCAI:234-241, 2015.

# What is an Autoencoder?

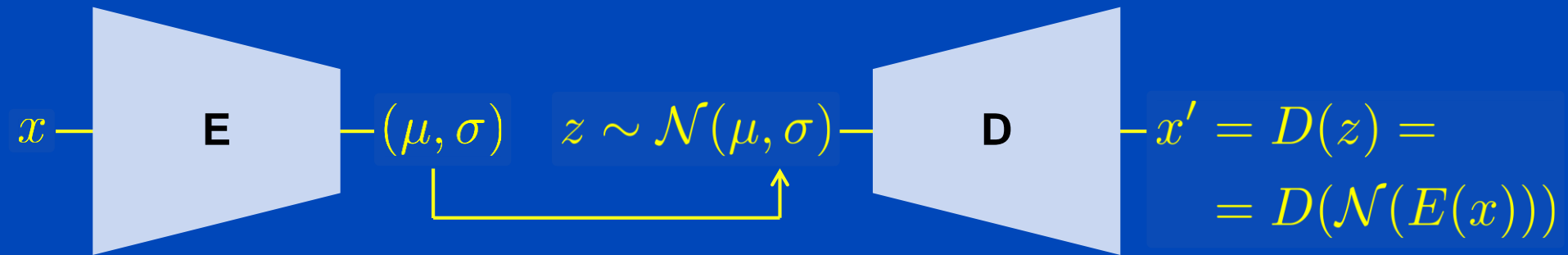
- In and output domain are the same, here  $x$ .
- Bottleneck  $z$  enforces the encoder and decoder to do a good job.



- **Examples:**
  - Principal component analysis (linear autoencoder), lossless
  - PCA with dimensionality reduction (nonlinear due to clipping), lossy
  - Image compression and decoding, e.g. jpeg, lossy
- Latent space typically not interpretable.

# What is a Variational Autoencoder?

- Make latent space regular.
- Allow to sample in latent space from a given distribution, here: normal distribution.



- The VAE is a generative model.
- It allows to generate new data by sampling new values from the normal distribution.



# Loss Function

- The neural network parameters (weights and biases)  $w$  are chosen by minimizing a loss function (cost function)

$$w = \arg \min_w \sum_{n=1}^N L(x_n, y_n, w)$$

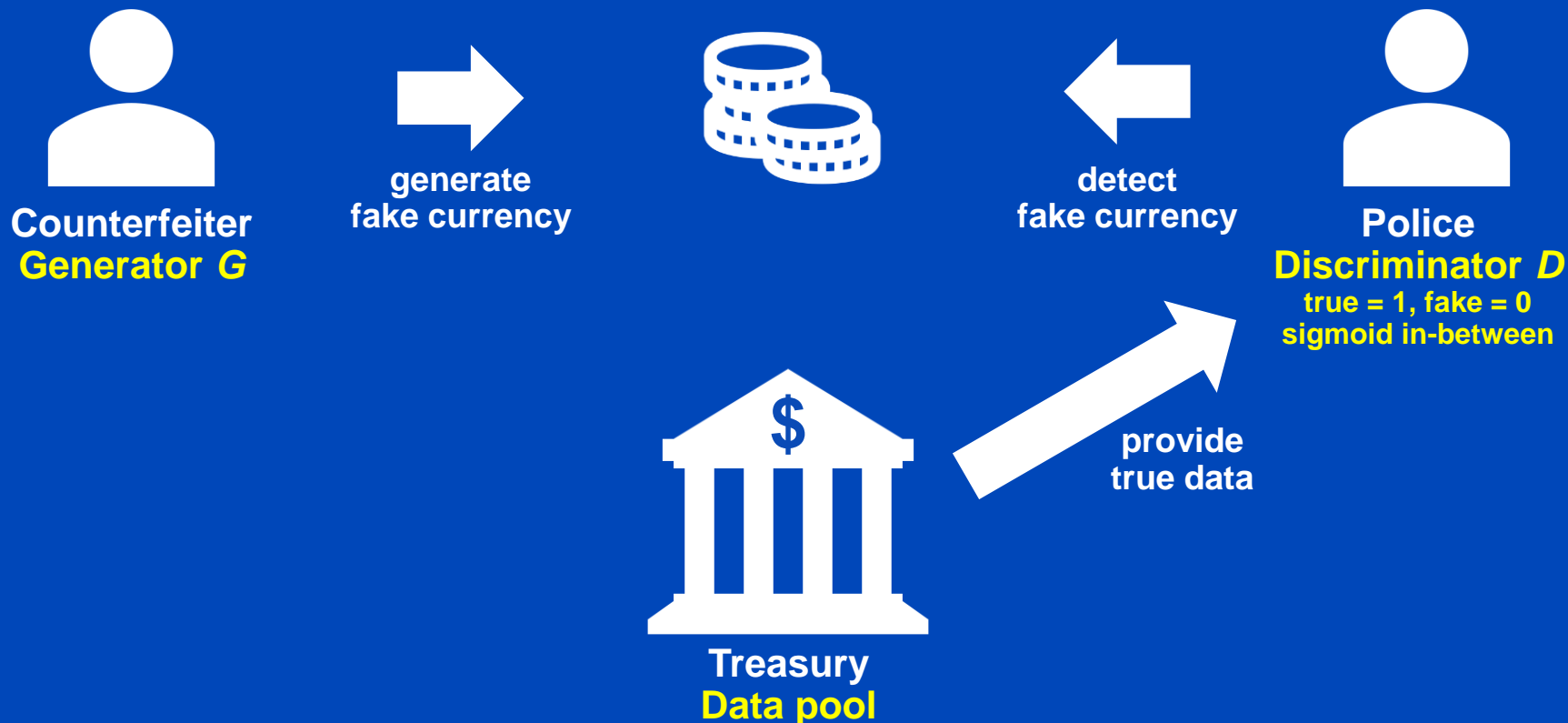
with  $x_n$  being the training data input,  $y(x_n, w)$  being the network output, and  $y_n$  being the so-called labels, i.e. the training target, and  $N$  being the number of training samples.

- An example for such a loss function is the MSE loss

$$L(x_n, y_n, w) = (y(x_n, w) - y_n)^2$$

# Generative Adversarial Network<sup>1</sup> (GAN)

- Useful, if no direct ground truth (GT) is available, the training data are unpaired, unsupervised learning



<sup>1</sup>I. Goodfellow et al. Generative Adversarial Nets, arXiv 2014

# Generative Adversarial Network (GAN)

- Typical loss function and minimax game:

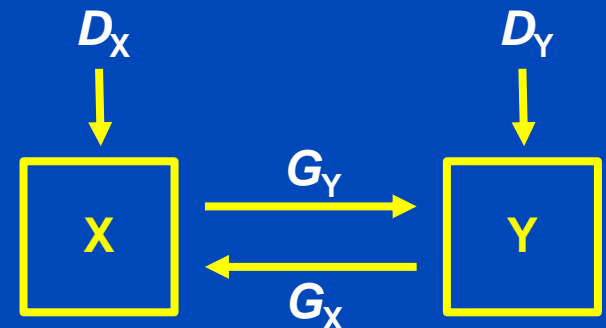
$$\min_G \max_D L(D, G) := E_x \ln (1 - D(G(x))) + E_y \ln D(y)$$

- Conditional GAN<sup>1</sup>

- Conditional GANs sample the generator input  $x$  not from a uniform distribution but from a conditional distribution, e.g. noisy CT images.
- Need some measure to ensure similarity to input distribution (e.g. pixelwise loss added to the minimax loss function)

- Cycle GAN<sup>2</sup>

- Two GANs ( $X \rightarrow Y$  and  $Y \rightarrow X$ )
- Demand cyclic consistency, i.e.  $x = G_X(G_Y(x))$  and  $y = G_Y(G_X(y))$



<sup>1</sup>Isola et al. 2017

<sup>2</sup>Zhu et al., 2017

# Deep MAR Examples

### Reducing Metal Streak Artifacts in CT Images via Deep Learning: Pilot Results

Lei Gengyi, Qingyao Yang, Tao Xu, Baohua Chen, Xiaohu Fu, Binbin Du, Ma Guoqiang

- Takes 32x32 input patch from NMAR image and produces 20x20 output patch
- Very basic CNN

### Gjesteby, 2017

- Same network as in previous work
- Detail image is the high-pass filtered original image
- Detail image and NMAR image are both put as inputs in 2 streams that converge later in the CNN
- Network uses residual error and cost function is a combination of MSE and perceptual loss

### Deep Neural Network for CT Metal Artifact Reduction with a Perceptual Loss Function

Lei Gengyi, Qingyao Yang, Tao Xu, Baohua Chen, Xiaohu Fu, Binbin Du, Ma Guoqiang

### Gjesteby, 2018

- Inputs for the network are the NMAR image and the high-pass filtered original image
- Corrects streaks after NMAR
- Loss function is MSE or perceptual loss (from VGG network)
- SE blocks over something like a residual error

### Gjesteby, 2018

### A dual-stream deep convolutional network for reducing metal streak artifacts in CT images

Lei Gengyi, Qingyao Yang, Qingyao Yang, Tao Xu, Binbin Du, Xiaohu Fu, Baohua Chen, Ma Guoqiang

### Gjesteby, 2019

### Gjesteby, 2019

### Gjesteby, 2019

### Metal artifact reduction for practical dental computed tomography by improving interpolation-based reconstruction with deep learning

Xiaohu Fu, Li Zhang, and Yongqiang Yang

### Xing, 2019

- Perform initial LIMAR to obtain images with interpolation artifacts
- Apply U-Net to pre-corrected images to reduce artifacts
- Network minimizes L2-norm loss outside of the metal regions

### Xing, 2019

### Metal artifact reduction on cervical CT images by deep residual learning

Qi Huang<sup>1</sup>, Jian Wang<sup>1</sup>, Fan Tang<sup>1</sup>, Tao Zhang<sup>2</sup> and Yu Zhang<sup>1</sup>

### Zhang, 2018

### Zhang, 2018

- Metal is placed in real CT images. Artifacts are created by forward and back-projecting soft tissue, bone, and metal
- Network input is patch of artifact image I and output is the residual, i.e.  $R = I - G_I$
- Loss function is MSE of the residual
- Learning the residual is found to be better than learning the artifact-free image (no images)

### Convolutional Neural Network Based Metal Artifact Reduction in X-Ray Computed Tomography

Nanhe Zhang<sup>1</sup>, Senan Member, IEEE, and Hongyong Yu<sup>1</sup>, Senior Member, IEEE

### Yu, 2018

### Yu, 2018

- Training data are generated from clinical data with metal artifacts added afterwards through polychromatic forward- & back-projection
- Cost function is MSE
- CNN gets patches from the artifact BHC corrected, and LI corrected image as input, produces corrected patches
- Prior image is generated from CNN result by segmenting water and setting it to the average value of all water pixels and leaving bones intact
- Metal trace in the uncorrected sinogram is replaced with values from the prior image
- Having different types of MAR as input improves results

### Metal-Artifact Reduction Using Deep-Learning Based Sinogram Completion: Initial Results

Richard E. Cole, Yuesha Li, A. Gengyi, Qi Yang, Binbin Du

### Claus, 2017

- Trained and evaluated on simulated data with metal circle in the center (no other positions tested)
- Data are heavily simplified (random ellipses)
- Inputs are 2 81x21 sized patches from the sinogram next to metal patch. Won't work for complex metals
- Relatively small network (4 layers)

### Deep Learning Based Metal inpainting in the Projection Domain: Initial Results

Binbin Du, Gengyi Geng, Jijun W. Kruger, Balder Koenig, and Andrew Mauer

### Gottschalk, 2019

- Corrects C-Arm projection data
- Data were obtained by placing metal on top of human knee cadavers
- Loss function is MSE
- Networks are based on U-Net with additional skip connection from original image to output
- Basic network can be used to implicitly segment the metal for the Mask-MAR-Net
- Providing a metal mask significantly improves results
- Results are blurred slightly

### Gottschalk, 2019

### Gottschalk, 2019

### Deep Learning based Metal Inpainting in the Projection Domain using additional Neighboring Projection Information

Binbin Du, Gengyi Geng, Jijun W. Kruger, and Andrew Mauer

### Gottschalk, 2020

- U-Net corrects CBCT projections
- Has metal mask and 10 neighbouring projections as additional input channels

### Gottschalk, 2020

### Fast Enhanced CT Metal Artifact Reduction using Data Domain Deep Learning

Muhammad Usman Ghani, W. Chen, Karl, Felton, 2022

### Ghani, 2019

- Metal trace is replaced via a CGAN
- Uses transfer learning from training data to real data; not described in depth
- Not applied to medical images

### Ghani, 2019

### Generative Mask Pyramid Network for CT/CBCT Metal Artifact Reduction with Joint Projection-Sinogram Correction

Huili Liao<sup>1</sup>, Wei An Liu<sup>1</sup>, Zhiliang Han<sup>1</sup>, Lixun Yin<sup>1,2</sup>, William J. Sekerac<sup>3</sup>, Si Kevin Zhou<sup>1</sup>, and Jiebo Luo<sup>1</sup>

### Liao, 2019

### Liao, 2019

- First replaces metal trace in the projections (i.e. fixed angle but varying  $\xi$  and  $z$ )
- Then transforms the projections into sinograms and uses a second network to improve those
- Both networks are GANs with a U-Net generator and CNN discriminator
- Uses a Mask Pyramid to ensure the metal mask is seen by all stages of the U-Net
- Data are regular CT scans with metal traces from other patients imposed on them

### DuoNet: Dual Domain Network for CT Metal Artifact Reduction

Wei An Liu<sup>1</sup>, Huili Liao<sup>1</sup>, Cheng Peng<sup>1</sup>, Xiaohua Guo<sup>1</sup>, Jiebo Luo<sup>1</sup>, Jiebo Luo<sup>1</sup>, Rana Chellappa<sup>1</sup>, Shaohua Kevin Zhou<sup>1</sup>

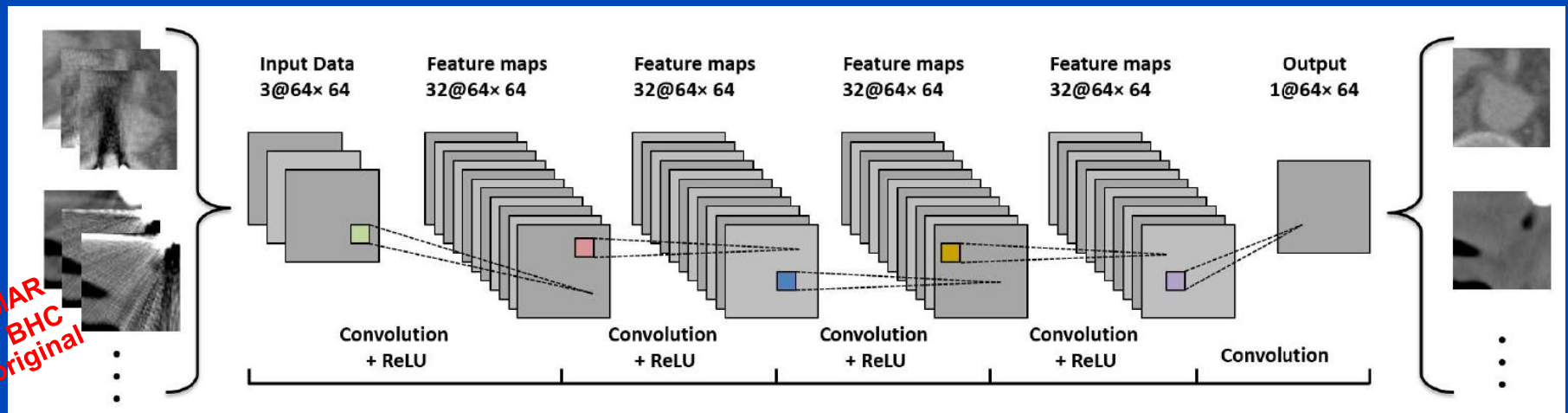
### Lin, 2019

### Lin, 2019

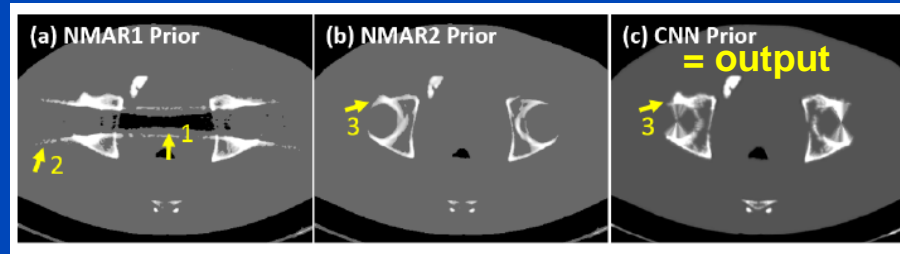
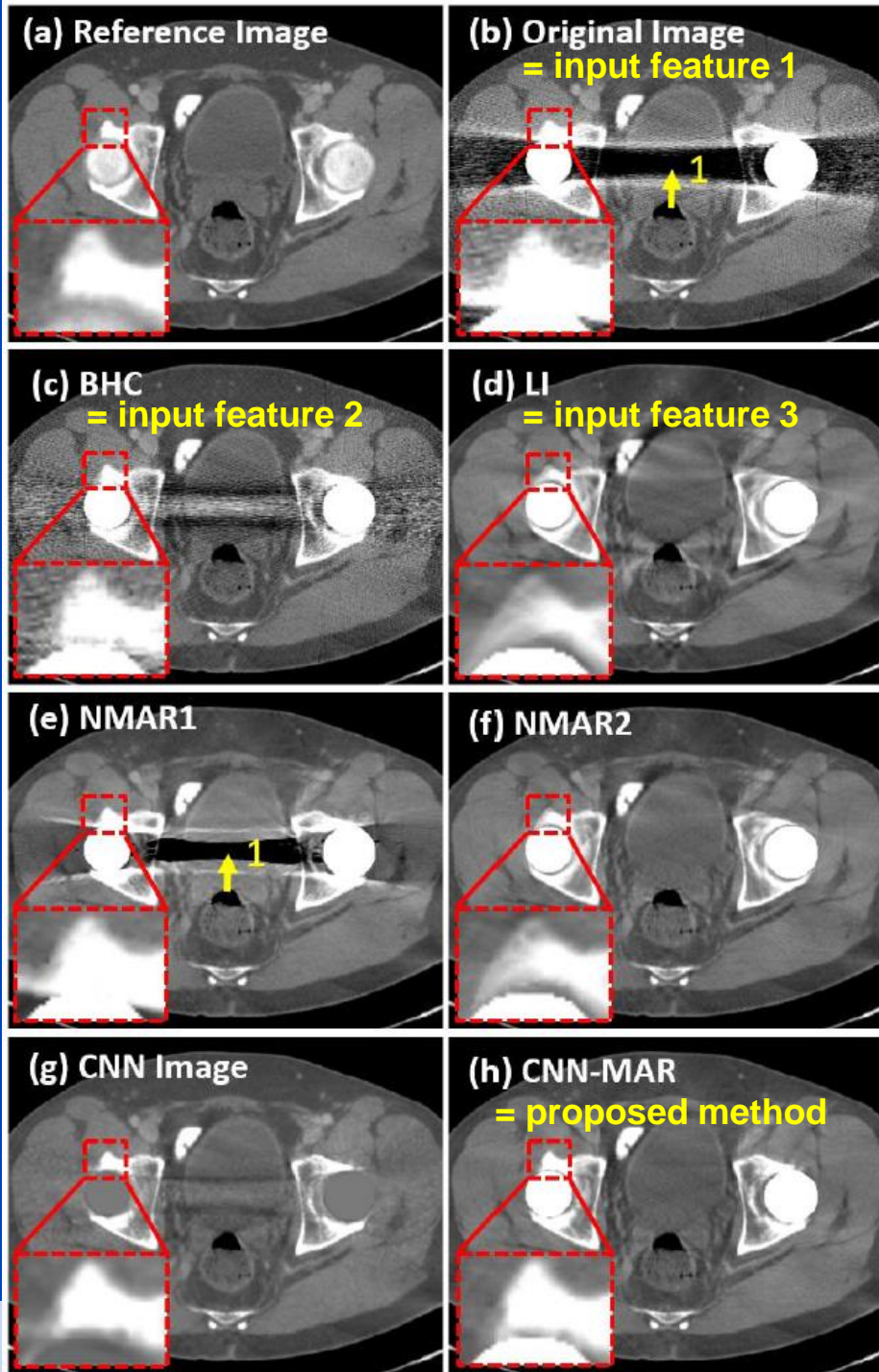
- Input are LI pre-corrected sinograms/images
- First improves the sinograms through a U-Net with mask pyramid (so all parts of the U-Net see the mask)
- Then applies FBP (Radon Inversion Layer) and uses the result as input for a second U-Net, which improves it in image domain
- Unclear how/when the LI and CNN results are combined

# MAR Example

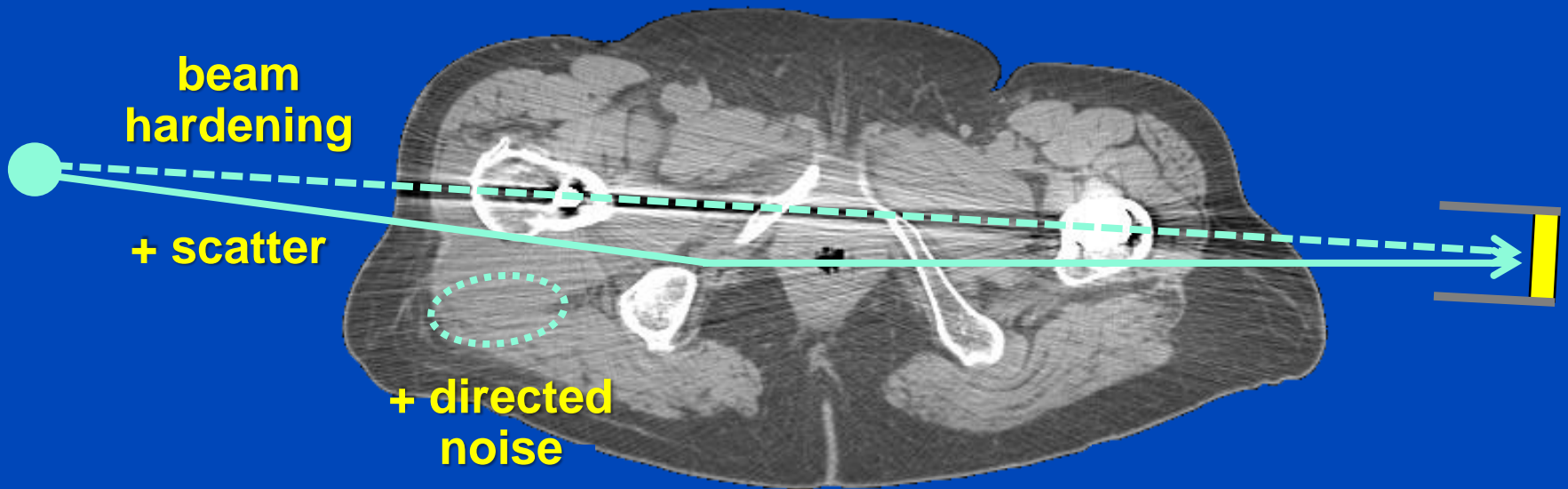
- Deep CNN-driven patch-based combination of the advantages of several MAR methods trained on simulated artifacts



- followed by segmentation into tissue classes
- followed by forward projection of the CNN prior and replacement of metal areas of the original sinogram
- followed by reconstruction



# Metal artifacts are



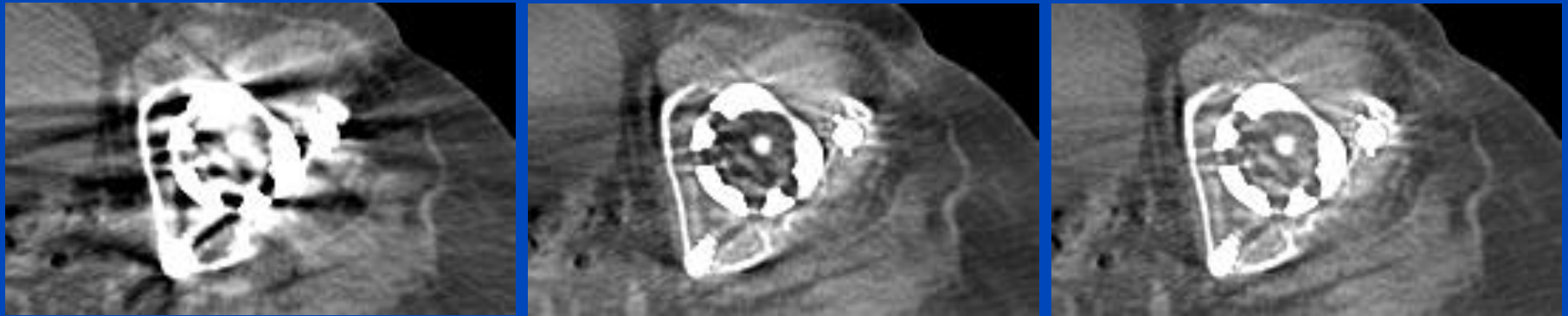
+ increased susceptibility to sampling artifacts and motion.

# MAR without Machine Learning is a Good Alternative: Frequency Split Normalized MAR<sup>1,2</sup>

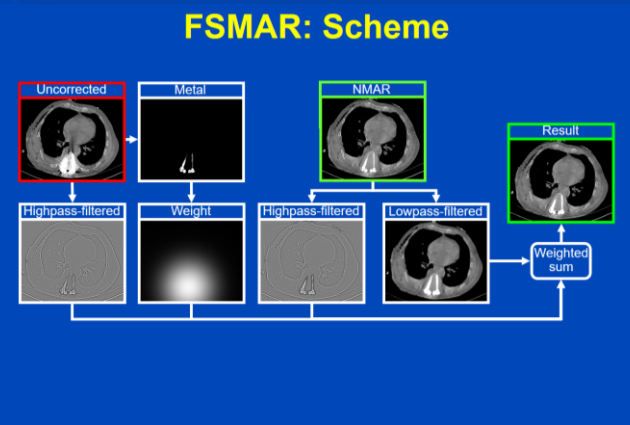
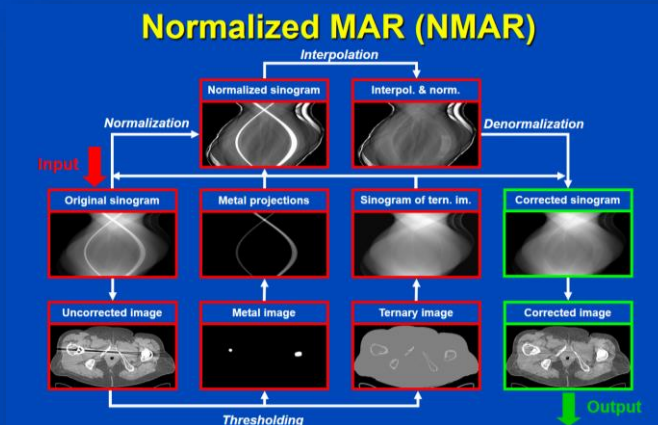
Uncorrected

FSLIMAR

FSNMAR



Patient with bilateral hip prosthesis, Somatom Definition Flash, (C=40/W=500).



<sup>1</sup>E. Meyer, M. Kachelrieß. Normalized metal artifact reduction (NMAR) in computed tomography. Med. Phys. 37(10):5482-5493, Oct. 2010.

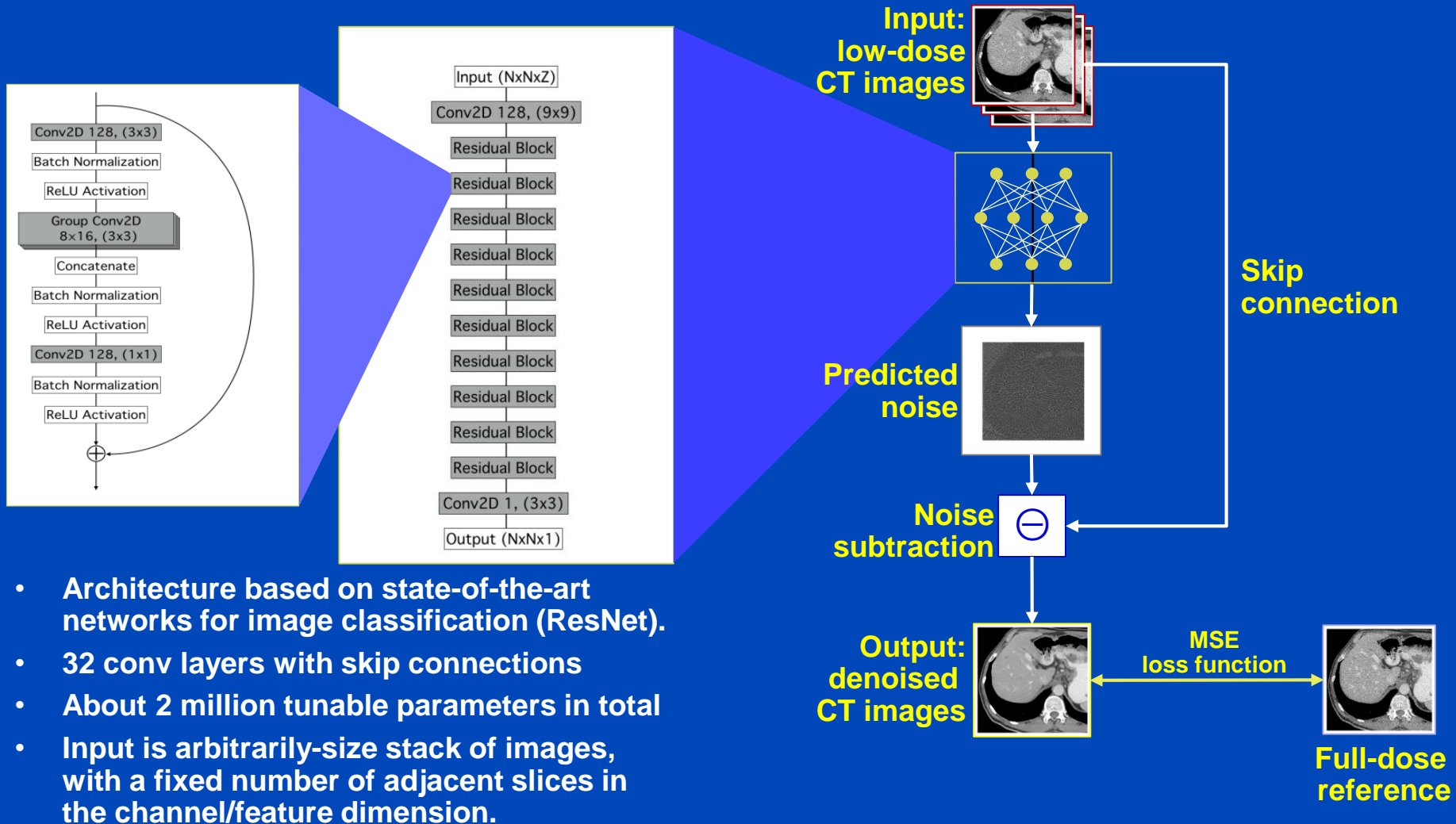
<sup>2</sup>E. Meyer, M. Kachelrieß. Frequency split metal artifact reduction (FSMAR) in CT. Med. Phys. 39(4):1904-1916, April 2012.



# Summary on Deep MAR

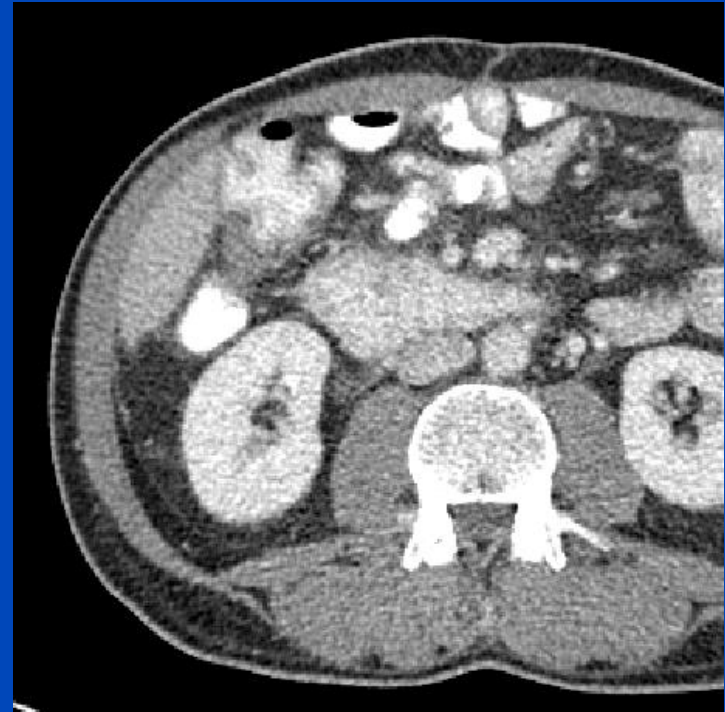
- **Most common uses for networks:**
  - Improve image quality in image domain after MAR
  - Use network for the sinogram inpainting
  - Produce a prior image, e.g. for NMAR
- **Additional observations:**
  - Training data are often produced by segmenting an artifact-free CT image, adding metal and applying a polychromatic forward projection to different types of tissue separately.
  - As of today, it seems hard to outperform NMAR, or hard to give convincing clinical examples.

# Noise Removal Example



- Architecture based on state-of-the-art networks for image classification (ResNet).
- 32 conv layers with skip connections
- About 2 million tunable parameters in total
- Input is arbitrarily-size stack of images, with a fixed number of adjacent slices in the channel/feature dimension.

# Noise Removal Example



Low dose images (1/4 of full dose)

# Noise Removal Example



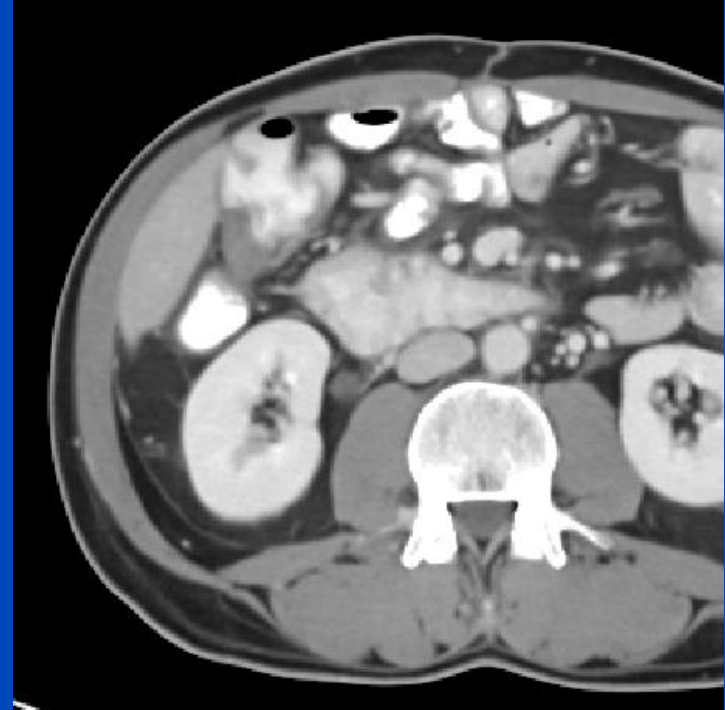
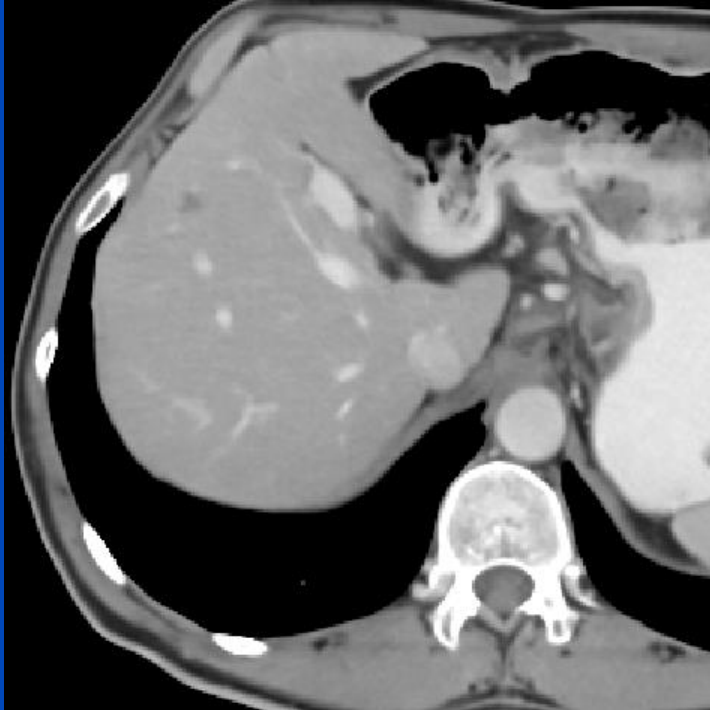
Denoised low dose

# Noise Removal Example



Full dose

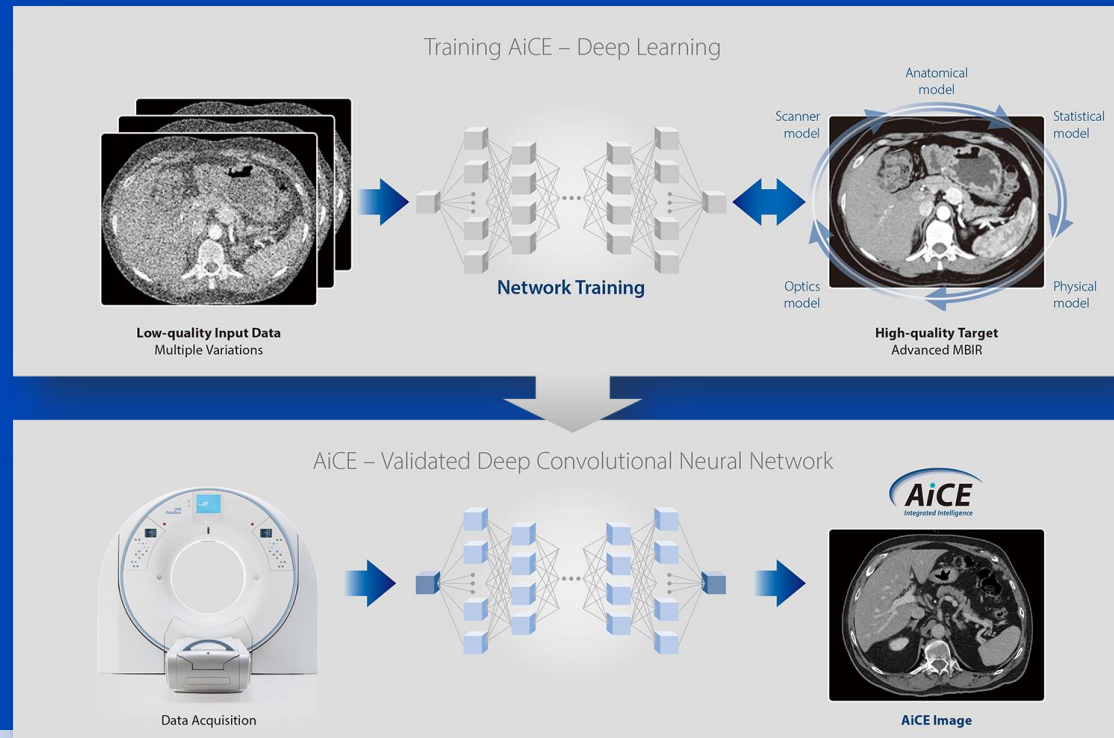
# Noise Removal Example



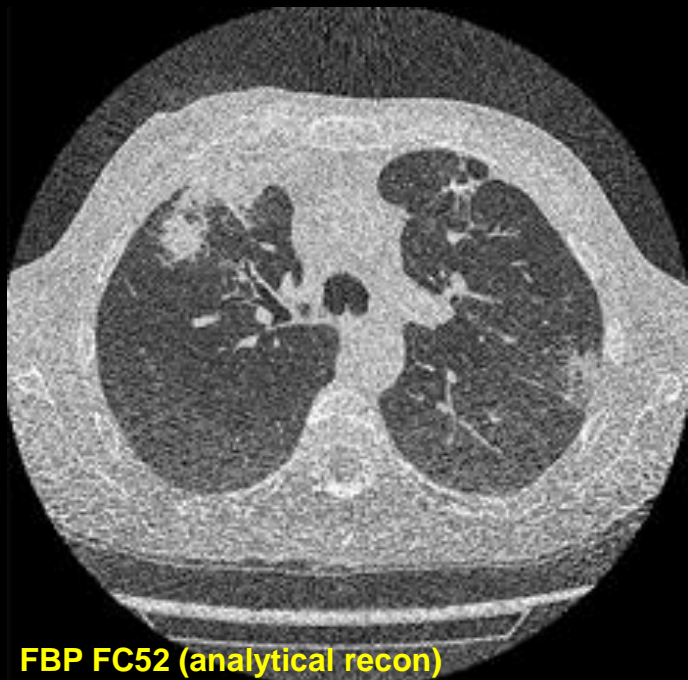
Denoised full dose

# Canon's AiCE

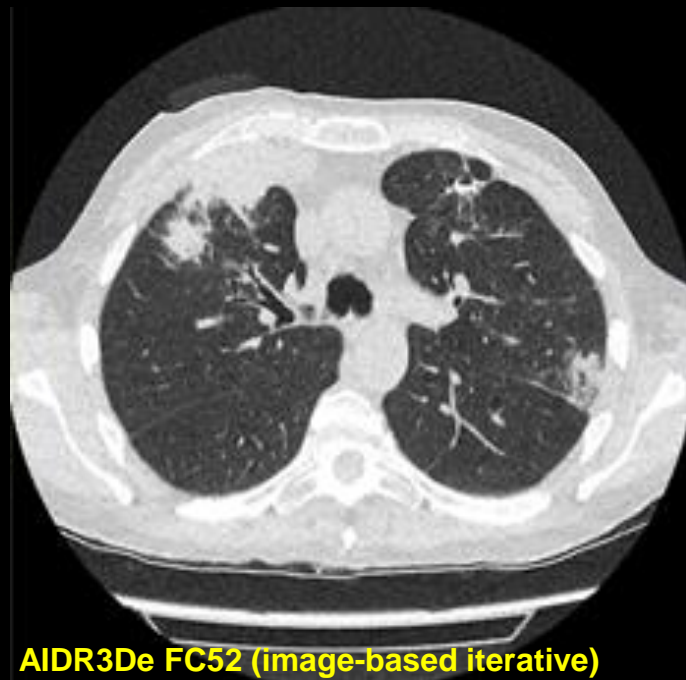
- Advanced intelligent Clear-IQ Engine (AiCE)
- Trained to restore low-dose CT data to match the properties of FIRST, the model-based IR of Canon.
- FIRST is applied to high-dose CT images to obtain a high fidelity training target



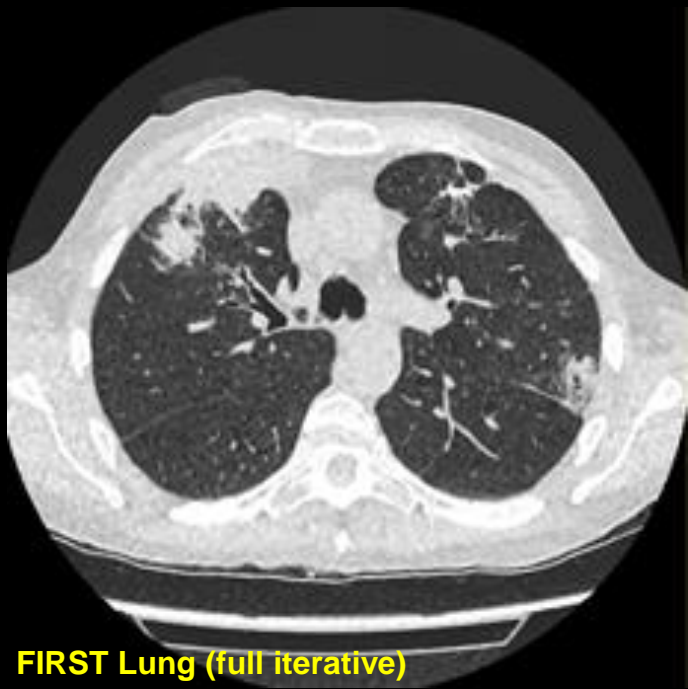
U = 100 kV  
CTDI = 0.6 mGy  
DLP = 24.7 mGy·cm  
D<sub>eff</sub> = 0.35 mSv



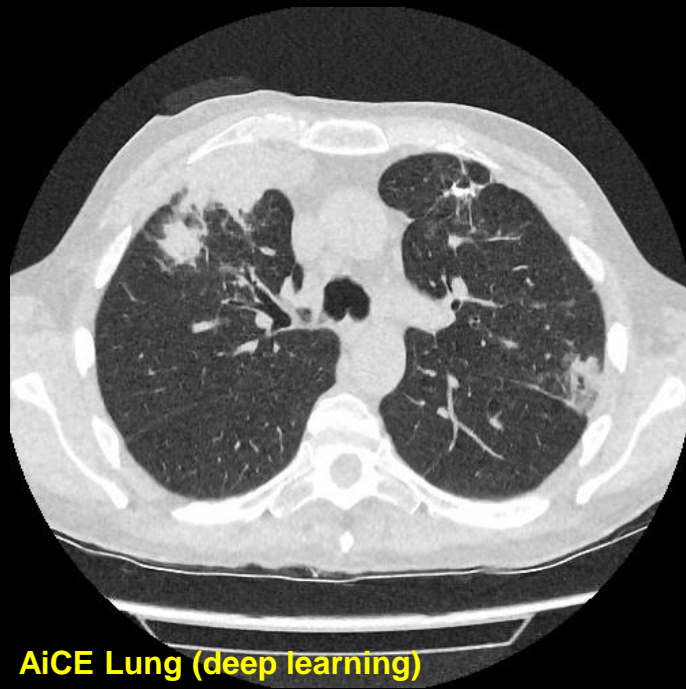
**FBP FC52 (analytical recon)**



**AIDR3De FC52 (image-based iterative)**



**FIRST Lung (full iterative)**



**AiCE Lung (deep learning)**



# GE's True Fidelity

- Based on a deep CNN
- Trained to restore low-dose CT data to match the properties of Veo, the model-based IR of GE.
- No information can be obtained in how the training is conducted for the product implementation.

## 2.5D DEEP LEARNING FOR CT IMAGE RECONSTRUCTION USING A MULTI-GPU IMPLEMENTATION

*Amirkoushyar Ziabari\**, *Dong Hye Ye* <sup>\*</sup> <sup>†</sup>, *Somesh Srivastava* <sup>‡</sup>, *Ken D. Sauer* <sup>⊕</sup>  
*Jean-Baptiste Thibault* <sup>‡</sup>, *Charles A. Bouman* <sup>\*</sup>

<sup>\*</sup> Electrical and Computer Engineering at Purdue University

<sup>†</sup> Electrical and Computer Engineering at Marquett University

<sup>‡</sup> GE Healthcare

<sup>⊕</sup> Electrical Engineering at University of Notre Dame

### ABSTRACT

While Model Based Iterative Reconstruction (MBIR) of CT scans has been shown to have better image quality than Filtered Back Projection (FBP), its use has been limited by its high computational cost. More recently, deep convolutional neural networks (CNN) have shown great promise in both denoising and reconstruction applications. In this research, we propose a fast reconstruction algorithm, which we call Deep Learning MBIR (DL-MBIR).

streaking artifacts caused by sparse projection views in CT images [8]. More recently, Ye, et al. [9] developed method for incorporating CNN denoisers into MBIR reconstruction as advanced prior models using the Plug-and-Play framework [10, 11].

In this paper, we propose a fast reconstruction algorithm, which we call Deep Learning MBIR (DL-MBIR), for approximately achieving the improved quality of MBIR using a deep residual neural network. The DL-MBIR method is trained to

ss.IV] 20 Dec 2018



**FBP**

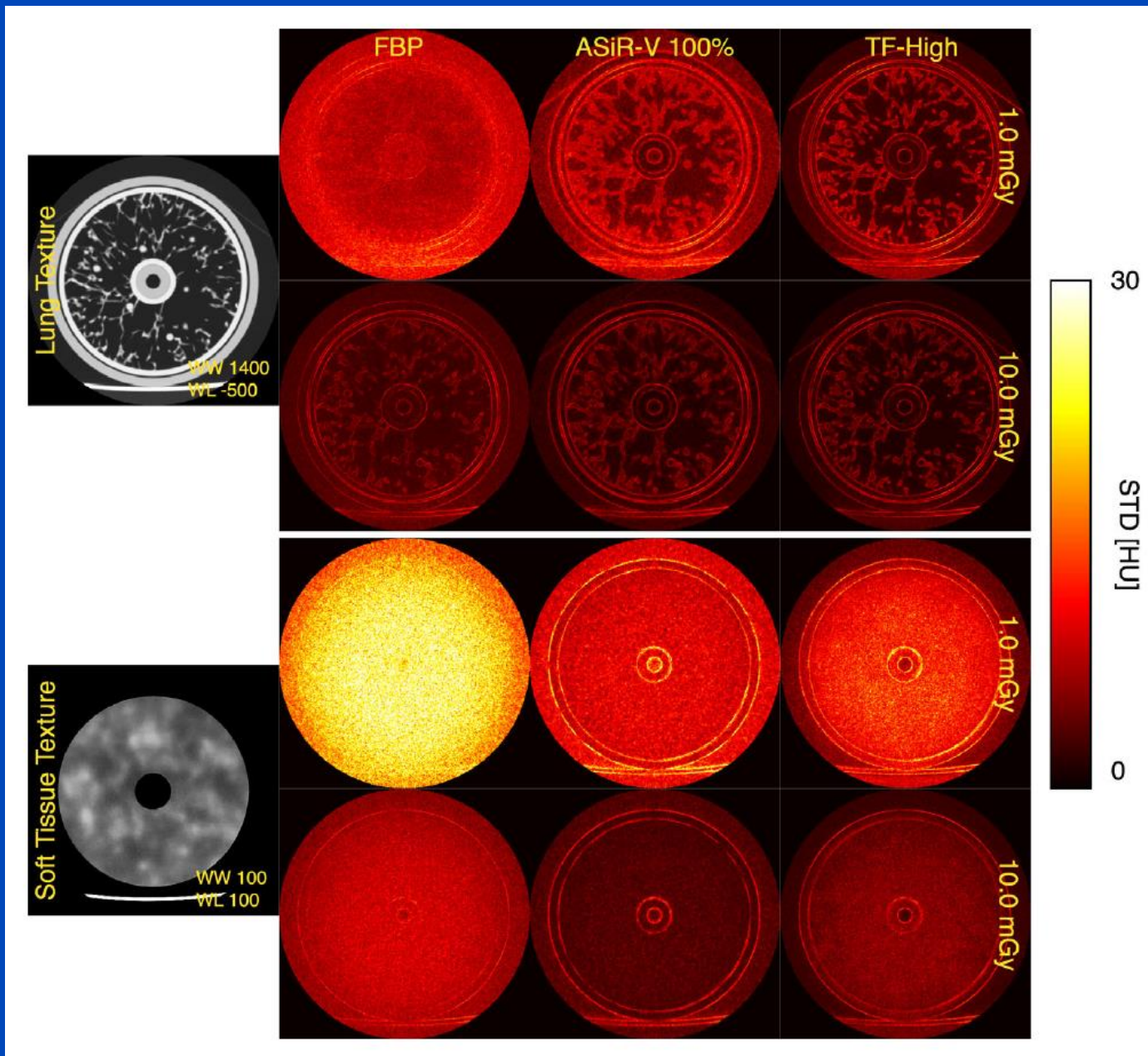


**ASIR V 50%**



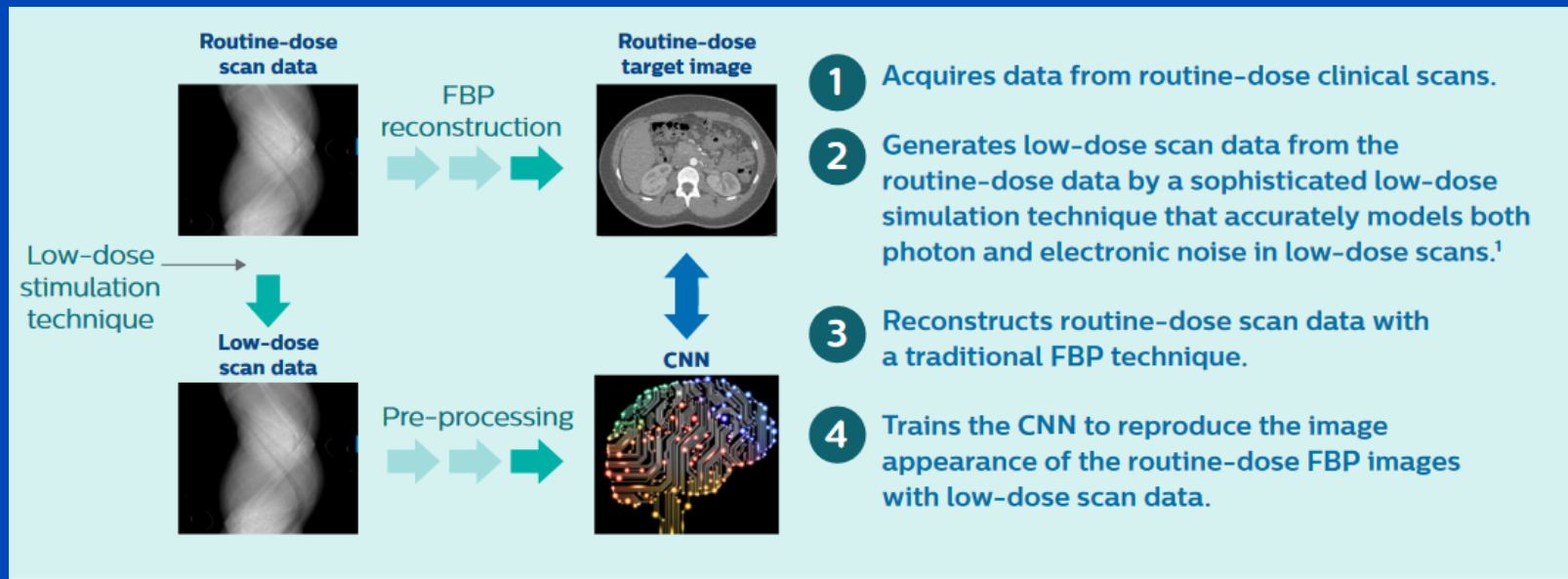
**True Fidelity**

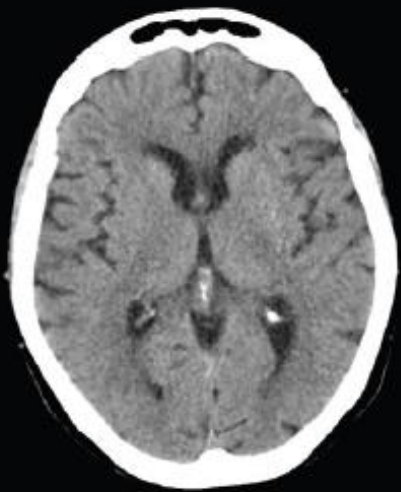
**Courtesy of GE Healthcare**



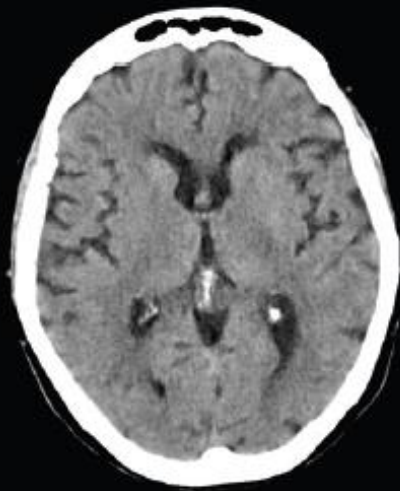
# Philips' Precise Image

- Noise-injected data serve as low dose examples while their original reconstructions are the labels. A CNN learns how to denoise the low dose images.





**iDose<sup>4</sup> 1.4 mSv**



**Precise Image 0.7 mSv**



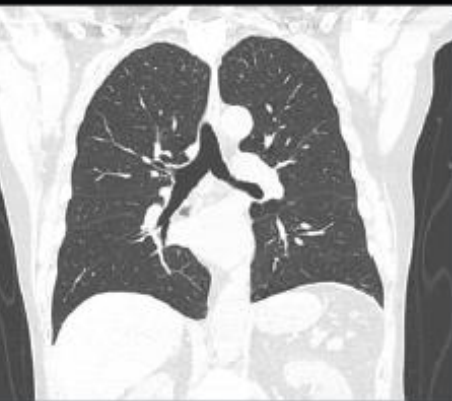
**iDose<sup>4</sup> 5.1 mSv**



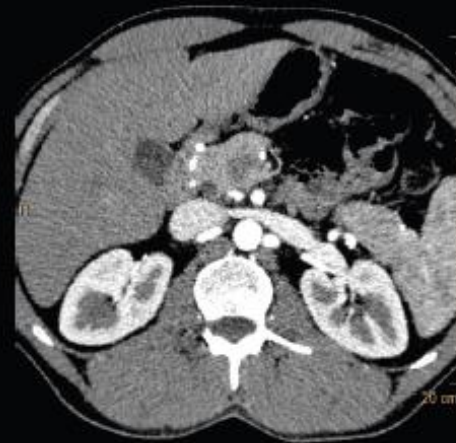
**Precise Image 2.6 mSv**



**iDose<sup>4</sup> 1.5 mSv**



**Precise Image 0.75 mSv**



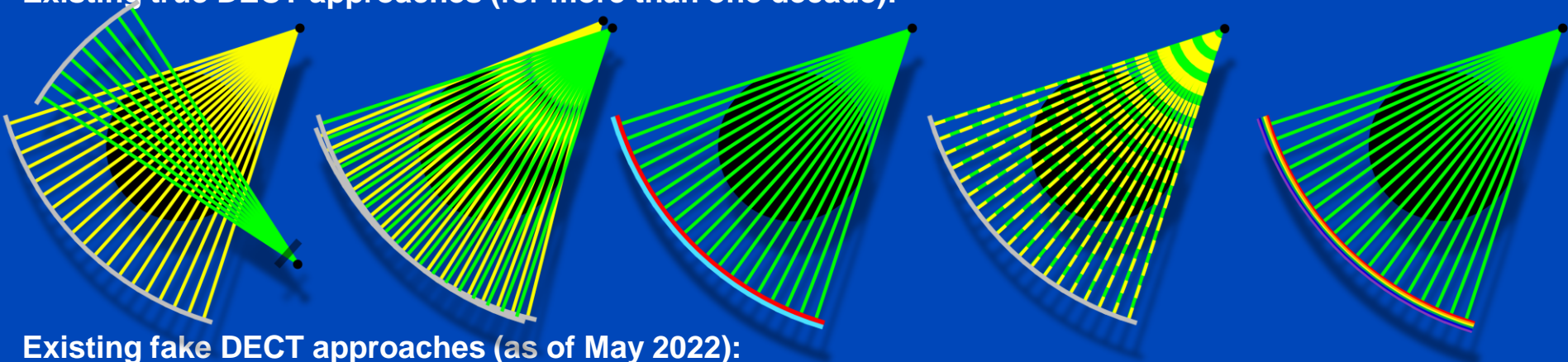
**iDose<sup>4</sup> 5.4 mSv**



**Precise Image 2.6 mSv**

# True and Fake DECT

Existing true DECT approaches (for more than one decade):



Existing fake DECT approaches (as of May 2022):

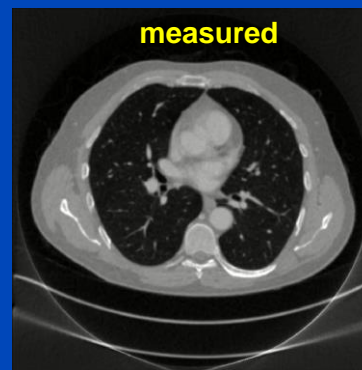
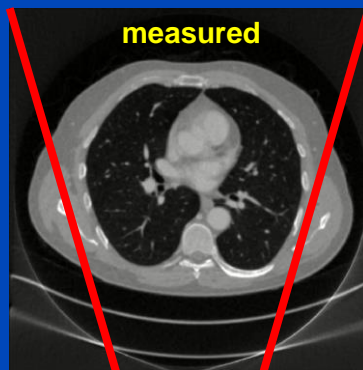
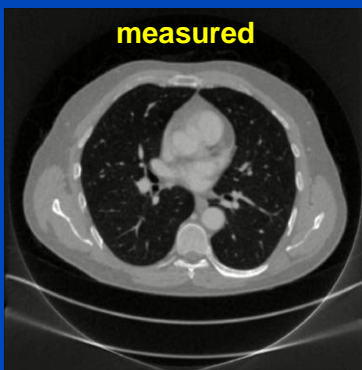
- [1] J. Ma, Y. Liao, Y. Wang, S. Li, J. He, D. Zeng, Z. Bian, “**Pseudo dual energy CT** imaging using deep learning-based framework: basic material estimation“, *SPIE Medical Imaging 2018*.
- [2] W. Zhao, T. Lv, P. Gao, L. Shen, X. Dai, K. Cheng, M. Jia, Y. Chen, L. Xing, “A deep learning approach for dual-energy CT imaging **using a single-energy CT** data“, *Fully3D 2019*.
- [3] D. Lee, H. Kim, B. Choi, H. J. Kim, “Development of a deep neural network for generating synthetic dual-energy chest x-ray images **with single x-ray exposure**“, *PMB 64(11)*, 2019.
- [4] L. Yao, S. Li, D. Li, M. Zhu, Q. Gao, S. Zhang, Z. Bian, J. Huang, D. Zeng, J. Ma, “Leveraging deep generative model for direct energy-resolving CT imaging **via existing energy-integrating CT** images“, *SPIE Medical Imaging 2020*.
- [5] D. P. Clark, F. R. Schwartz, D. Marin, J. C. Ramirez-Giraldo, C. T. Badea, “Deep learning based **spectral extrapolation** for dual-source, dual-energy x-ray CT“, *Med. Phys.* 47 (9): 4150–4163, 2020.
- [6] C. K. Liu, C. C. Liu, C. H. Yang, H. M. Huang, “Generation of brain dual-energy CT **from single-energy CT** using deep learning“, *Journal of Digital Imaging* 34(1):149–161, 2021.
- [7] T. Lyu, W. Zhao, Y. Zhu, Z. Wu, Y. Zhang, Y. Chen, L. Luo, S. Li, L. Xing, “Estimating dual-energy CT imaging **from single-energy CT** data with material decomposition convolutional neural network“, *Medical Image Analysis* 70:1–10, 2021.
- [8] F. R. Schwartz, D. P. Clark, Y. Ding, J. C. Ramirez-Giraldo, C. T. Badea, D. Marin, “Evaluating renal lesions using **deep-learning based extension** of dual-energy FoV in dual-source CT—A retrospective pilot study“, *European Journal of Radiology* 139:109734, 2021.
- [9] Y. Li, X. Tie, K. Li, J. W. Garrett, G.-H. Chen, “Deep-En-Chroma: **mining the spectral fingerprints in single-kV CT** acquisitions using energy integration detectors“, *SPIE Medical Imaging 2022*.

**Real DECT  
(ground truth)**

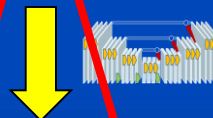
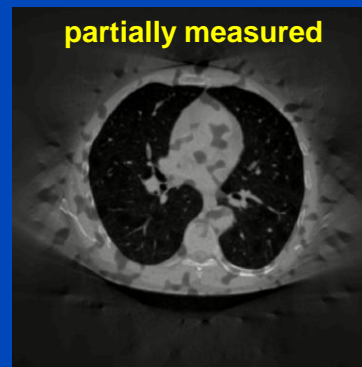
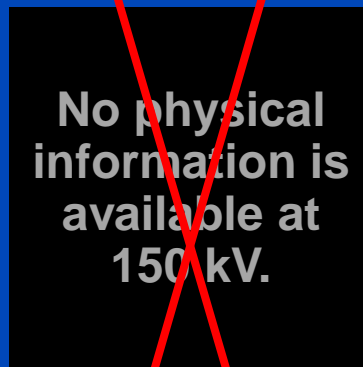
**Fake DECT  
(often proposed)**

**Partial DECT  
(small B FOM)**

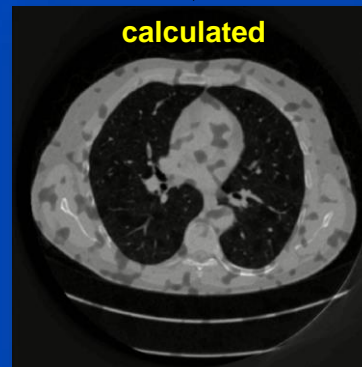
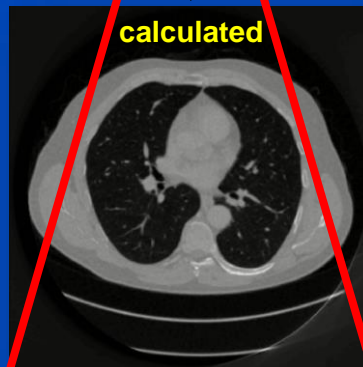
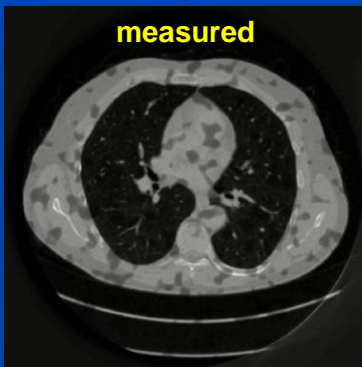
70 kV



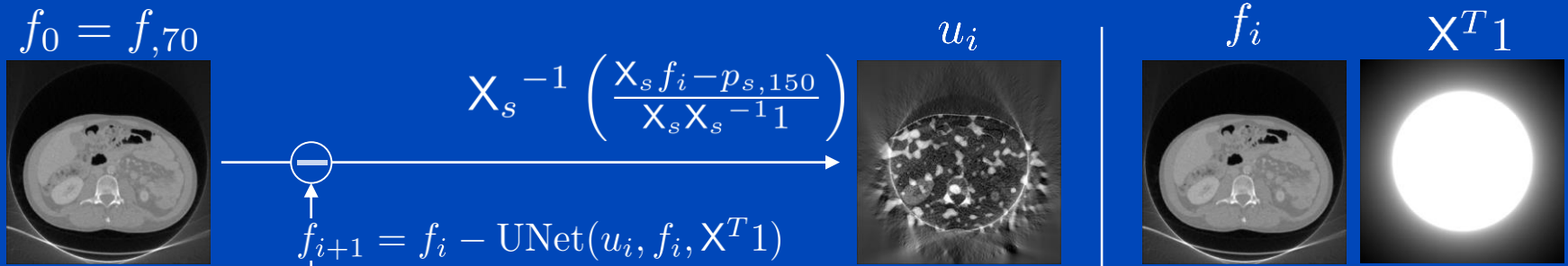
150 kV Sn



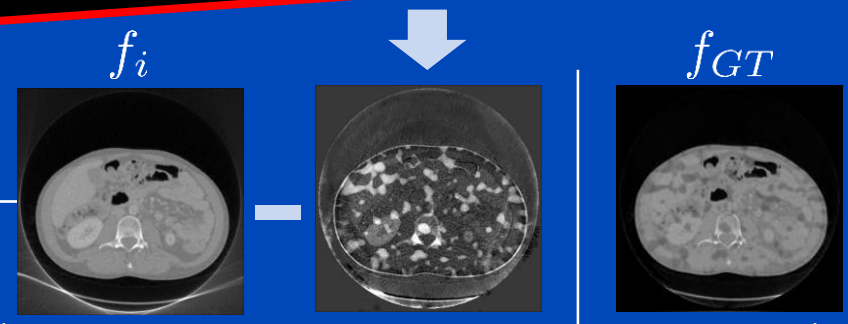
final 150 kV Sn



# Algorithm for Partial DECT



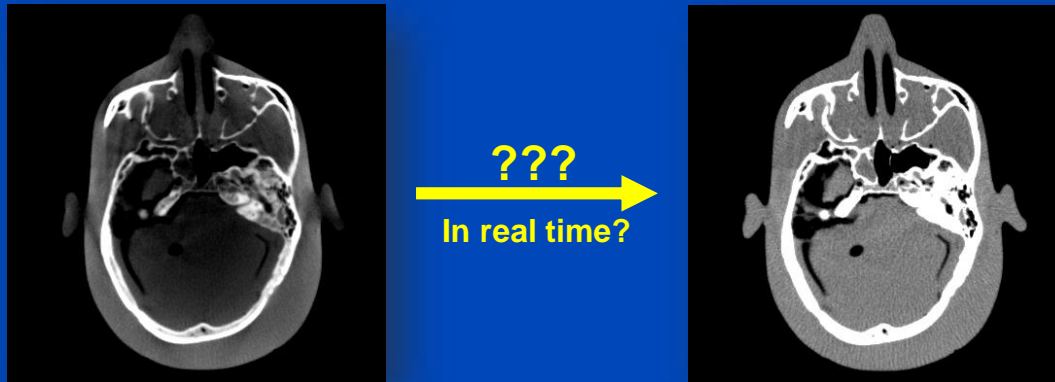
**Measuring the physical properties of the patient at more than one energy cannot be avoided!**



$$L = \|w \cdot (f_i - \text{UNet}_i(u_i, f_i, X^T 1) - f_{GT})\|^2$$

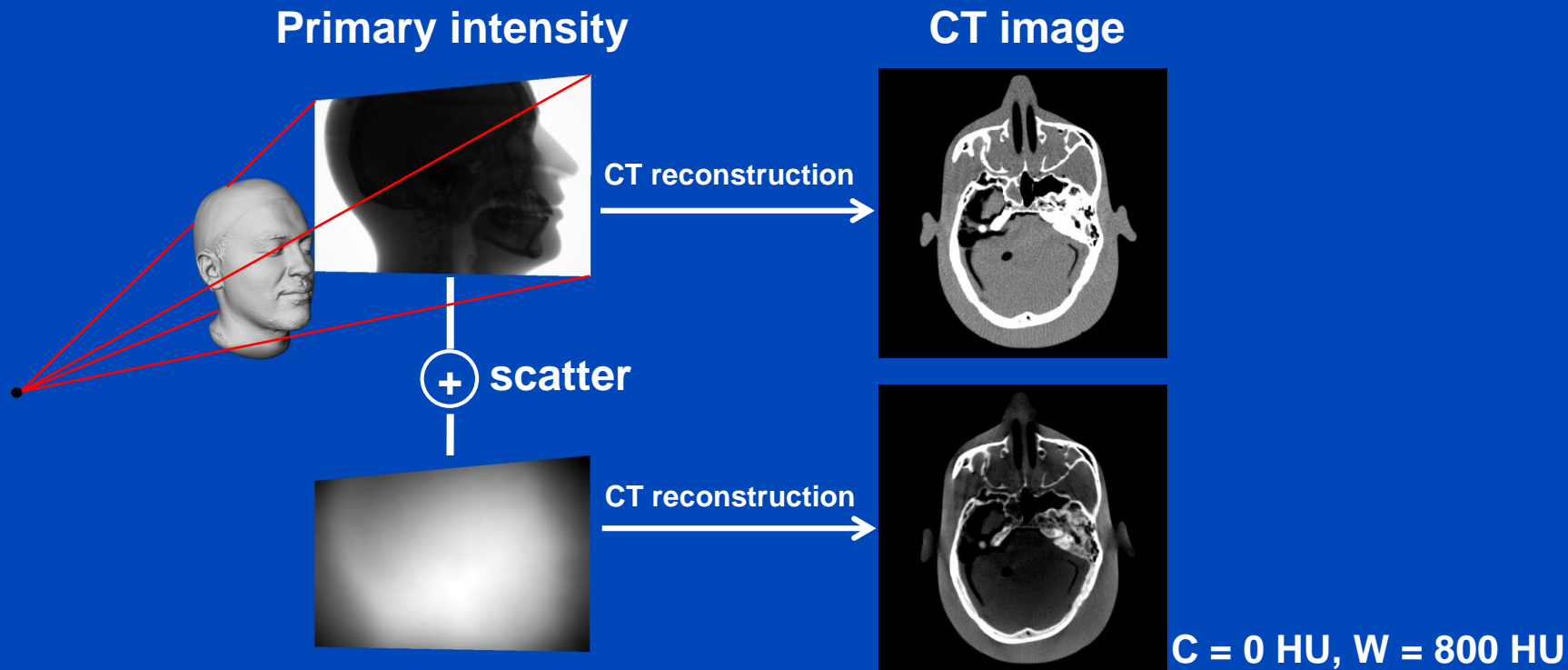


# Deep Scatter Estimation



# Motivation

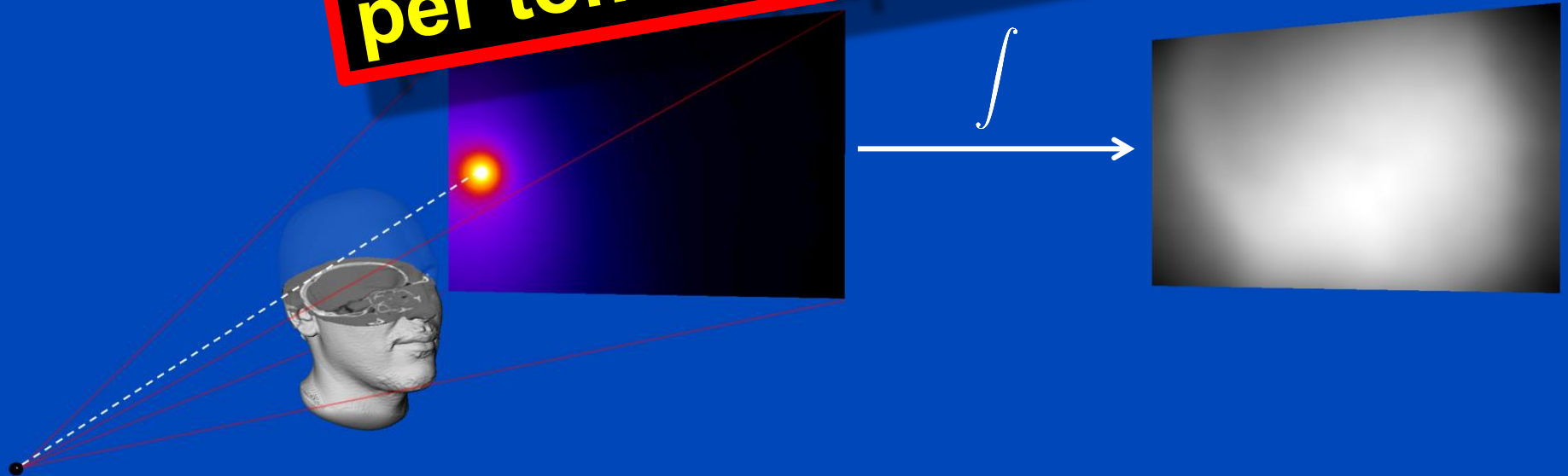
- X-ray scatter is a major cause of image quality degradation in CT and CBCT.
- Appropriate scatter correction is crucial to maintain the diagnostic value of the CT examination.



# Monte Carlo Scatter Estimation

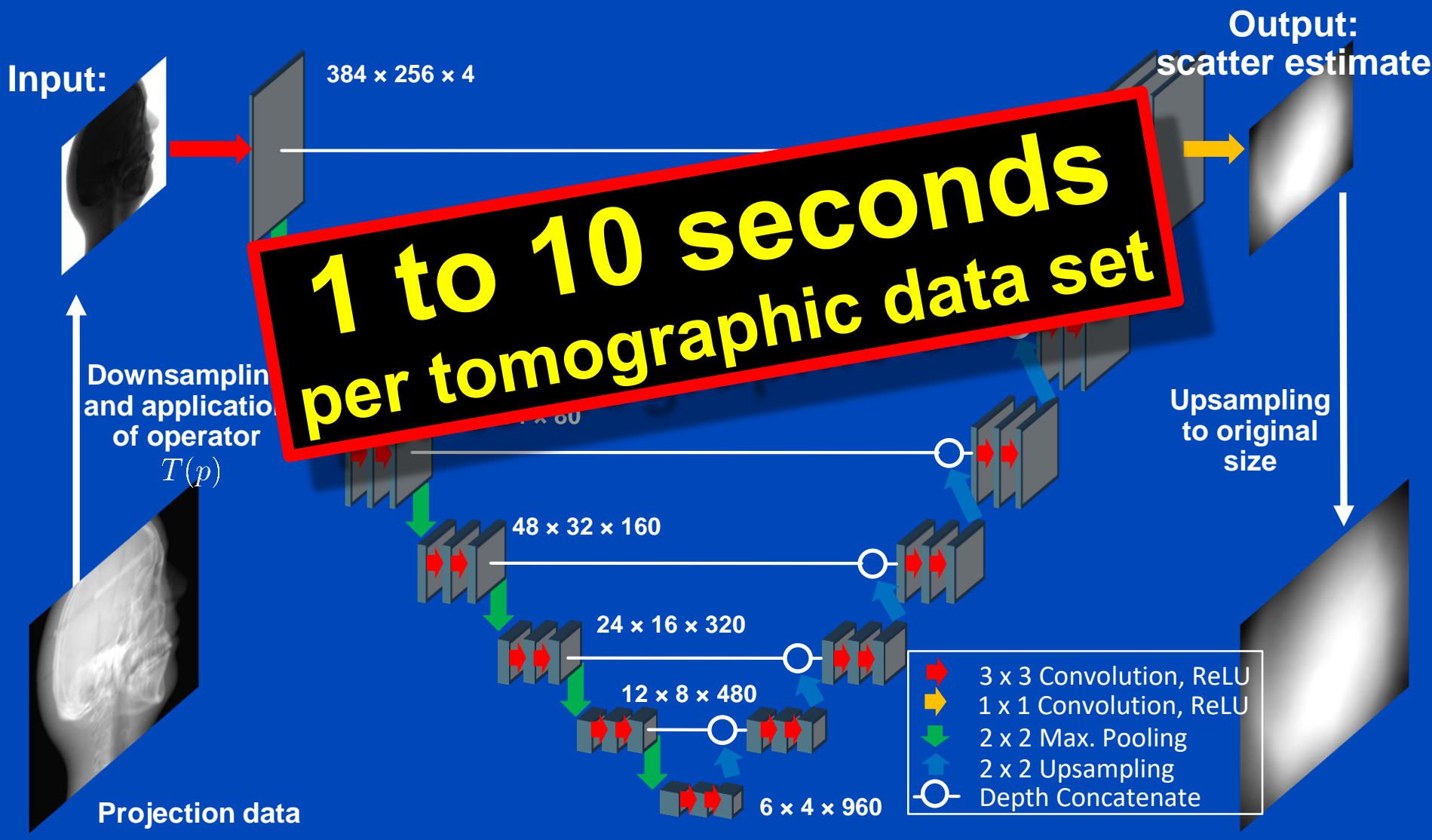
- Simulation of photon trajectories according to physical interaction probabilities.
- Simulating a large number of trajectories well approximates the complete scatter distribution

**1 to 10 hours  
per tomographic data set**



# Deep Scatter Estimation

## Network architecture & scatter estimation framework



# Reconstructions of Measured Data

Slit Scan

No Correction

Kernel-Based  
Scatter Estimation

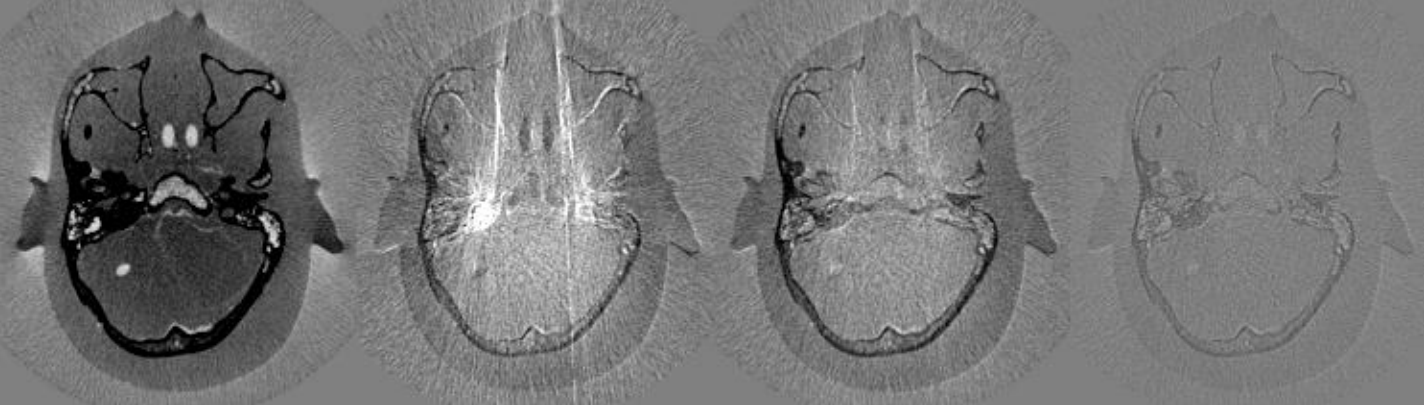
Hybrid Scatter  
Estimation

Deep Scatter  
Estimation

CT Reconstruction



Difference to slit scan



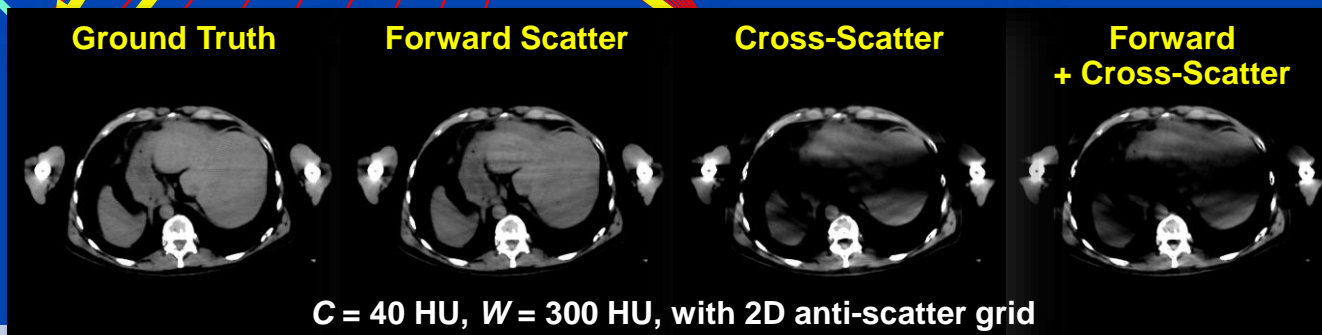
$C = 0 \text{ HU}, W = 1000 \text{ HU}$

# Scatter in Dual Source CT (DSCT)



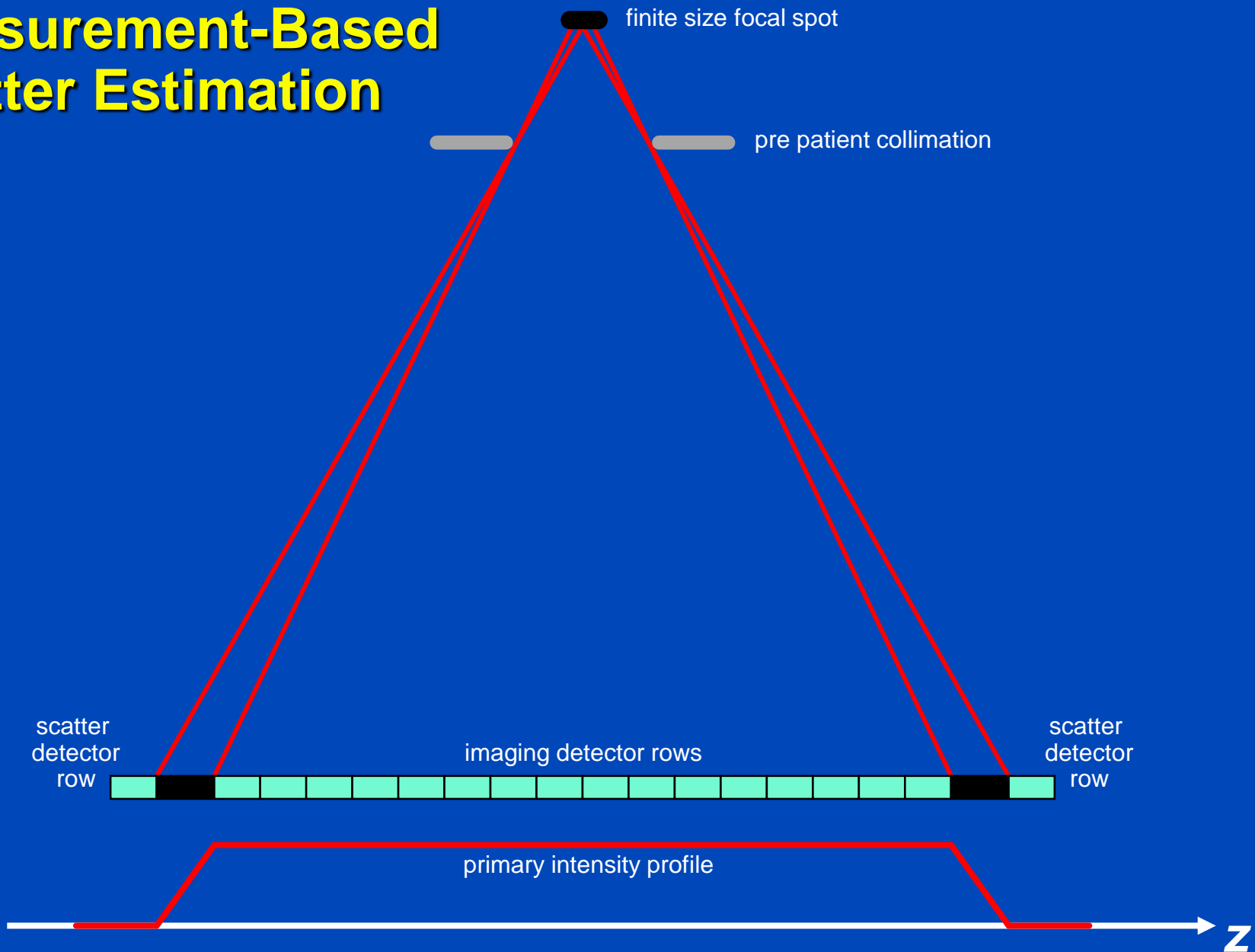
Siemens SOMATOM Force  
dual source cone-beam spiral CT

$$q = -\ln \frac{I_{\text{primary}} + S_{\text{forward}} + \rho S_{\text{cross}}}{I_0}$$



C = 40 HU, W = 300 HU, with 2D anti-scatter grid

# Measurement-Based Scatter Estimation



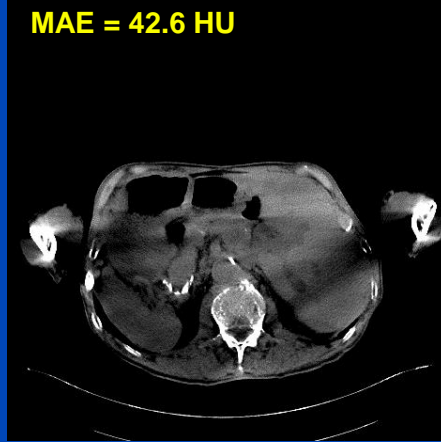
# Cross-DSE

Ground Truth



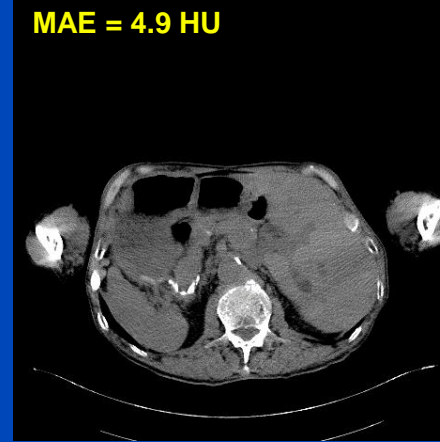
Uncorrected

MAE = 42.6 HU



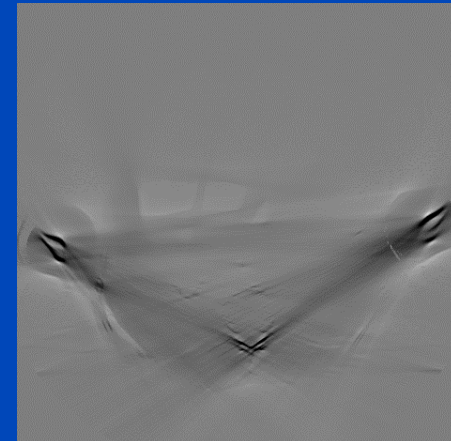
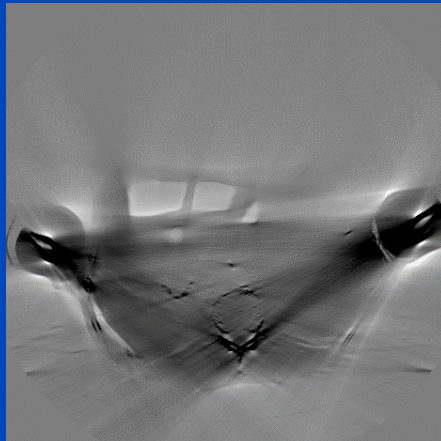
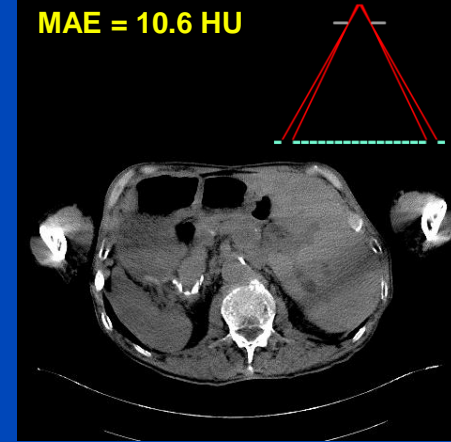
xDSE (2D, xSSE)

MAE = 4.9 HU



Measurement-based

MAE = 10.6 HU



**xDSE (2D, xSSE) maps**

**primary + forward scatter + cross-scatter + cross-scatter approximation → cross-scatter**

Images  $C = 40$  HU,  $W = 300$  HU, difference images  $C = 0$  HU,  $W = 300$  HU



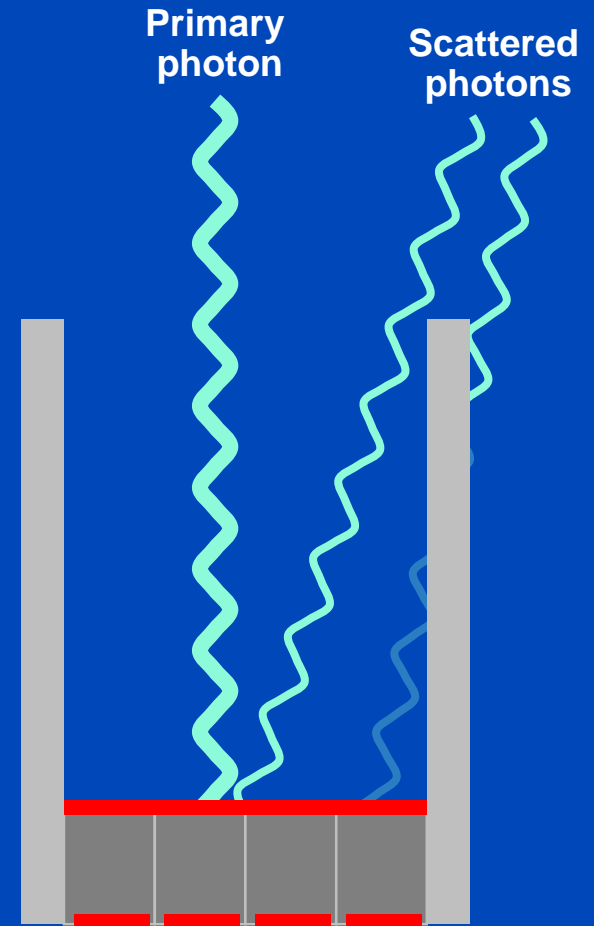
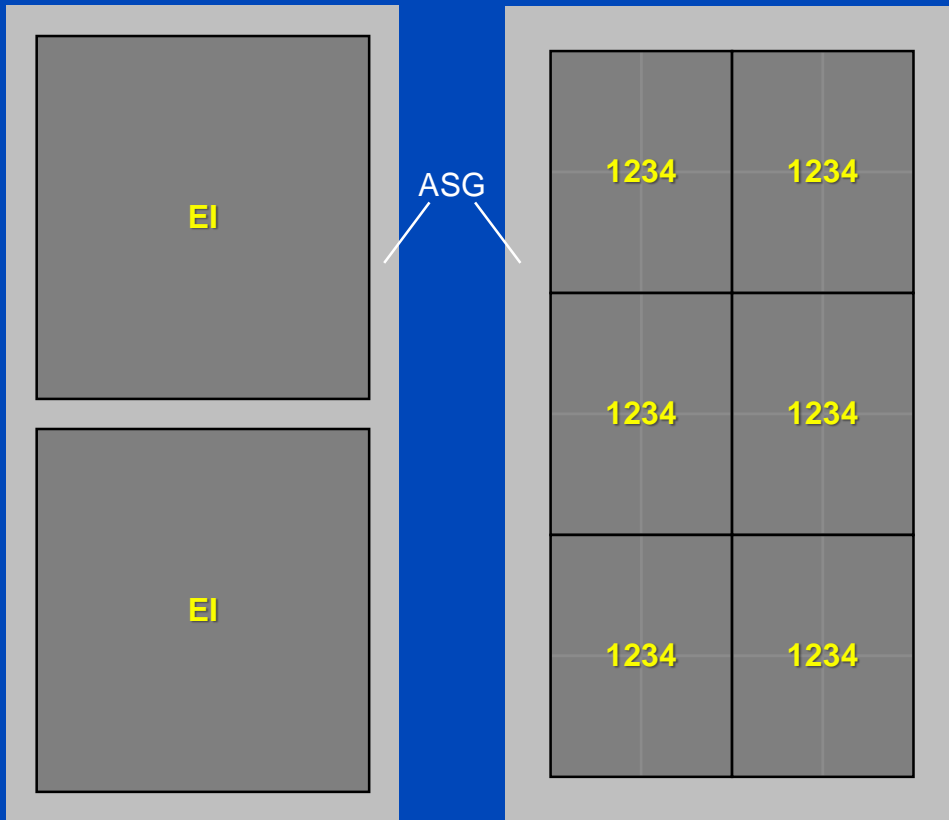
# Conclusions on DSE

- DSE needs about 3 ms per CT and 10 ms per CBCT projection (as of 2020).
- DSE is a fast and accurate alternative to MC simulations.
- DSE outperforms kernel-based approaches in terms of accuracy and speed.
- Facts:
  - DSE can estimate scatter from a single (!) x-ray image.
  - DSE can accurately estimate scatter from a primary+scatter image.
  - DSE generalizes to all anatomical regions.
  - DSE works for geometries and beam qualities differing from training.
  - DSE may outperform MC even though DSE is trained with MC.
- DSE is not restricted to reproducing MC scatter estimates.
- DSE can rather be trained with any other scatter estimate, including those based on measurements.

# Scatter of Coarse ASG

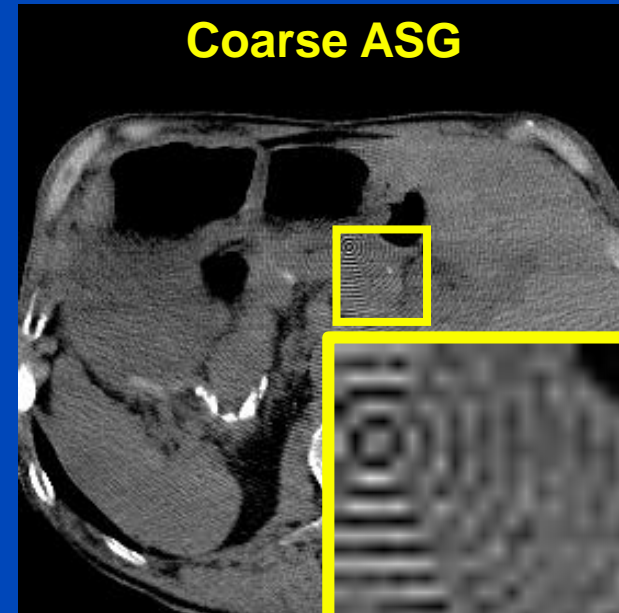
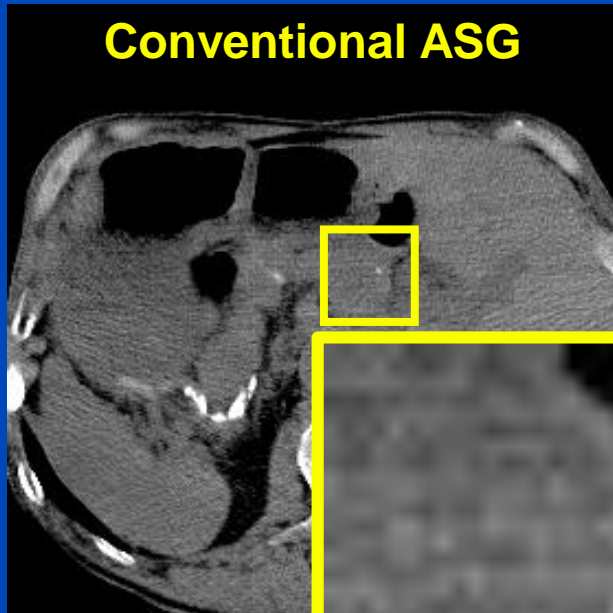
**Conventional ASG**  
Somatom Force  
920 × 96 detector pixels  
pixel size 0.52 × 0.56 mm at iso

**Coarse ASG**  
Naeotom Alpha  
1376 × 144 macro pixels  
pixel size 0.3 × 0.352 mm at iso



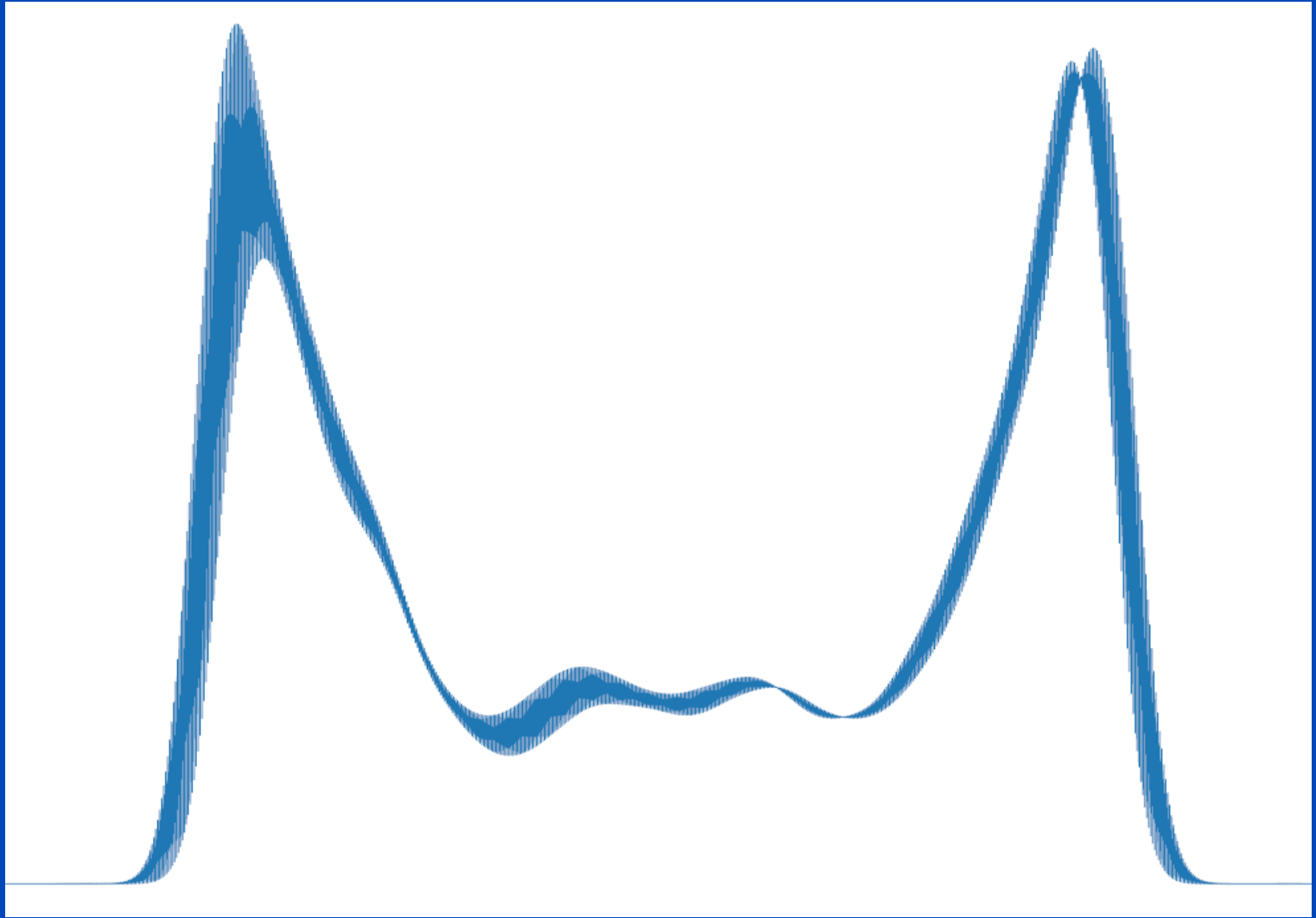
**Coarse ASGs lead to changing scatter intensity between neighboring pixels.**

# Scatter Artifacts of Coarse ASG



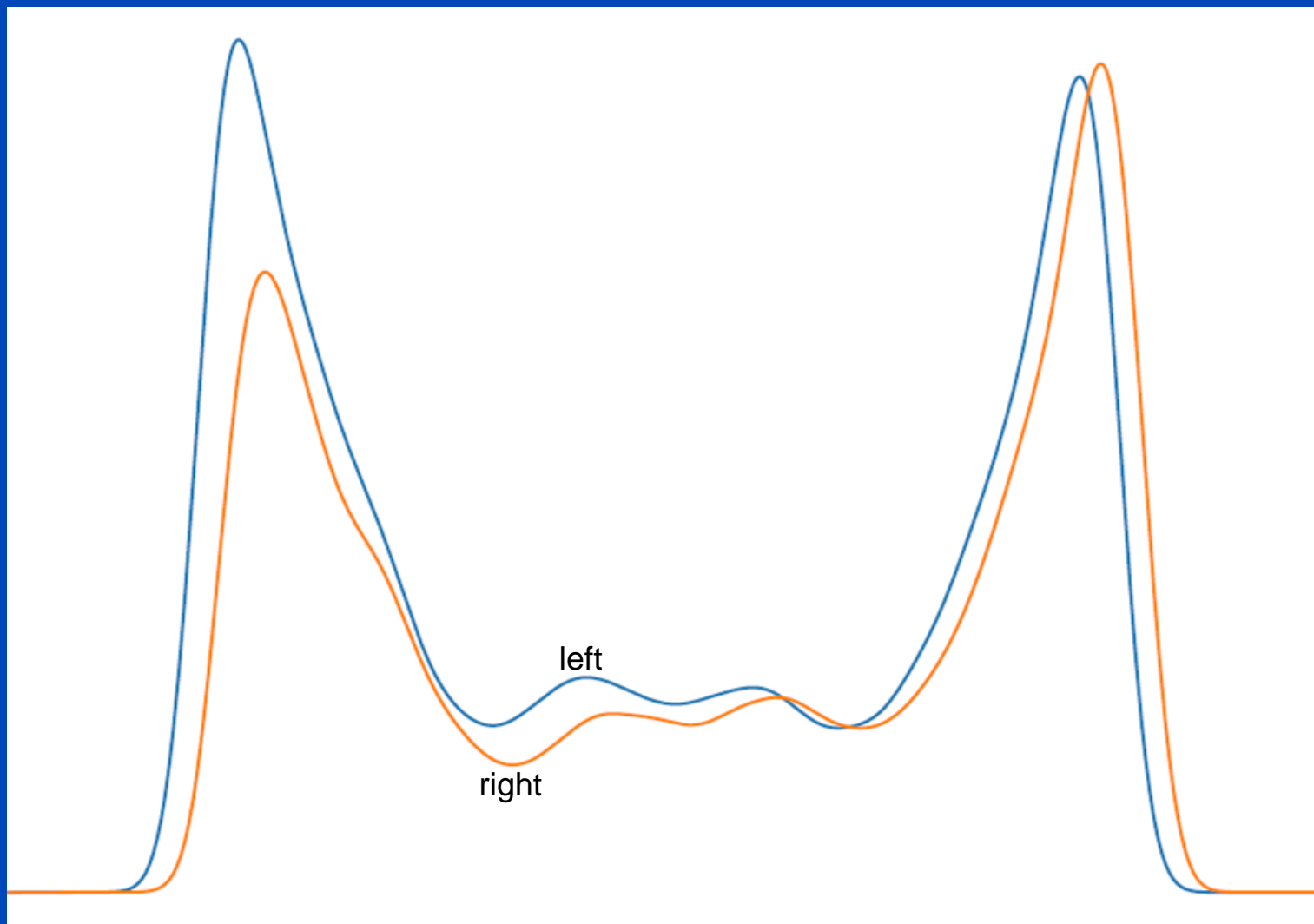
Coarse ASG can lead to scatter-induced moiré artifacts.

Reconstruction:  $C = 40$  HU,  $W = 300$  HU



→  $\beta$

Scatter distribution averaged over all detector rows

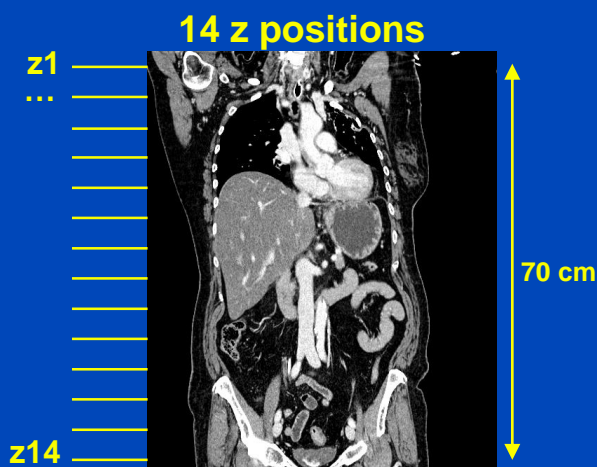


→  $\beta$

Scatter distribution averaged over all detector rows

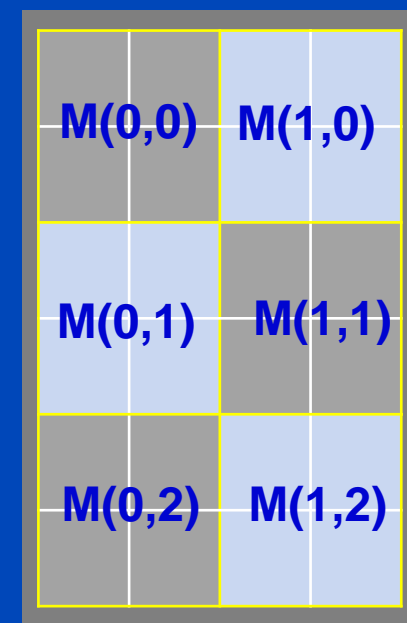
# Training and Validation Data

- **Monte Carlo simulation** with the geometry of the photon counting CT scanner NAEOTOM Alpha (Siemens Healthineers)
- 12 patients for training and 4 for validation
- 14 z-positions with 36 projections each simulated for each patient
- **8064 paired scatter and primary data pairs**
- Simulation of coarse ASG with macro pixel with detector dimension of **1376 × 144 pixels**
- 6 different macro pixels locations
- Smooth only across same macro-pixel locations



Training and validation patients with high variety and different clinical situations, important to consider **scatter-to-primary ratio**

Example of validation data set:



# DSE for coarse ASG

Detector dimension

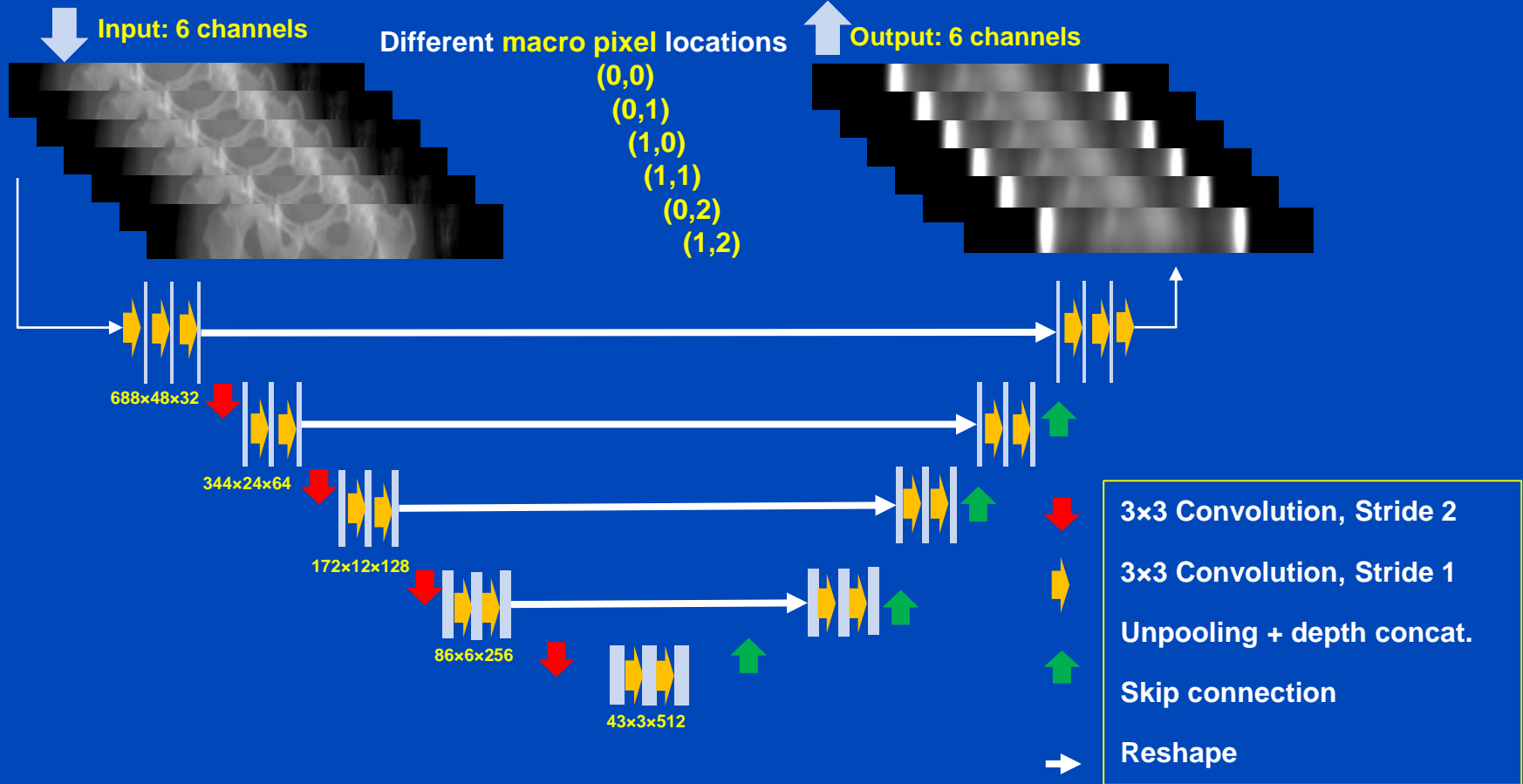
1376x144

Input mapping

$$p = -\ln\left(\frac{I_{\text{primary}}}{I_0} + \frac{I_{\text{scatter}}}{I_0}\right)$$

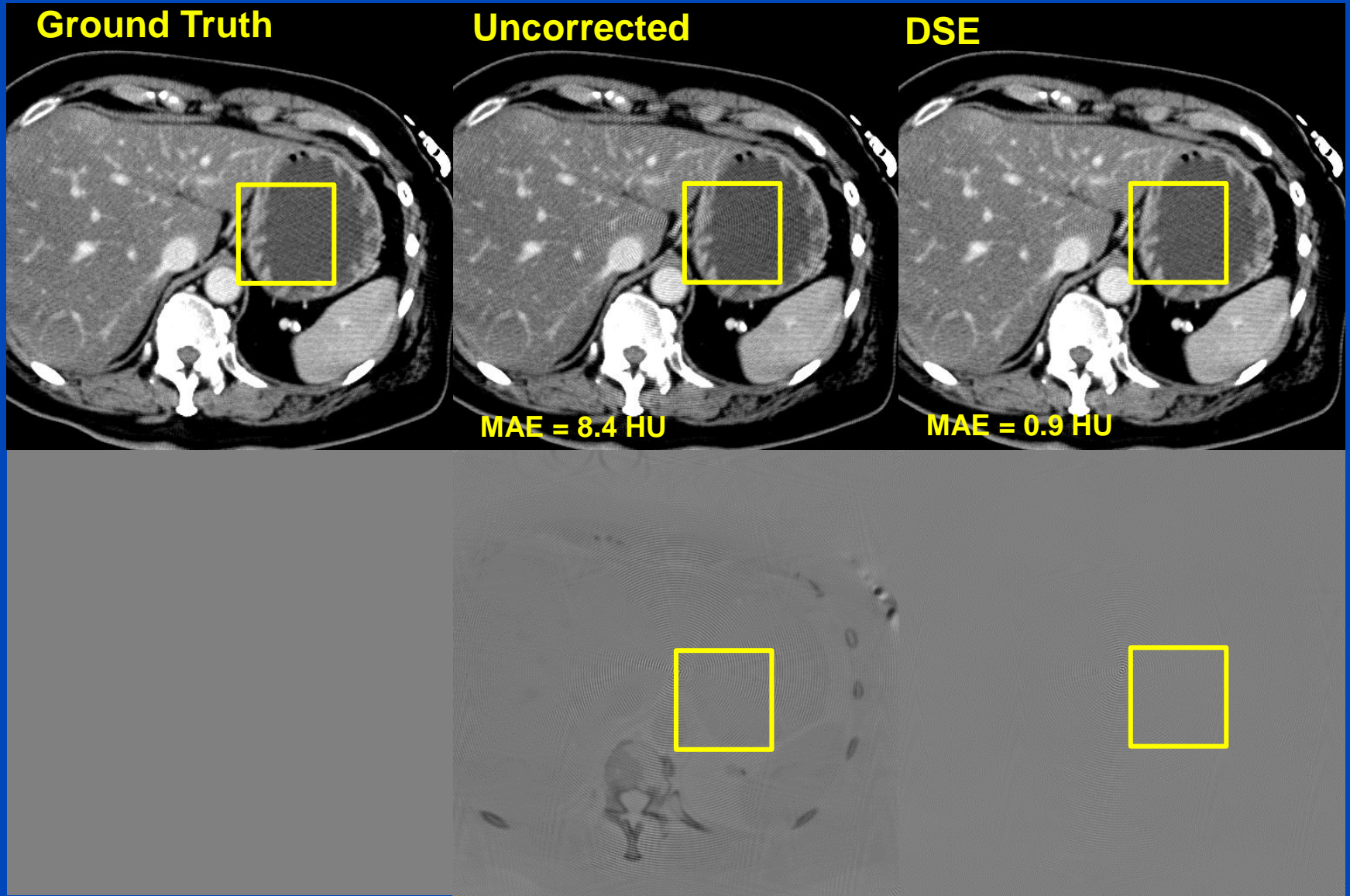
Each channel corresponds to a different pixel position between the lamella of the ASG

Merging 6 different channels to obtain total scatter correction term



This paper received the "Highest Impact Paper Award" for the highest impact score at the 7th International Conference on Image Formation in X-Ray Computed Tomography in June 2022

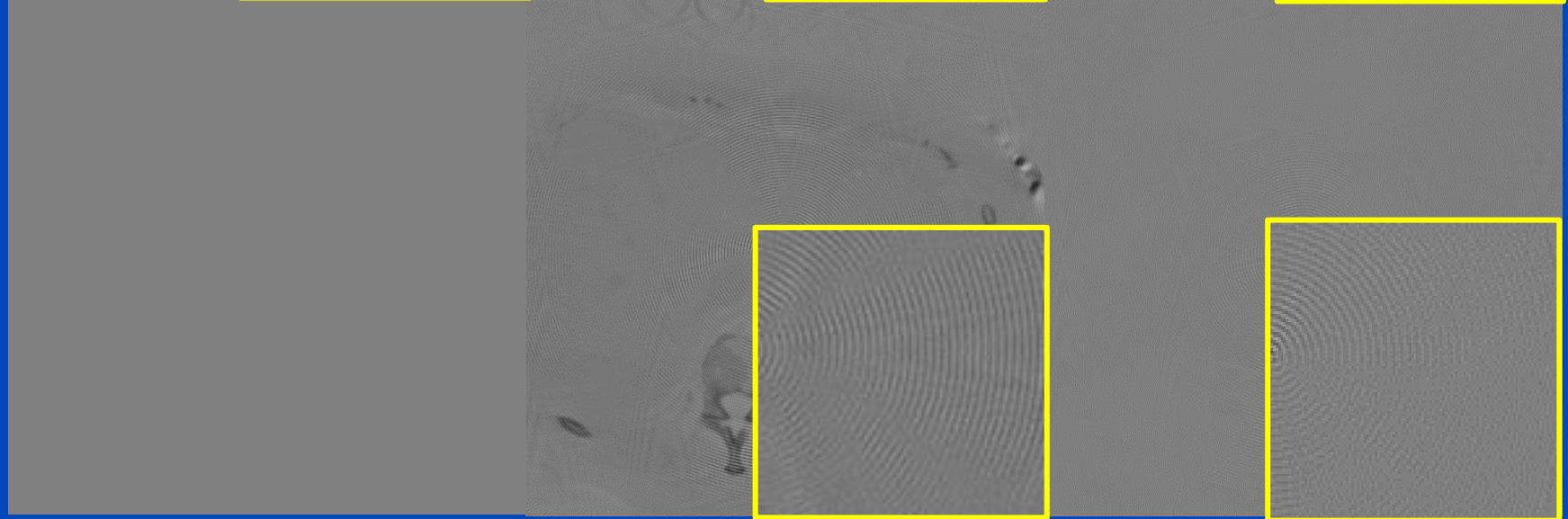
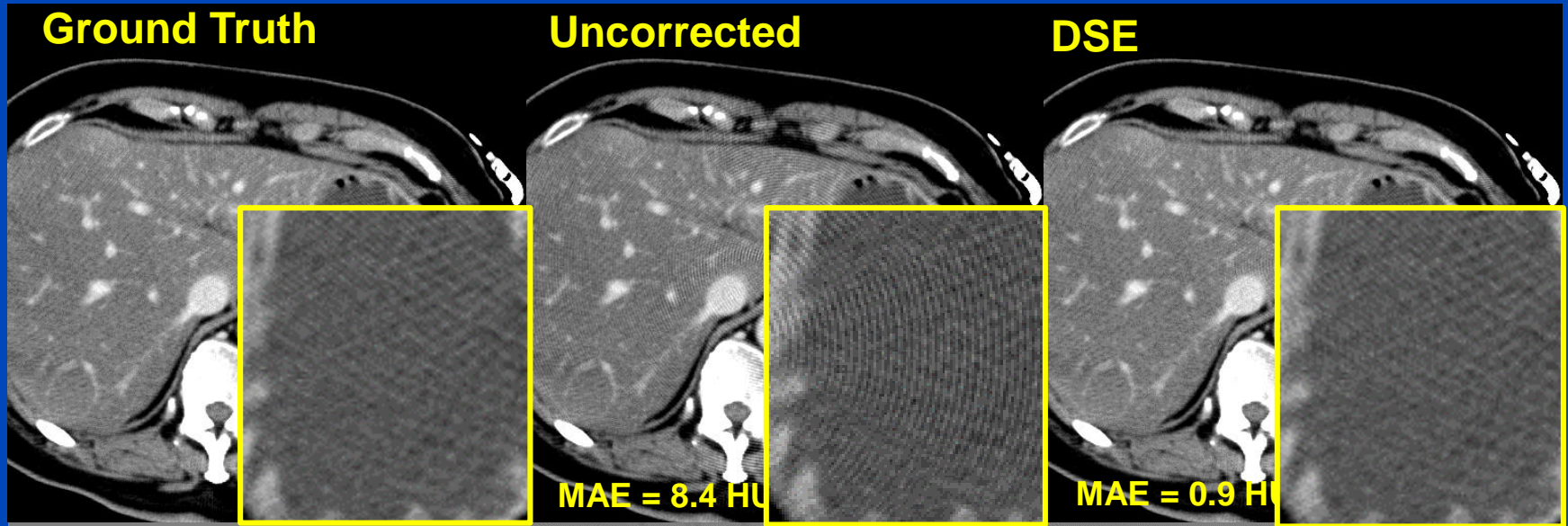
# Results in Reconstructed Images



Simulated Reconstruction  $C = 0$  HU,  $W = 400$  HU,  
Difference to GT  $C = 0$  HU,  $W = 50$  HU



# Results in Reconstructed Images

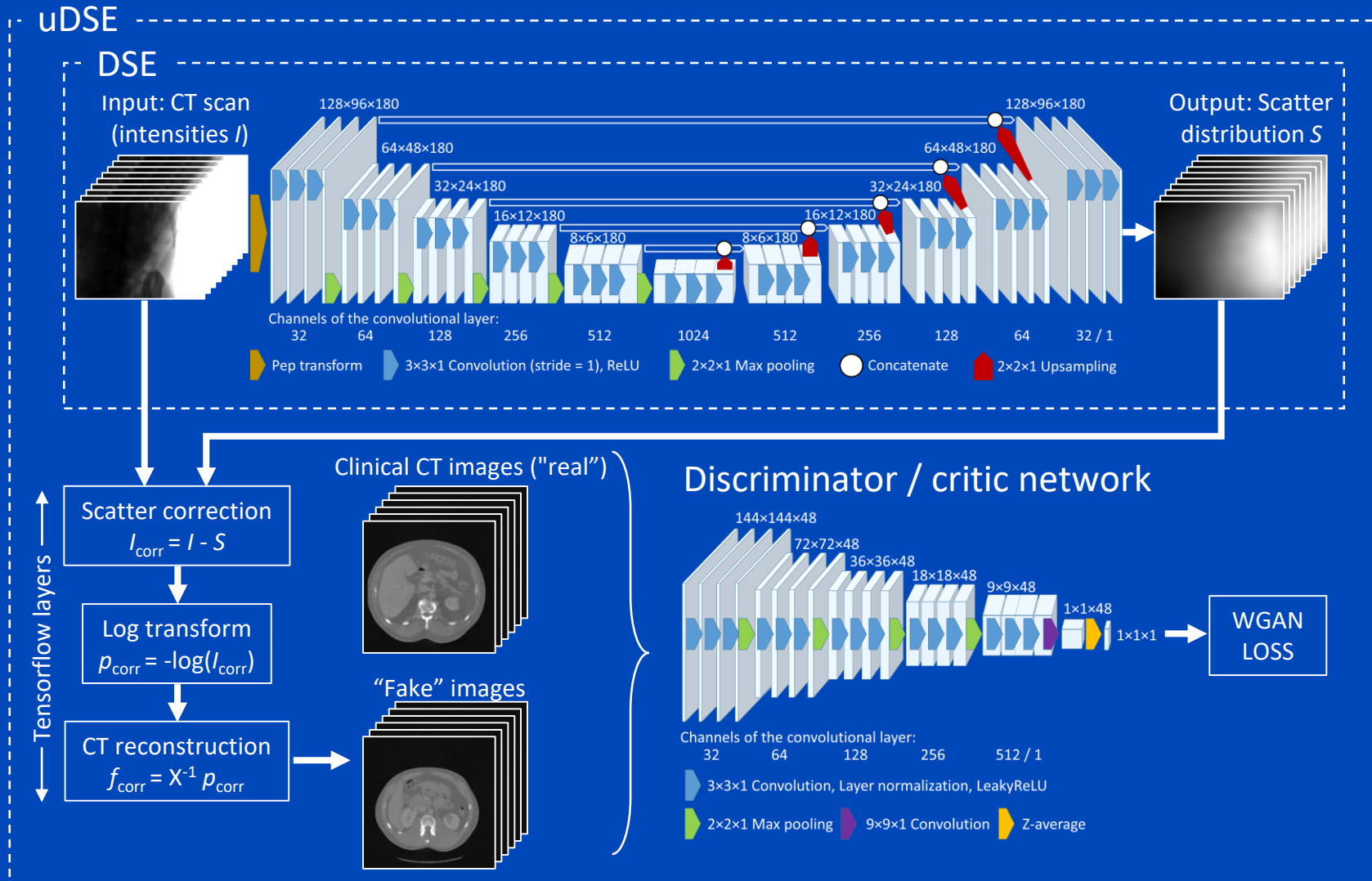


Simulated Reconstruction  $C = 0$  HU,  $W = 400$  HU,  
Difference to GT  $C = 0$  HU,  $W = 50$  HU

# Conclusions

- Coarse anti-scatter grid can lead to moiré artifacts due to scattered radiation.
- DSE reduces the mean absolute error (MAE) from about 9 HU to under 1 HU.
- The moiré pattern's amplitude can be reduced from 30 HU to less than 5 HU.

# uDSE – Basis Principle



# Datasets

- Training and testing data were generated using CT simulations based on 65 clinical CT reconstructions.
- Based on the corresponding voxel volumes, CBCT scans (120 kV, shifted detector, RFD = 1100 mm, RF = 700 mm, 360 views 360°) were simulated at five different z-positions within the abdomen region.
- Generation of one scatter corrupted dataset (30 patients) that was used as input to the generator network, one scatter-free dataset (30 patients) that was used to provide ideal reference for the critic network, and a scatter-corrupted dataset (remaining patients) for testing.

# Training

- Training of conventional DSE as reference using the following loss function:

$$L_{\text{DSE}}(\theta) = \sum_n^B \left| \frac{\text{DSE}_{\theta}(I_n) - S_n}{S_n} \right|$$

- Training of uDSE using a WGAN setup:

$$L_{\text{critic}}(\theta_c) = \sum_n^B C_{\theta_c}(G_{\theta_g}(I_n)) - C_{\theta_c}(f_{\text{real}, n}),$$

$$L_{\text{gen}}(\theta_g) = - \sum_n^B C_{\theta_c}(G_{\theta_g}(I_n)),$$

# Results

## Scatter Estimates

Primary + scatter (input)

Ground truth

DSE scatter prediction

uDSE scatter prediction

$C = 0.06, W = 0.12$

$C = 0.007, W = 0.007$

$C = 0.007, W = 0.007$

$C = 0.007, W = 0.007$

Error w.r.t.  
ground truth

$C = 0 \%, W = 40 \%$

$C = 0 \%, W = 40 \%$

$C = 0 \%, W = 40 \%$

# Results

## CT Reconstructions

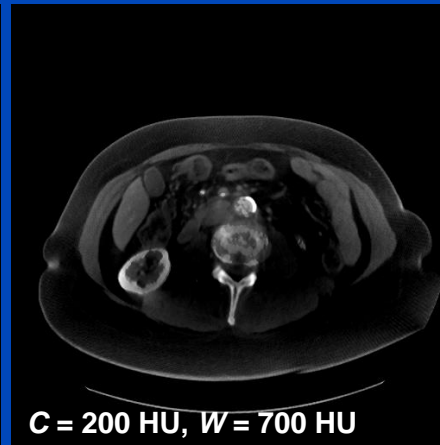
Ground truth

No correction

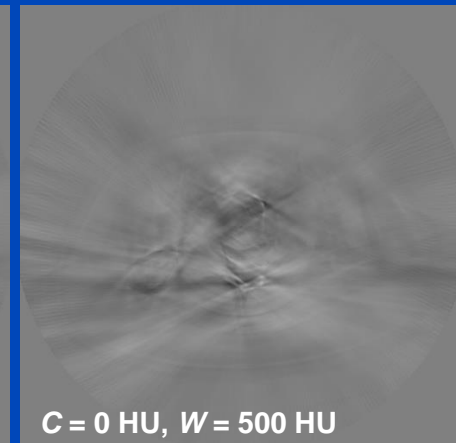
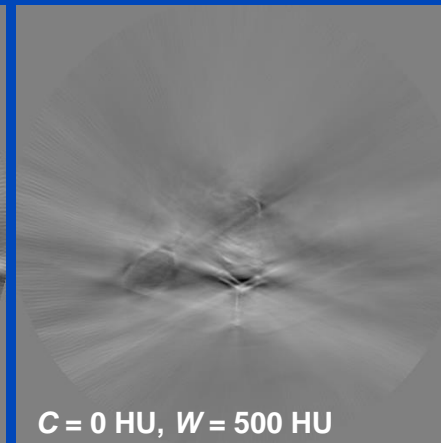
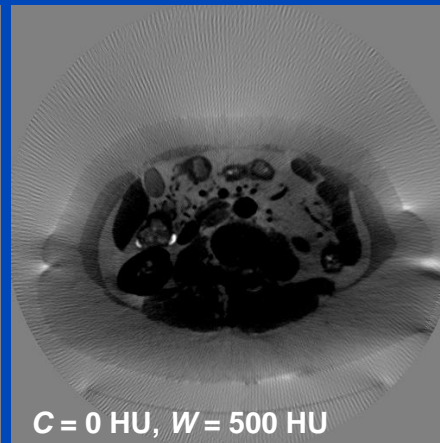
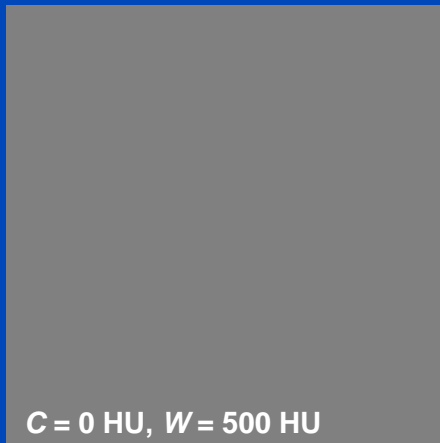
DSE correction

uDSE correction

CT reconstruction



Difference to ground truth

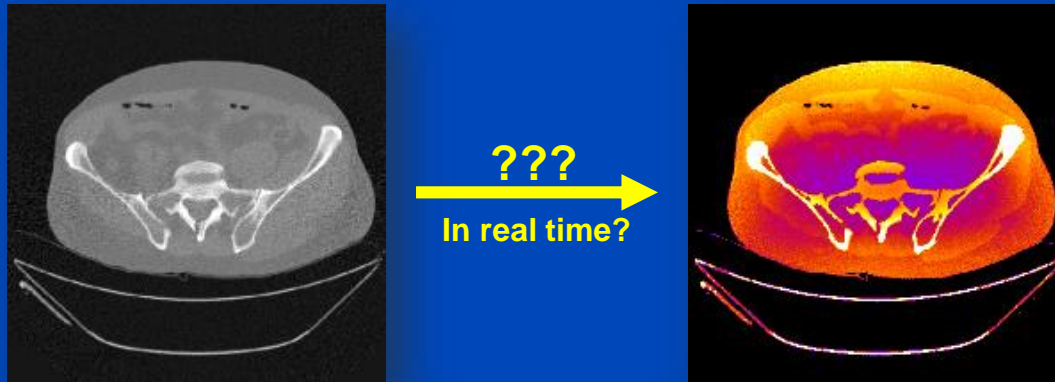


# Conclusions on uDSE

- This study demonstrates the feasibility of learning CT scatter estimation in absence of labeled data.
- uDSE is able to remove most of the present scatter artifacts and yields similar CT value accuracy (mean error of 27.9~HU vs. 24.7~HU) as a state-of-the-art supervised scatter estimation approach
- In general uDSE is not restricted to CBCT but can be trained with any tomographic input and any scatter-free reference as long as both distributions are sufficiently equal after scatter correction.
- Thus, uDSE has the potential to extend the concept of neural network-based scatter estimation and correction to scenarios where labels are not available or cannot be generated with sufficient accuracy.



# Deep Dose Estimation



# Estimation of Dose Distributions

- Useful to study dose reduction techniques
  - Tube current modulation
  - Prefiltration and shaped filtration
  - Tube voltage settings
  - ...
- Useful to estimate patient dose
  - Risk assessment requires segmentation of the organs (difficult)
  - Often semiantropomorphic patient models take over
  - The infamous k-factors that convert DLP into  $D_{\text{eff}}$  are derived this way, e.g.  $k_{\text{chest}} = 0.014 \text{ mSv/mGy/cm}$
  - ...
- Could be useful for patient-specific CT scan protocol optimization
- However: Dose estimation does not work in real time!

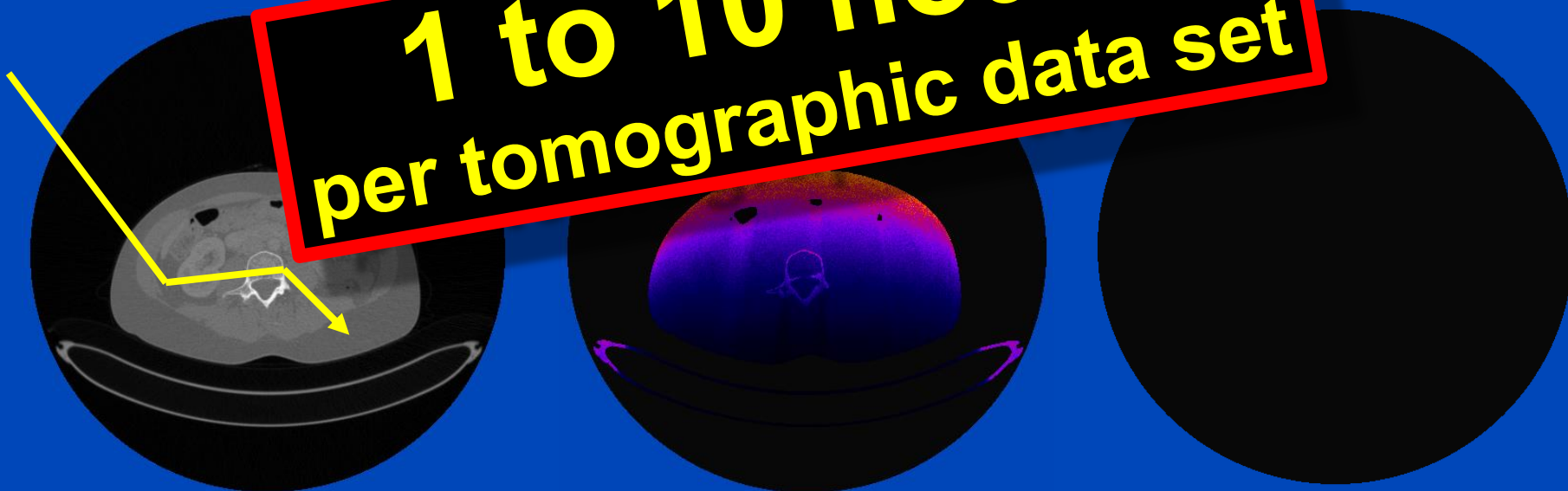
# MC Dose Simulation for a 360° Scan

Patient

Dose

Relative Dose

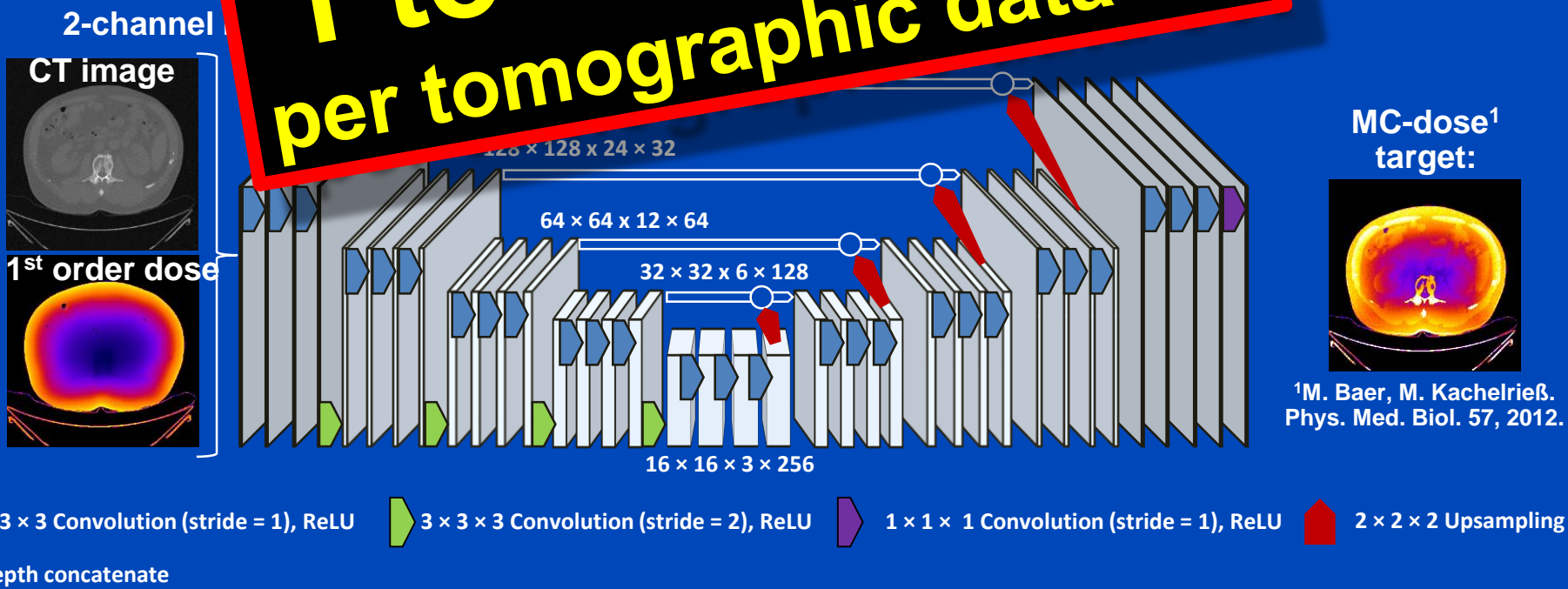
**1 to 10 hours  
per tomographic data set**



# Deep Dose Estimation (DDE)

- Combine fast and accurate CT dose estimation using a deep convolutional neural network
- Train the network to reproduce Monte Carlo (MC) estimates given the CT image as input.

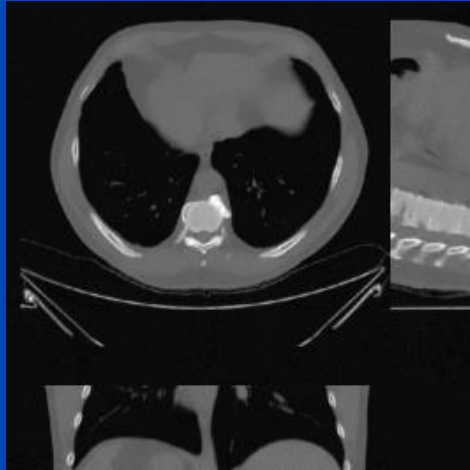
**1 to 10 seconds per tomographic data set**



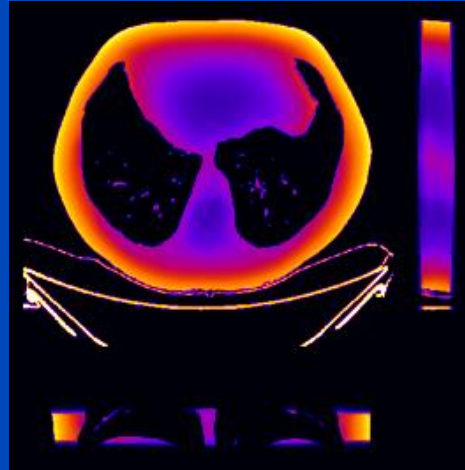
# Results

Thorax, tube A, 120 kV, no bowtie

CT image



First order dose

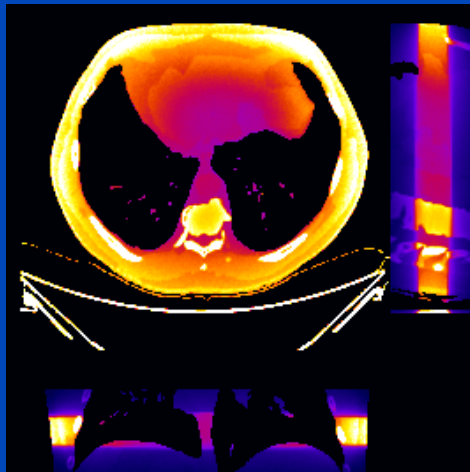


	MC	DDE
48 slices	1 h	0.25 s
whole body	20 h	5 s

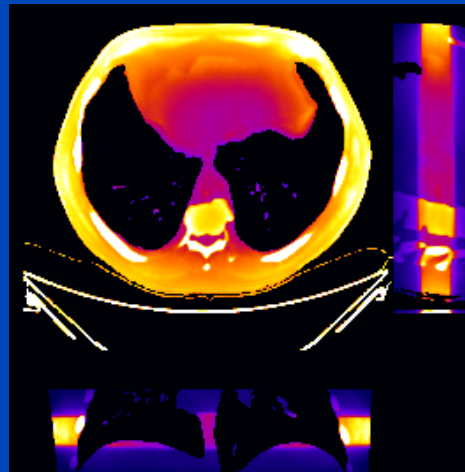
MC uses 16 CPU kernels  
DDE uses one Nvidia Quadro P600 GPU

DDE training took 74 h for 300 epochs,  
1440 samples, 48 slices per sample

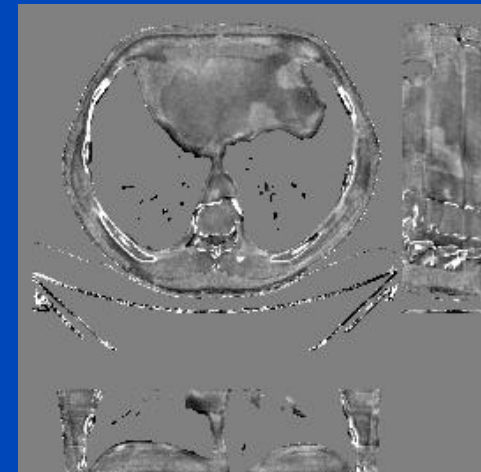
MC ground truth



DDE



Relative error

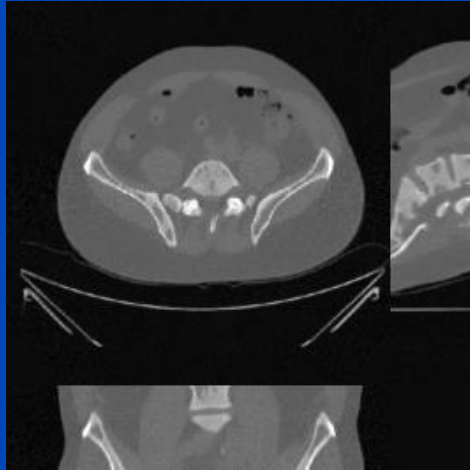


C = 0%  
W = 40%

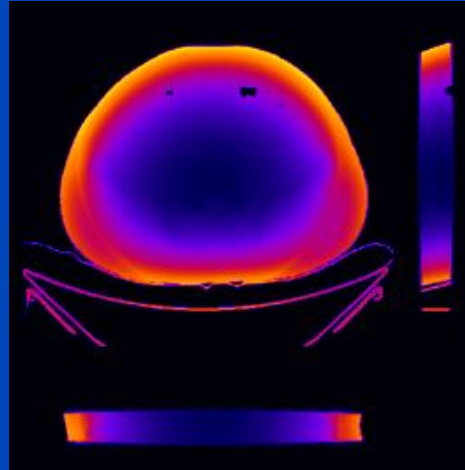
# Results

Pelvis, tube B, 120 kV, no bowtie

CT image



First order dose

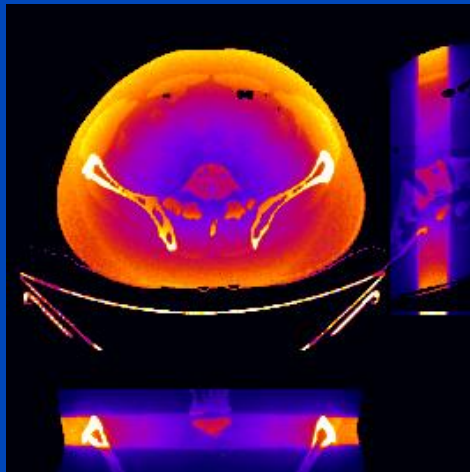


	MC	DDE
48 slices	1 h	0.25 s
whole body	20 h	5 s

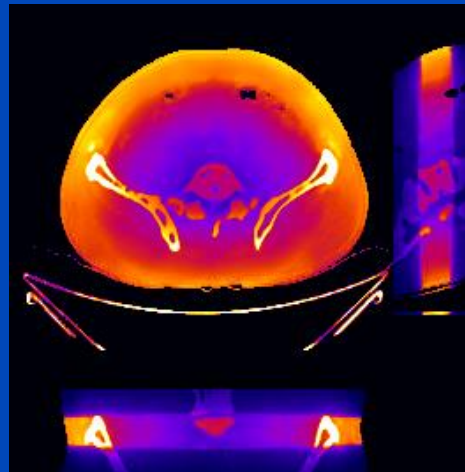
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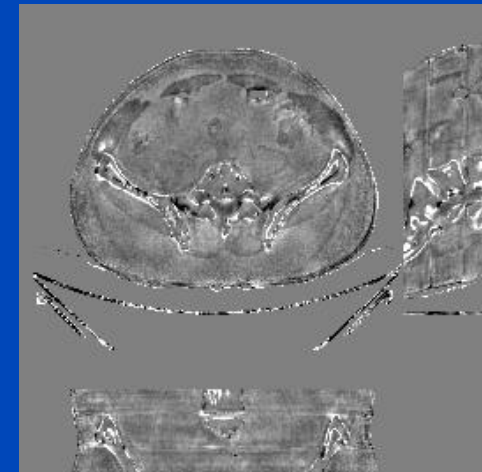
MC ground truth



DDE



Relative error



C = 0%  
W = 40%

# DDE's Organ Dose and $D_{\text{eff}}$ MAPEs

Organ and ICRP weight		80 kV	100 kV	120 kV
Bone marrow	0.12	5.2%	6.7%	7.1%
Bone surface	0.01	5.7%	7.0%	7.2%
Brain	0.01	5.1%	4.9%	5.3%
Breast	0.12	1.0%	1.4%	2.1%
Colon	0.12	0.9%	1.7%	1.9%
Esophagus	0.04	1.3%	2.4%	2.3%
Gonads	0.08	3.2%	2.7%	2.2%
Liver	0.04	2.9%	1.1%	0.8%
Lung	0.12	1.7%	3.5%	4.0%
Remainder	0.12	0.9%	1.9%	2.3%
Salivary glands	0.01	4.9%	5.1%	5.3%
Skin	0.01	2.8%	3.3%	4.2%
Stomach	0.12	2.3%	1.1%	0.8%
Thyroid gland	0.04	3.1%	3.0%	2.3%
Urinary bladder	0.04	1.7%	1.7%	1.3%
<b>Effective dose</b>		<b>1.2%</b>	<b>2.5%</b>	<b>2.7%</b>

Weighting factors and mean absolute percentage error of the DDE organ dose values with respect to the ground truth Monte Carlo organ dose values.

# Conclusions on DDE

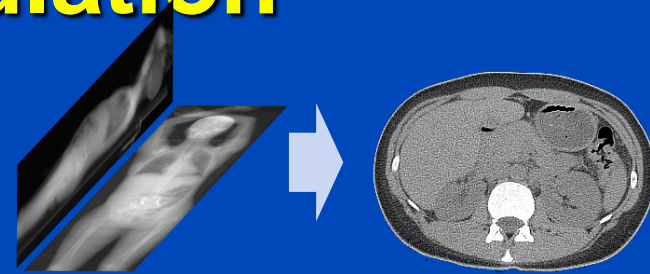
- **DDE provides accurate dose predictions**
  - for circle scans
  - for sequence scans
  - for partial scans (less than 360°)
  - for limited angle scans (less than 180°)
  - for spiral scans
  - for different tube voltages
  - for scans with and without bowtie filtration
  - for scans with tube current modulation
- **In practice it may therefore be not necessary to perform separate training runs for these cases.**
- **Thus, accurate real-time patient dose estimation may become feasible with DDE.**



# Patient Risk-Minimizing Tube Current Modulation

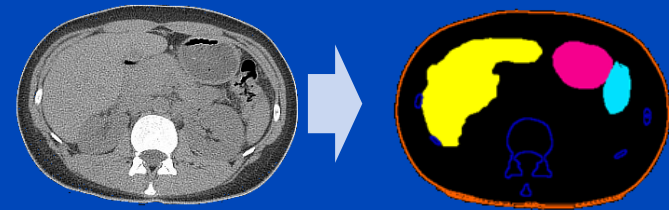
## 1. Coarse reconstruction from two scout views

- E.g. X. Ying, et al. X2CT-GAN: Reconstructing CT from biplanar x-rays with generative adversarial networks. CVPR 2019.



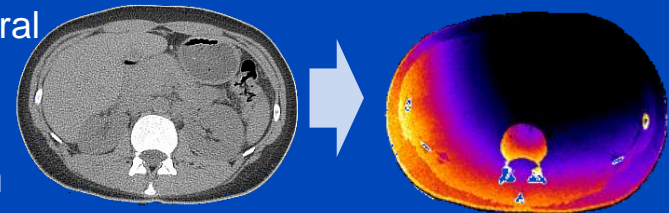
## 2. Segmentation of radiation-sensitive organs

- E.g. S. Chen, M. Kachelrieß et al., Automatic multi-organ segmentation in dual-energy CT (DECT) with dedicated 3D fully convolutional DECT networks. Med. Phys. 2019.



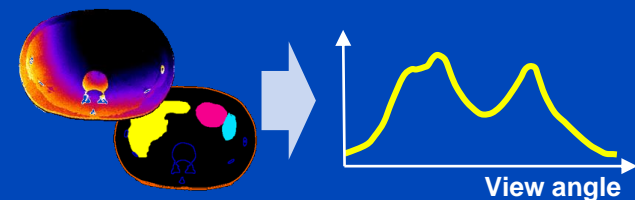
## 3. Calculation of the effective dose per view using the deep dose estimation (DDE)

- J. Maier, E. Eulig, S. Dorn, S. Sawall and M. Kachelrieß. Real-time patient-specific CT dose estimation using a deep convolutional neural network. IEEE Medical Imaging Conference Record, M-03-178: 3 pages, Nov. 2018.

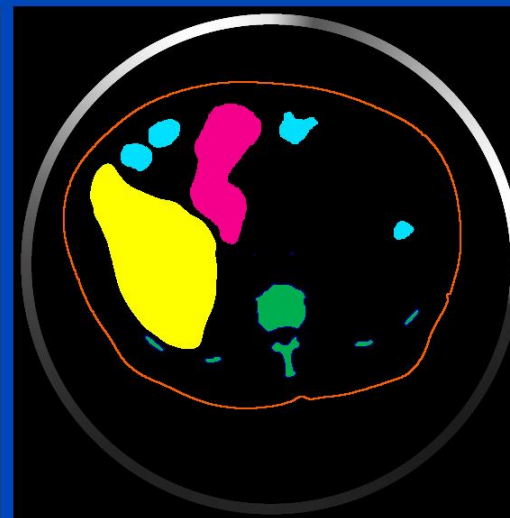
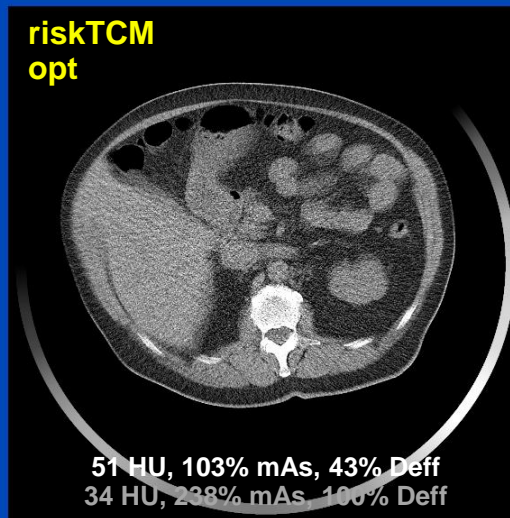
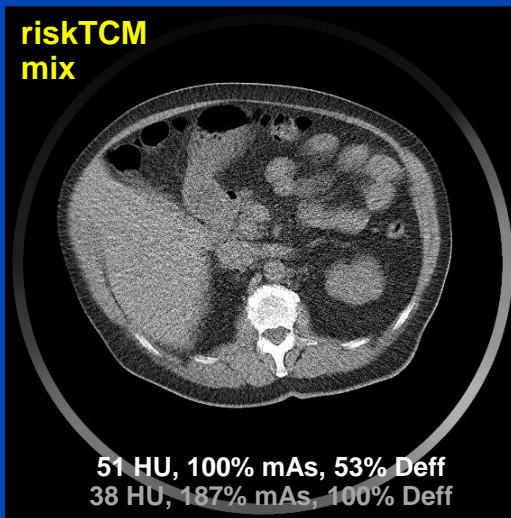
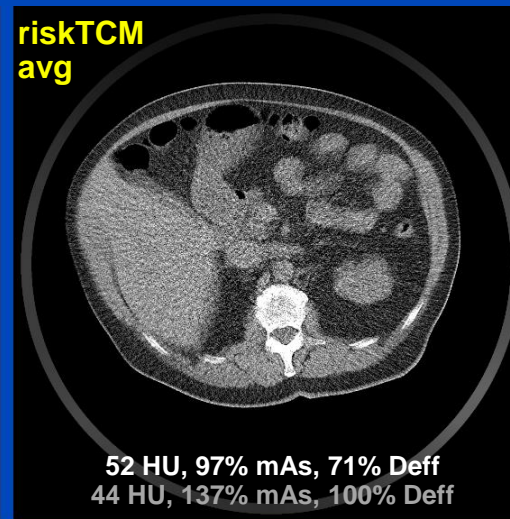
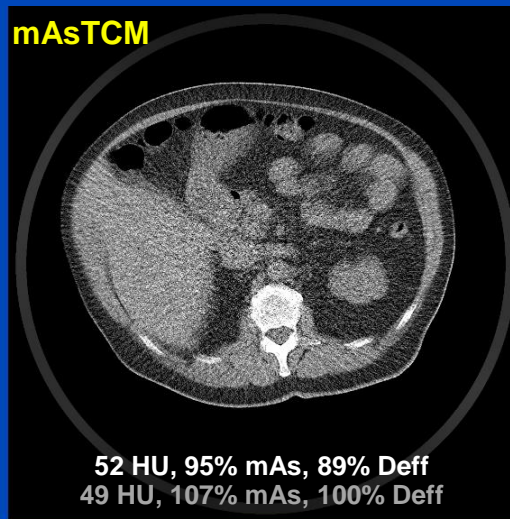
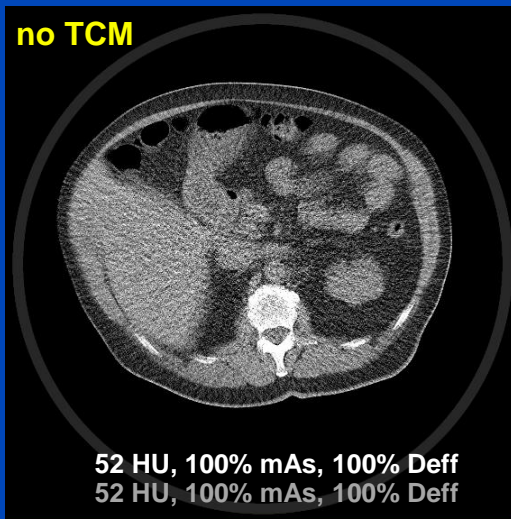


## 4. Determination of the tube current modulation curve that minimizes the radiation risk

- L. Klein, C. Liu, J. Steidel, L. Enzmann, M. Knaup, S. Sawall, A. Maier, M. Lell, J. Maier, and M. Kachelrieß. Patient-specific radiation risk-based tube current modulation for diagnostic CT. Med. Phys. 49(7):4391-4403, July 2022.



# Patient 04 - Abdomen



Re	0.12
BS	0.01
Br	0.01
Br	0.12
Co	0.12
RB	0.12
SG	0.01
Es	0.04
Li	0.04
Lu	0.12
Sk	0.01
St	0.12
Go	0.08
Th	0.04
BI	0.04

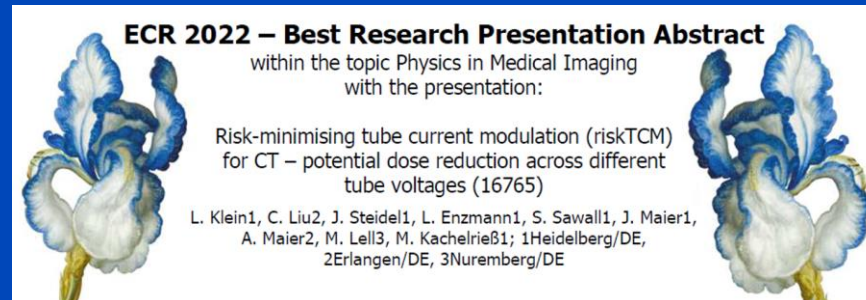
C = 25 HU, W = 400 HU

# Conclusions on RiskTCM

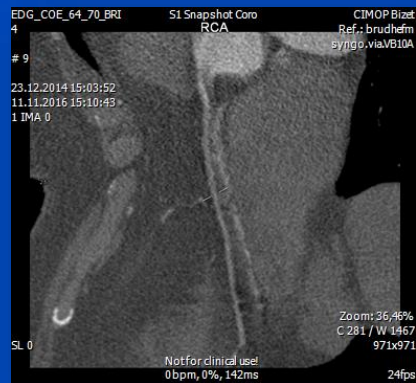
- Risk-specific TCM minimizes the patient risk.
- With  $D_{\text{eff}}$  as a risk model riskTCM can reduce risk by up to 30%, compared with the gold standard mAsTCM.
- Other risk models, in particular age-, weight- and sex-specific models, can be used with riskTCM as well.
- Note:

**It is up to the vendors to take action!**

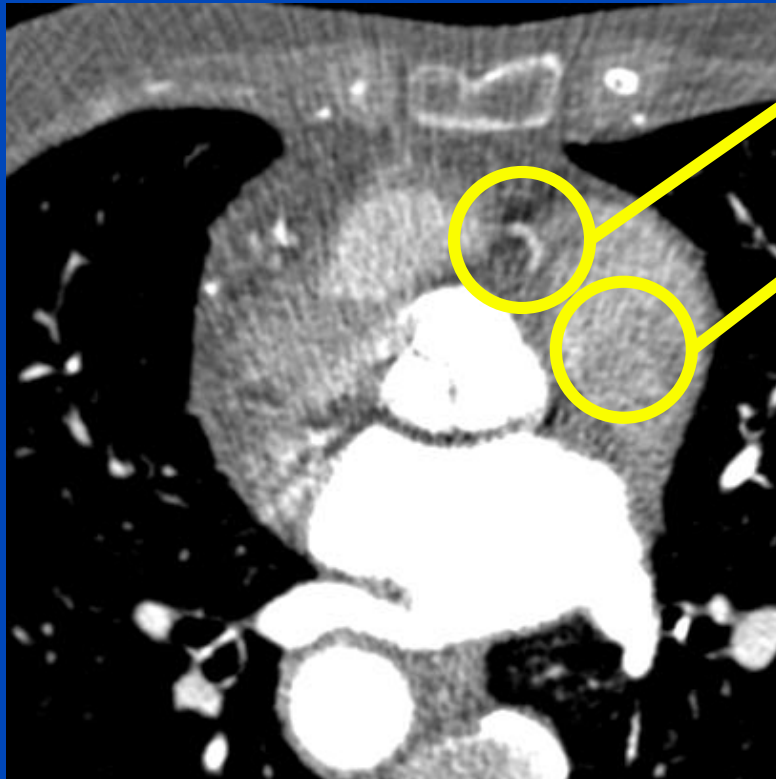
- **good for the patient**
- detector flux equalizing TCM = good for the detector



# Deep Cardiac Motion Compensation



# Motivation



$C = 0 \text{ HU}$ ,  $W = 1200 \text{ HU}$

Motion artifacts

High noise levels

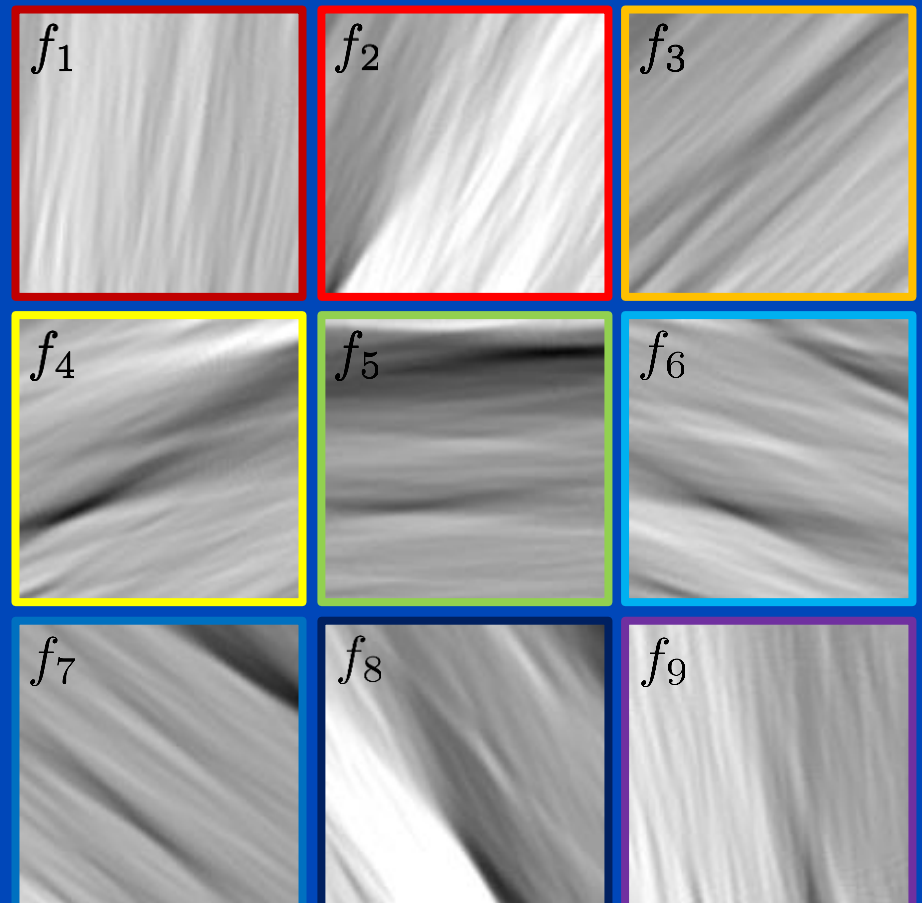
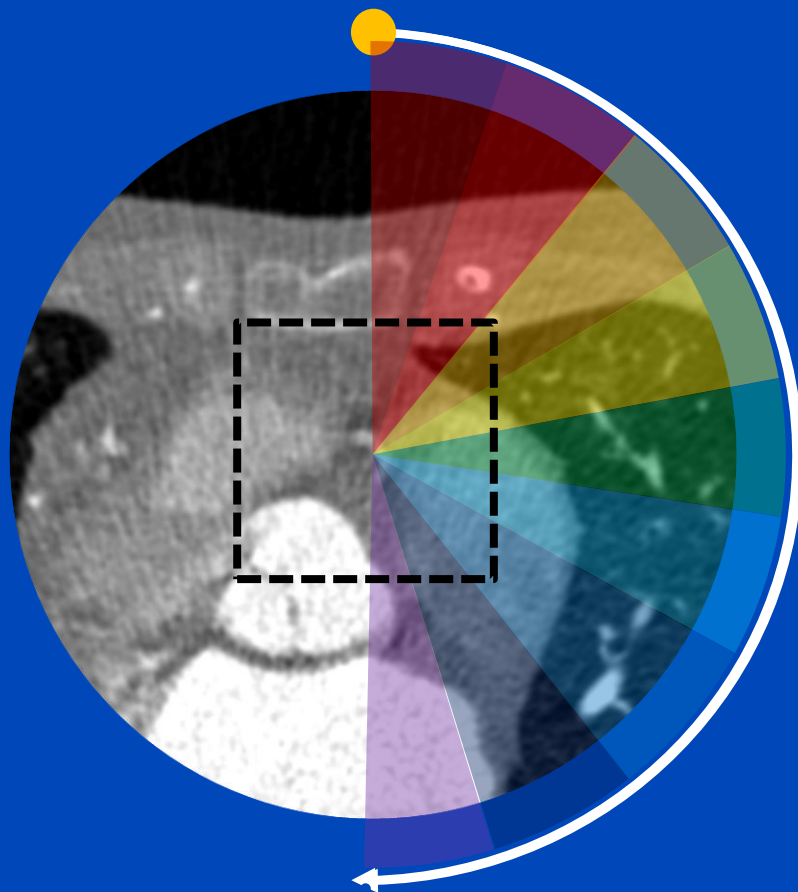
**Table 3: Reason for FFR<sub>CT</sub> Rejection in the ADVANCE Registry and Clinical Cohort** \*

Reason for Rejection	FFR <sub>CT</sub> Rejected*	
	ADVANCE Registry ( $n = 80$ )	Clinical Cohort ( $n = 892$ )
Inadequate image quality <sup>†</sup>		
Blooming	4 (5.0)	29 (3.0)
Clipped structure	4 (5.0)	39 (4.3)
Motion artifacts	63 (78.0)	729 (81.4)
Image noise	2 (2.5)	198 (22.1)
Inappropriate submission		
Stent or previous coronary artery bypass graft present	5 (6.2)	116 (13.0)
Cardiac hardware present	2 (2.5)	29 (3.2)

The rejection rate was 892 of 10 416 cases submitted

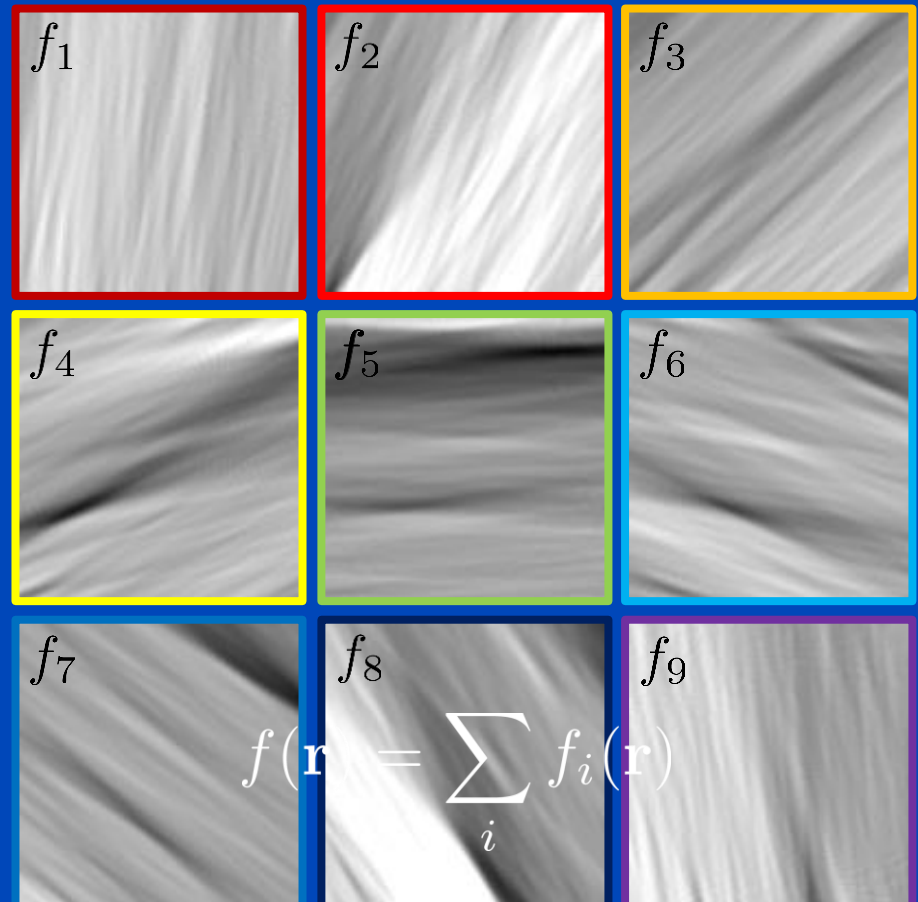
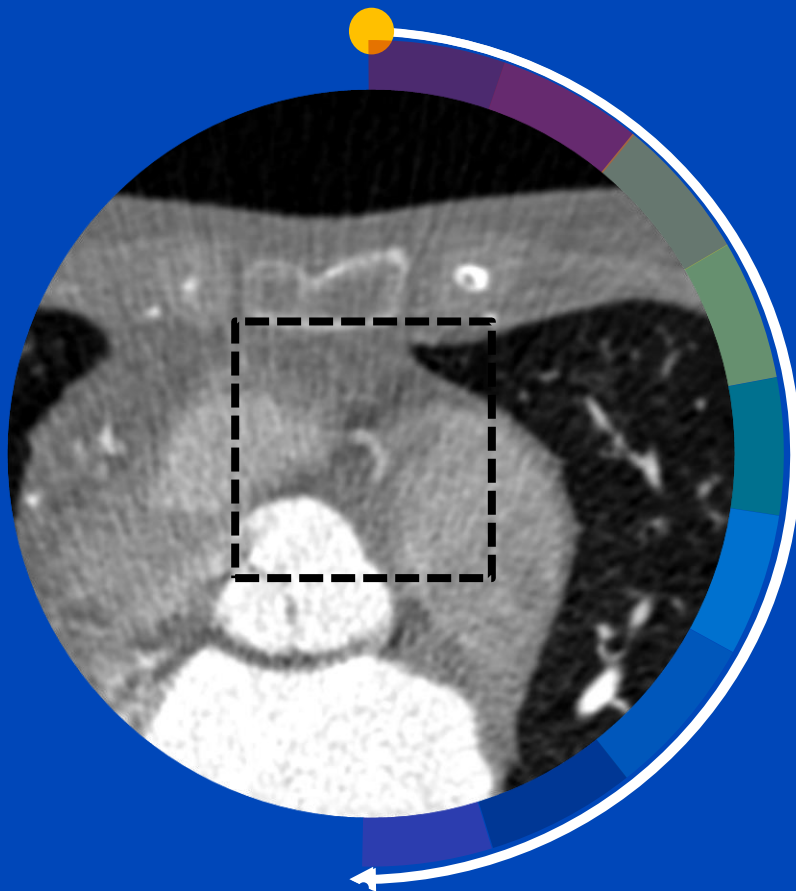
\* G. Pontone et al., “Determinants of Rejection Rate for Coronary CT Angiography Fractional Flow Reserve Analysis”, *Radiology*, 292(3), 597–605 (2019)

# Partial Angle-Based Motion Compensation (PAMoCo)

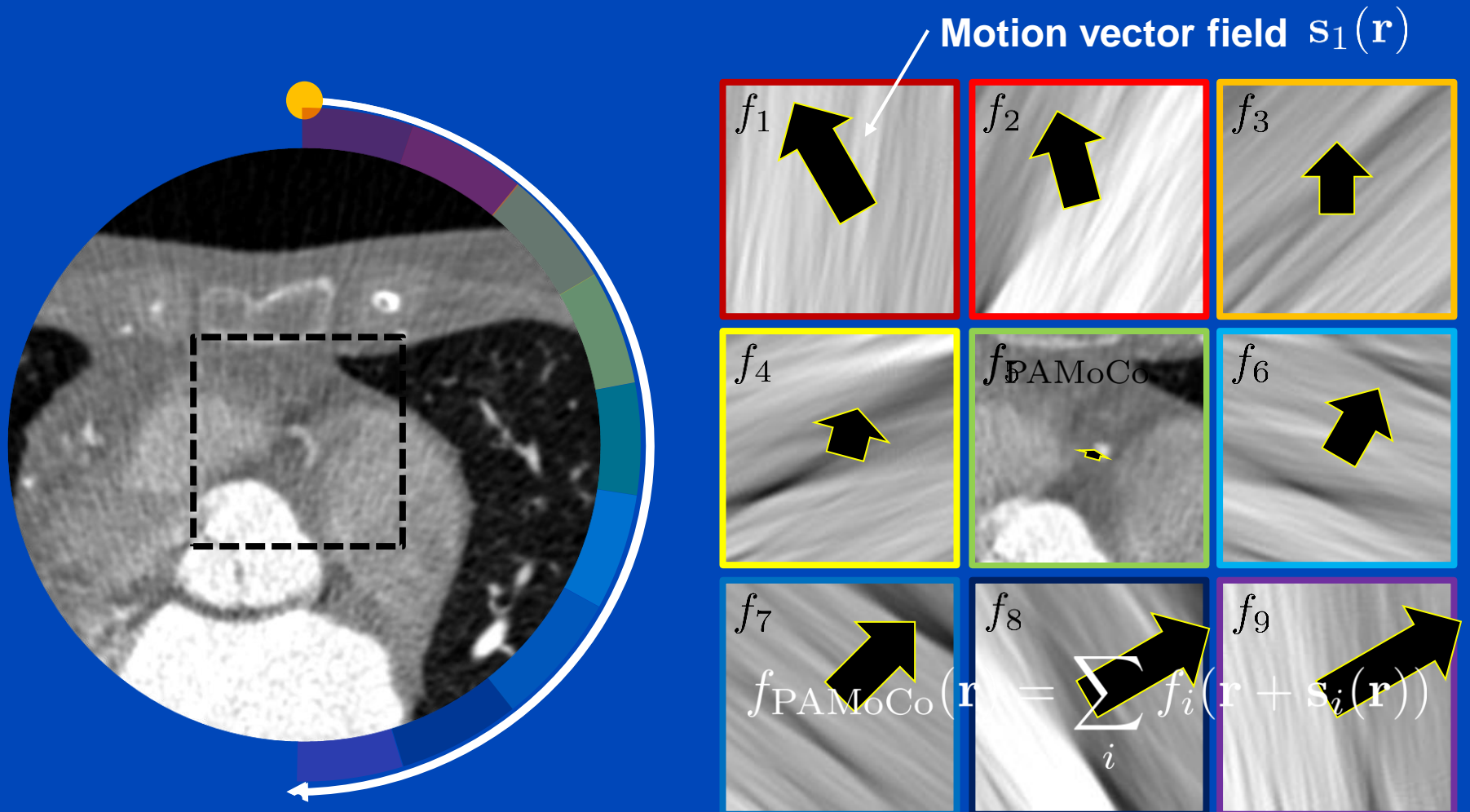


Animated rotation time = 100 × real rotation time

# Partial Angle-Based Motion Compensation (PAMoCo)



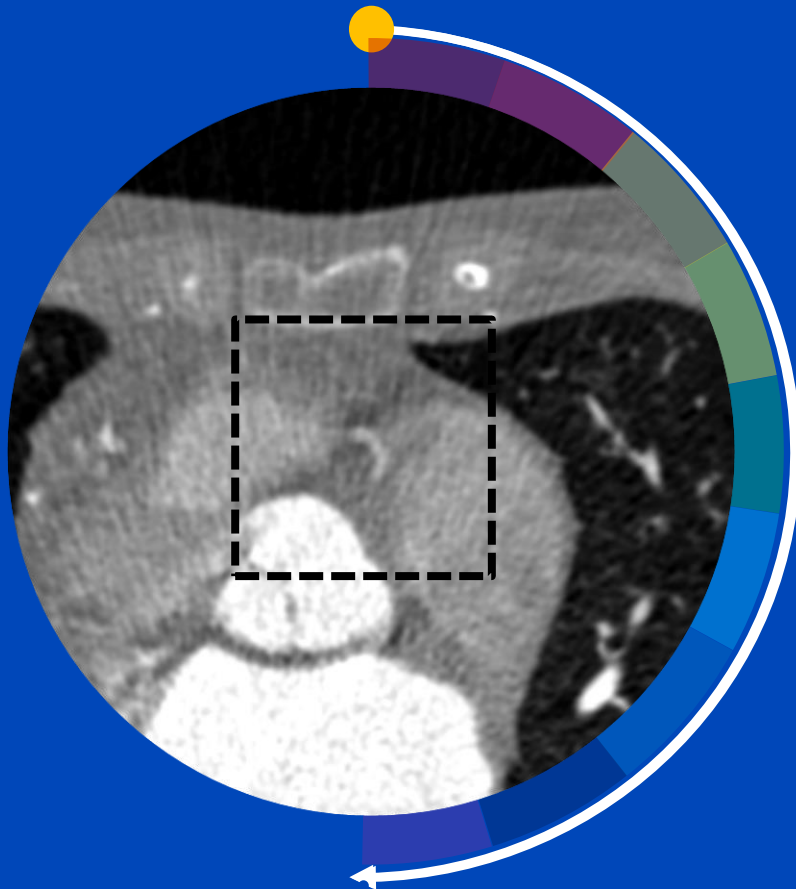
# Partial Angle-Based Motion Compensation (PAMoCo)



Apply motion vector fields (MVFs) to partial angle reconstructions



# Partial Angle-Based Motion Compensation (PAMoCo)



Prior work:

[1] S. Kim et al., “Cardiac motion correction based on partial angle reconstructed images in x-ray CT”, *Med. Phys.* 42 (5): 2560–2571 (2015).

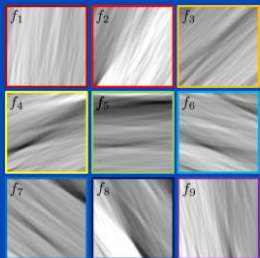
[2] J. Hahn et al., “Motion compensation in the region of the coronary arteries based on partial angle reconstructions from short-scan CT data”, *Med. Phys.* 44 (11): 5795–5813 (2017).

[3] S. Kim et al., “Cardiac motion correction for helical CT scan with an ordinary pitch”, *IEEE TMI* 37 (7): 1587–1596 (2018).

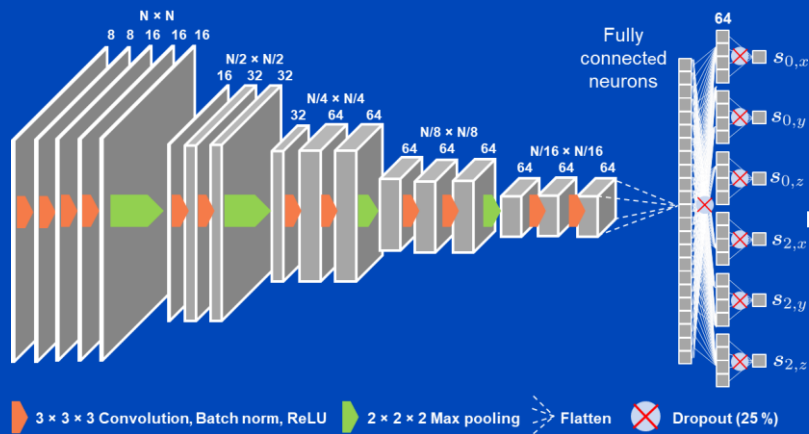
→ **Limitation: Challenging / time-consuming optimization**

# Deep Partial Angle-Based Motion Compensation (Deep PAMoCo)

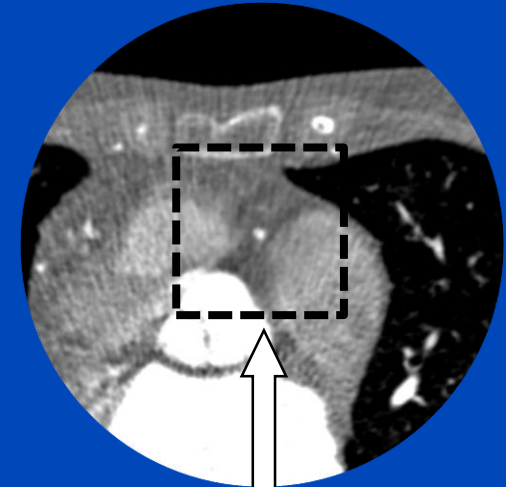
PARs centered around coronary artery



Neural network to predict parameters of a motion model

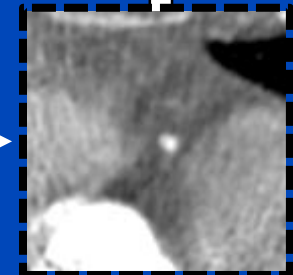


Reinsertion of patch into initial reconstruction



Spatial transformer

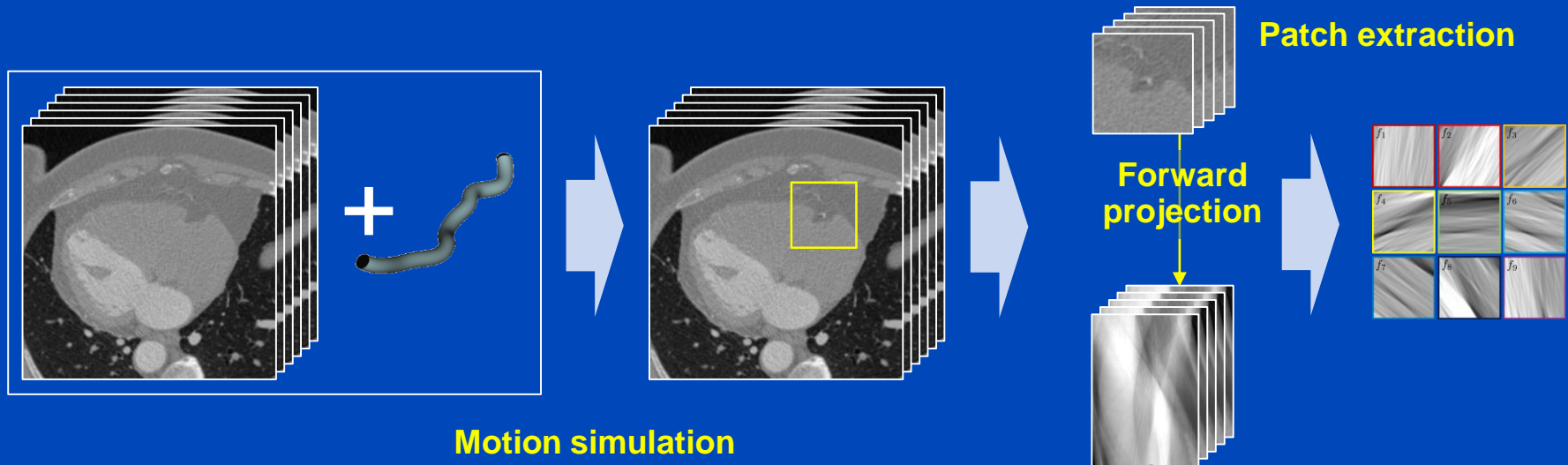
Application of the motion model to the PARs via a spatial transformer<sup>1</sup>



[1] M. Jaderberg et al., "Spatial transformer networks", NIPS 2015: 2017–2025 (2015).

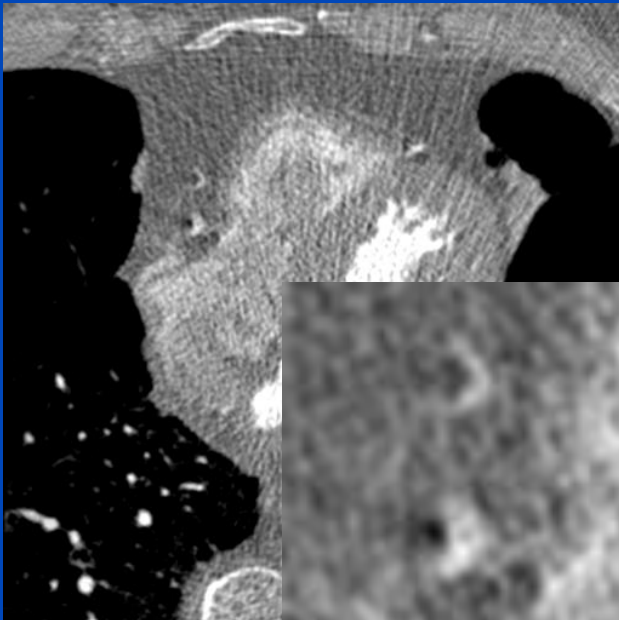
# Training Data Generation

- Removal of coronary arteries from real CT reconstructions.
- Insertion of artificial coronary arteries with different shape, size, and contrast.
- Simulation of CT scans with coronary artery motion.

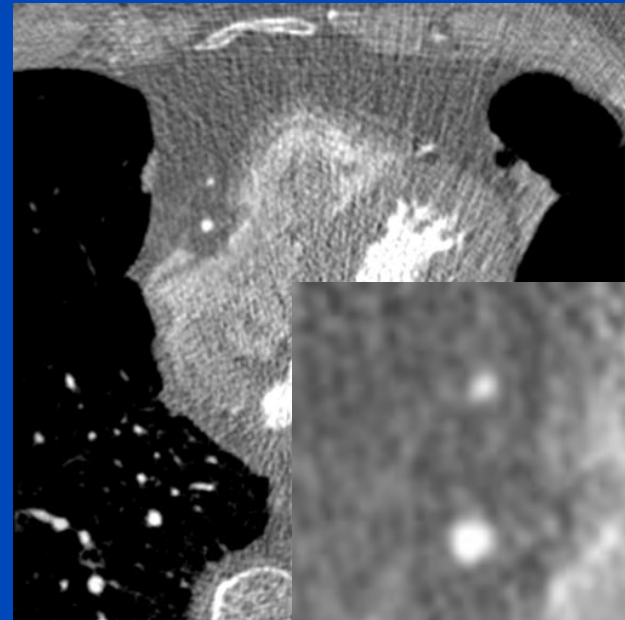


# Patient 1

Original



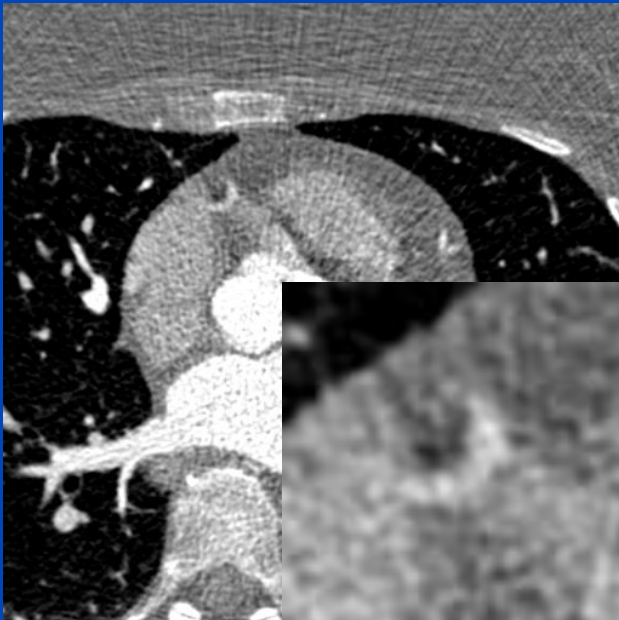
Deep PAMoCo



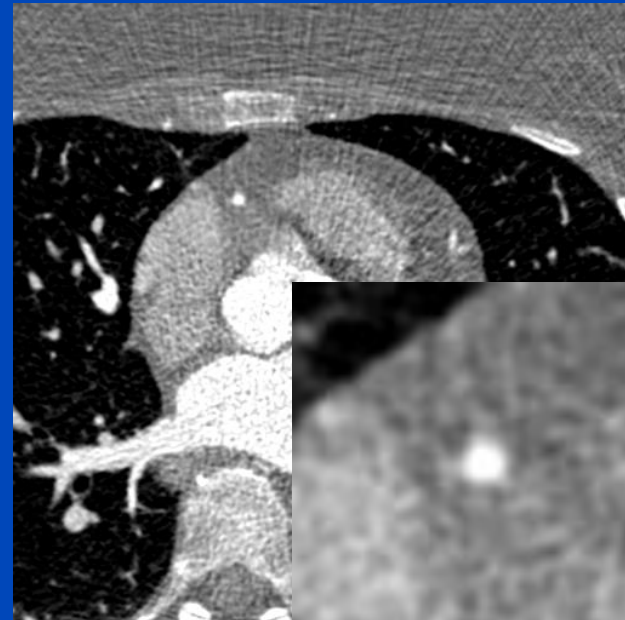
$C = 0 \text{ HU}$ ,  $W = 1400 \text{ HU}$

# Patient 2

Original



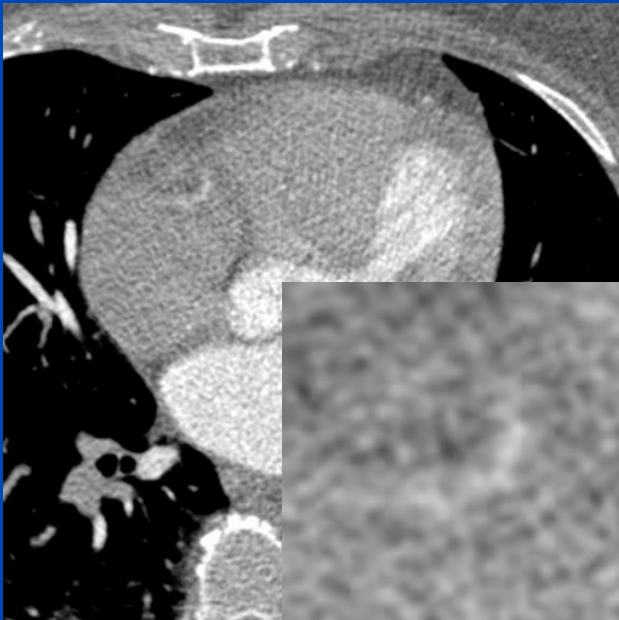
Deep PAMoCo



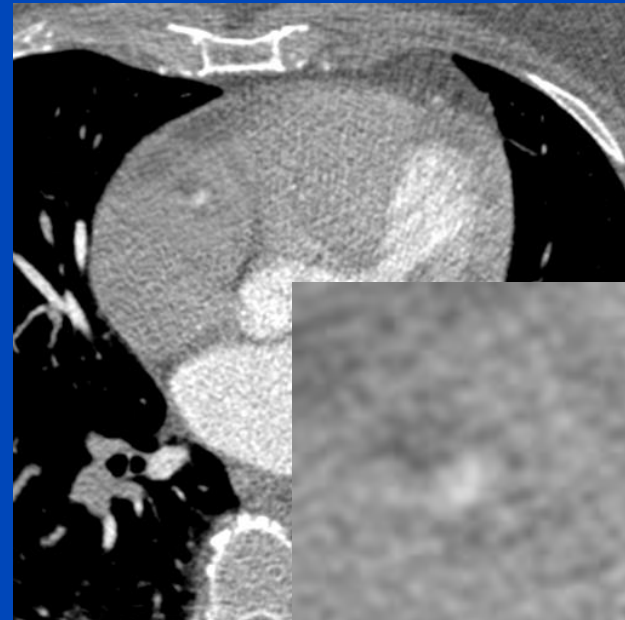
$C = 0 \text{ HU}$ ,  $W = 1600 \text{ HU}$

# Patient 3

Original



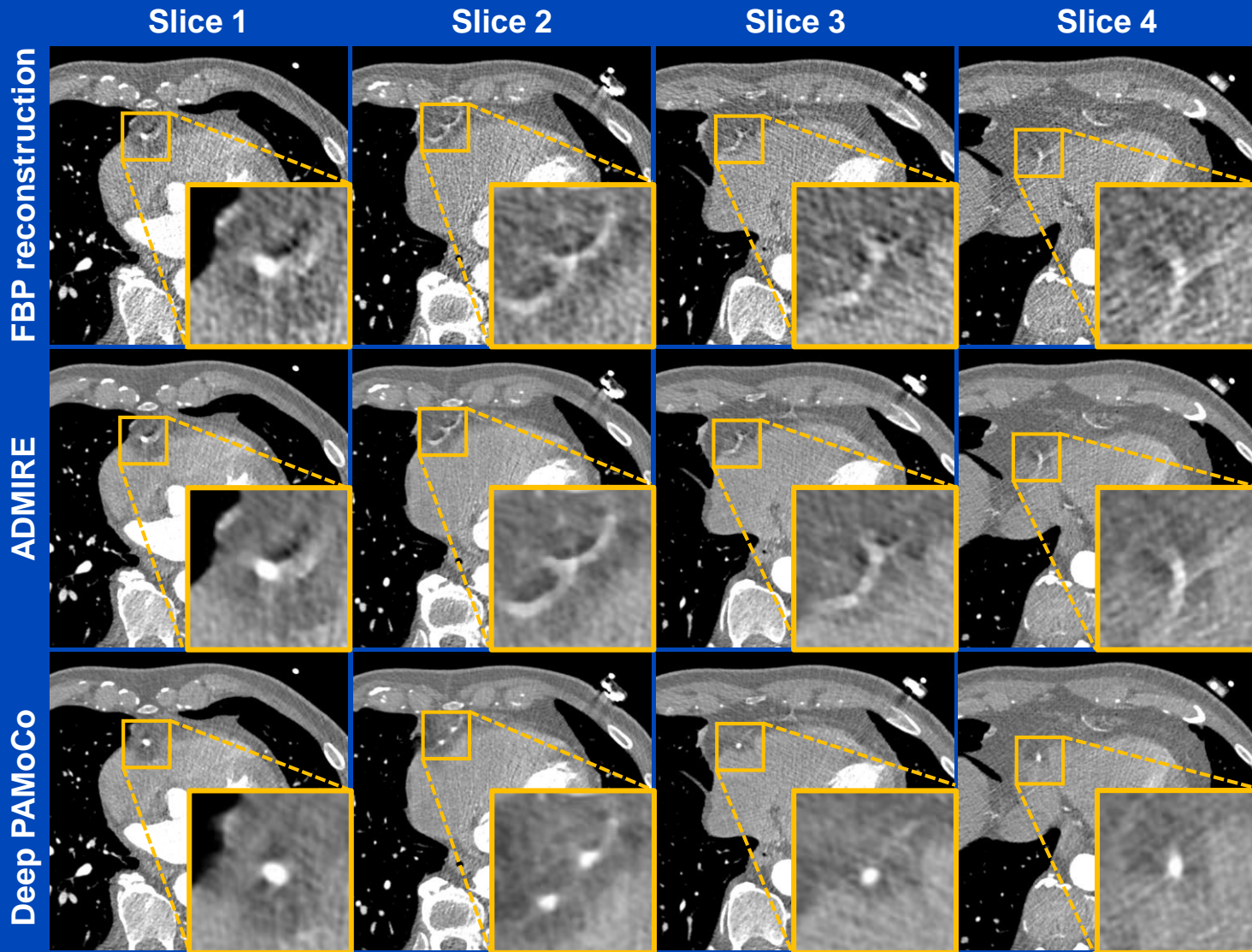
Deep PAMoCo



$C = 0 \text{ HU}$ ,  $W = 1000 \text{ HU}$

# Patient 4 (Iterative Recon)

Measurements at a Siemens Somatom AS, patient 1



$C = 0 \text{ HU}$ ,  $W = 1200 \text{ HU}$

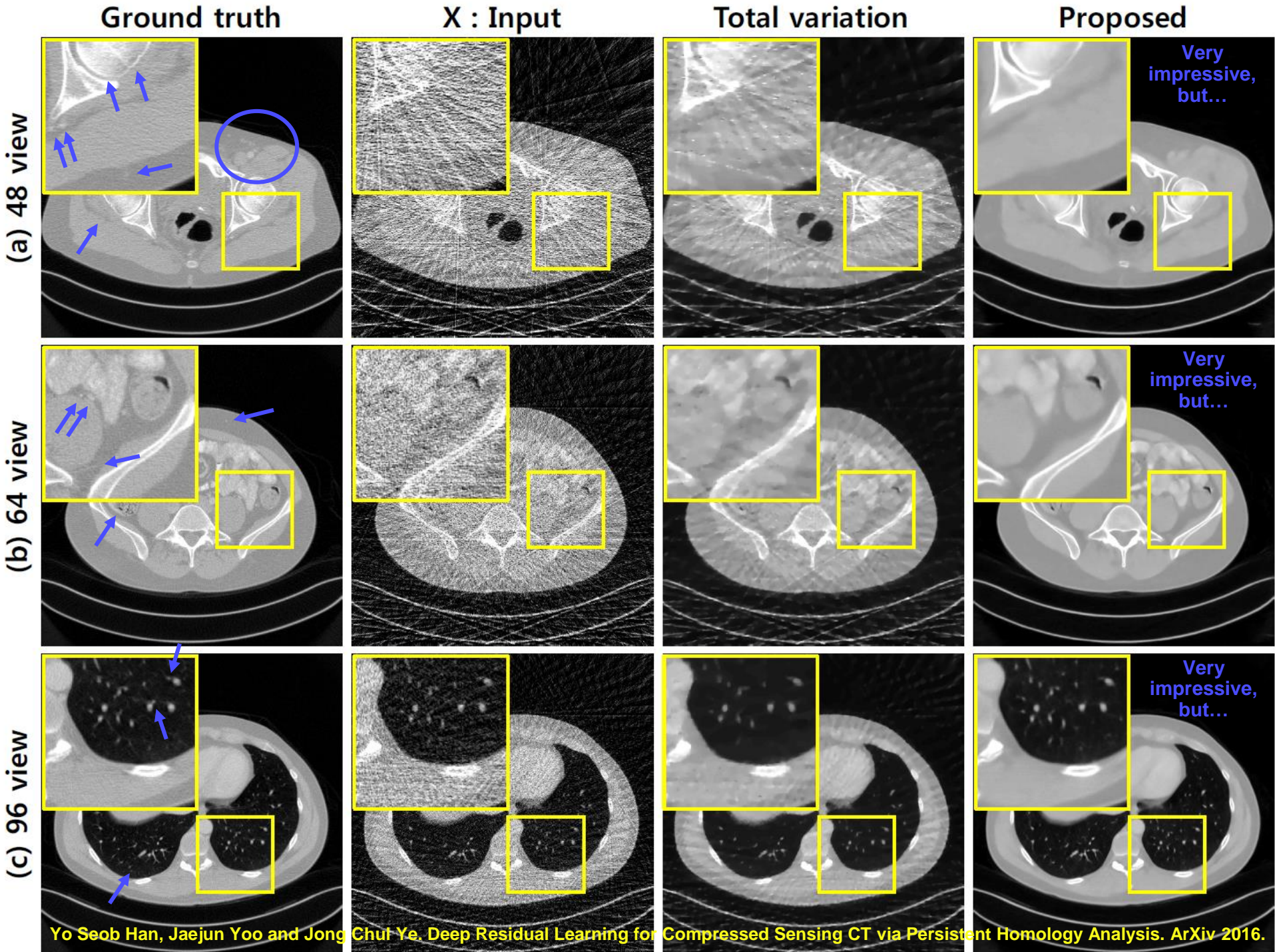
# Are the Methods Reliable?

- **Studies about explainability of AI in CT image formation are more than sparse.**
- **My thoughts:**
  - **Cosmetic corrections: Unclear if noise reduction, metal artifact reduction etc. is removing/adding lesions. The whole process is a black box.**
  - **Physical corrections: A clear physical meaning and rawdata fidelity appear more reliable. Examples:**
    - » **MAR or detruncation networks where the NN output is used only to forward project and inpaint/extrapolate the rawdata**
    - » **Scatter correction that estimates a smooth physically realistic (trained with MC) scatter signal in intensity domain**
    - » **Motion correction networks that estimate motion vectors rather than manipulating the voxel values**



# Explainable AI for CT: Analyzing CT Image Denoising Networks by Reconstructing their Invariances

- Elias Eulig, Björn Ommer, and Marc Kachelrieß
- RSNA 2022



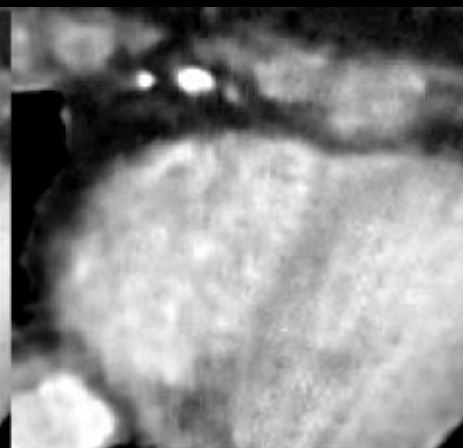
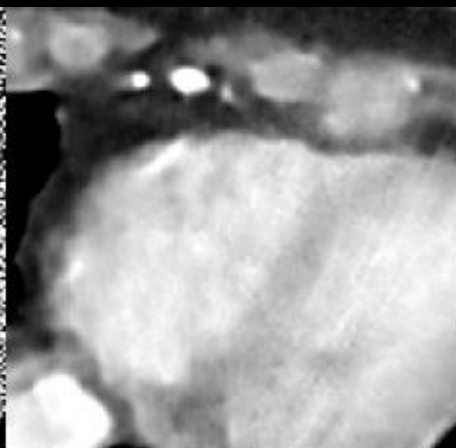
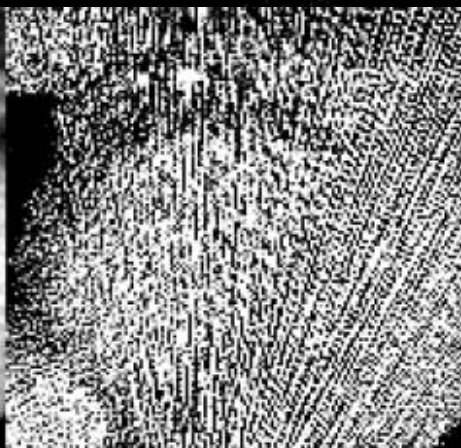
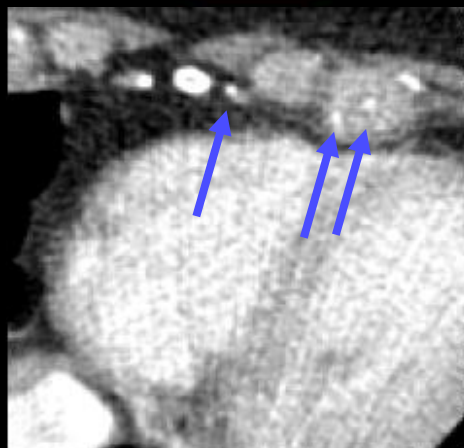
FBP(200 mAs)

FBP(10 mAs)

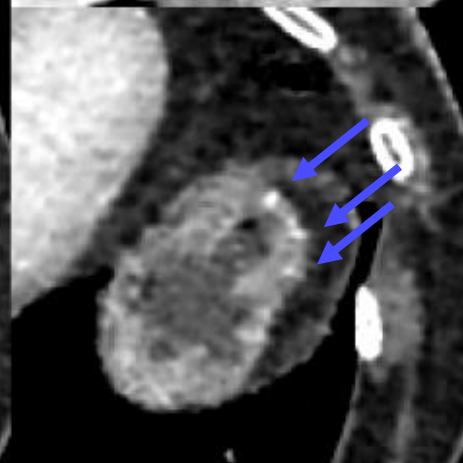
IRLNet(10 mAs, T-Net)

IRLNet(10 mAs, A-Net)

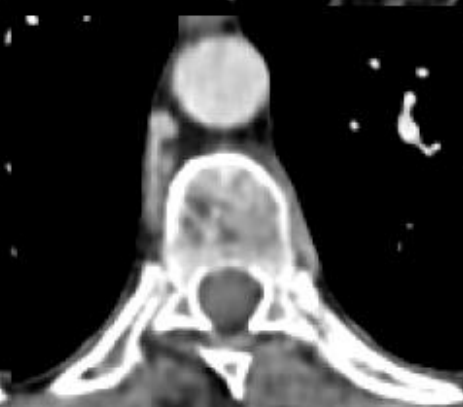
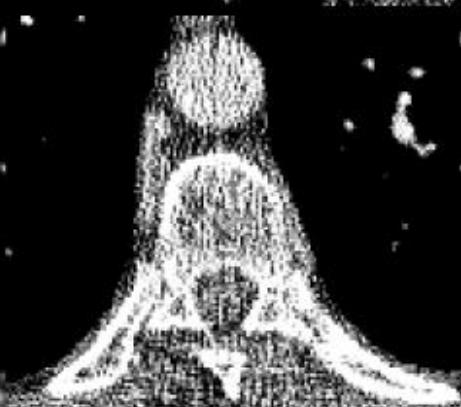
ROI 1



ROI 2



ROI 3



# Motivation

## In general:

- Deep learning methods are employed for many problems in medical image formation, including image-based noise reduction.
- However, they lack interpretability due to black-box nature of DNNs. Recent advancement in generative modelling signal false confidence.

## Aim of this work:

- Lay fundamentals for post-hoc interpretability and robustness analysis of denoising DNNs.
- Use two simple denoising networks  $f$  as initial examples:
  - Chen's simple 3-layer CNN trained with  $\mathcal{L}_2$  loss<sup>1</sup>
  - Yang's Wasserstein GAN with additional perceptual loss<sup>2</sup>
- See what they have learned to represent and what to ignore: For a given output  $x'$  there are many inputs  $x$  that produce the same output  $x' = f(x)$ .
- Employ low dose CT image and projection dataset for all studies.<sup>3</sup>

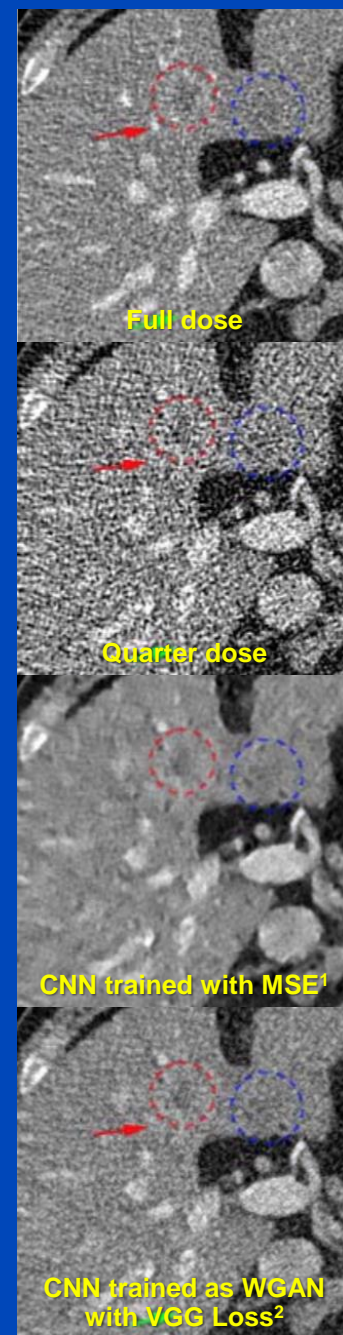


Figure from reference [2]

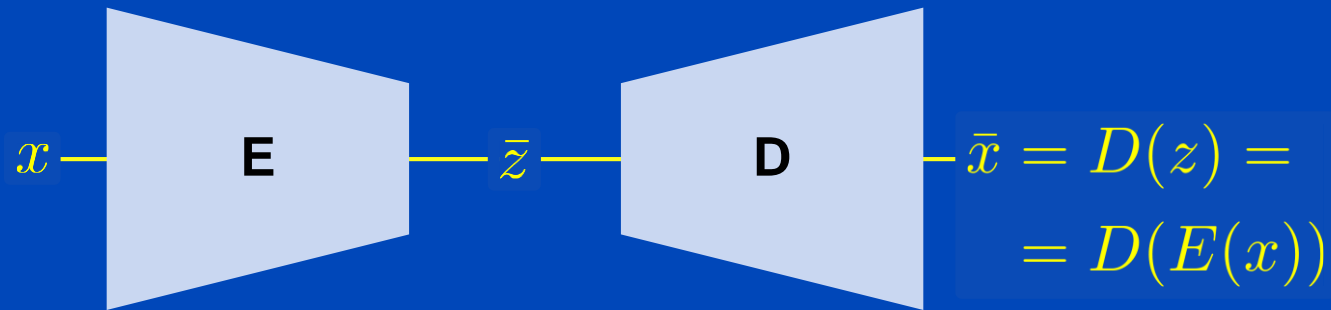
<sup>1</sup>H. Chen et al., "Low-dose CT denoising with convolutional neural network", ISBI 2017, 2017.

<sup>2</sup>Q. Yang et al., "Low-Dose CT Image Denoising Using a Generative Adversarial Network [...]", in *IEEE TMI*, vol. 37, no. 6, 2018.

<sup>3</sup>C. McCollough et al., "Data from low dose CT image and projection data [data set]," The Cancer Imaging Archive, 2020.

# Recap 1: What is an Autoencoder (AE)?

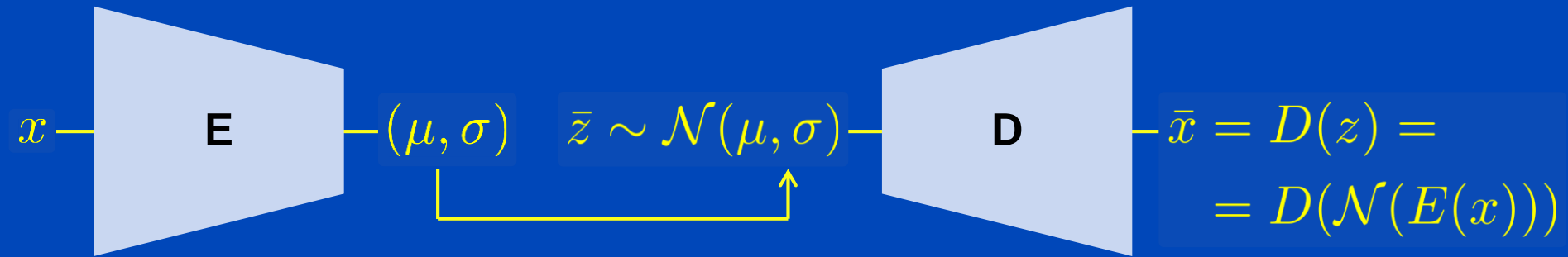
- In and output domain are the same, here  $x$ .
- Bottleneck  $z$  enforces the encoder and decoder to do a good job.



- **Examples:**
  - Principal component analysis (linear autoencoder), lossless
  - PCA with dimensionality reduction (nonlinear due to clipping), lossy
  - Image compression and decoding, e.g. jpeg, lossy
- Latent space typically not interpretable.

# Recap 2: What is a Variational AE (VAE)?

- Make latent space regular.
- Allow to sample in latent space from a given distribution, here: normal distribution.



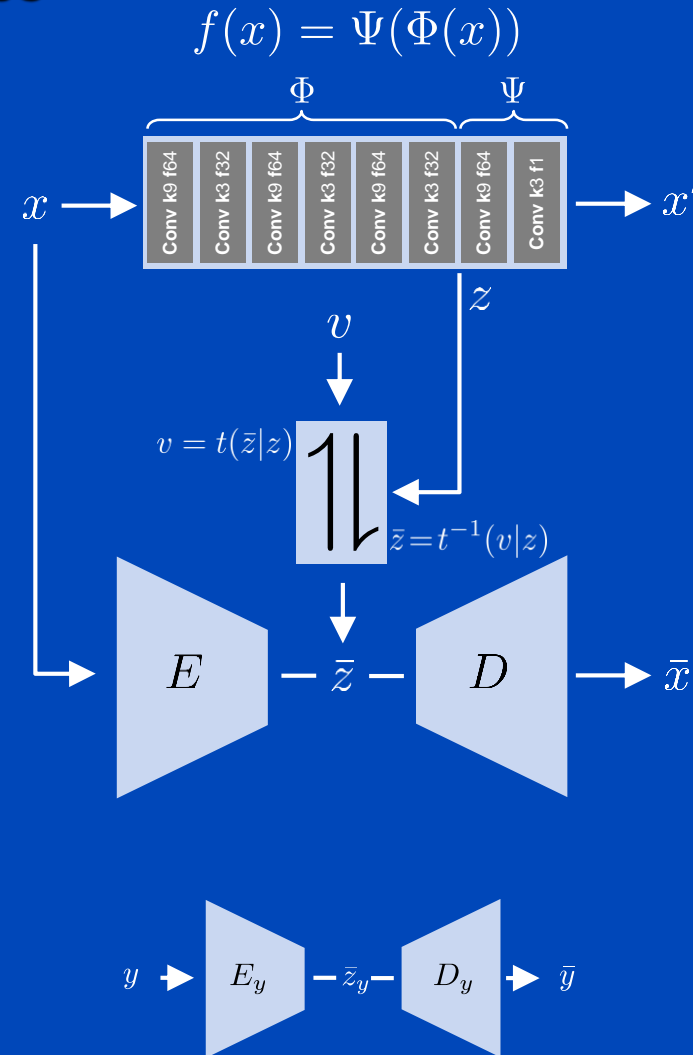
- The VAE is a generative model.
- It allows to generate new data by sampling new values from the normal distribution.

# Method

## Recovering Invariances

- Our work is based on Rombach et al.<sup>1</sup>
- Given a function or network  $f(x) = \Psi(\Phi(x))$  we analyze its internal latent representations  $z = \Phi(x)$ .
- Train a VAE to learn a complete data representation  $\bar{z} = E(x)$  of low dose images.
- Disentangle information captured in  $z$  and invariances  $v$  by learning a mapping  $v = t(\bar{z}|z)$ ,  $\mathcal{L}(v) = \mathcal{N}(0, 1)$
- $t(\cdot|z)$  is realized by a conditional invertible neural network (cINN).
- Generate new images varying only by their invariances

$$\bar{x} = D(t^{-1}(v|z)) \quad v \sim \mathcal{N}(0, 1)$$



Alternative: Use VAE in high dose domain, i.e.  $\text{VAE}_y$ , to visualize the invariances.

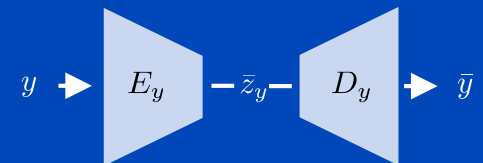
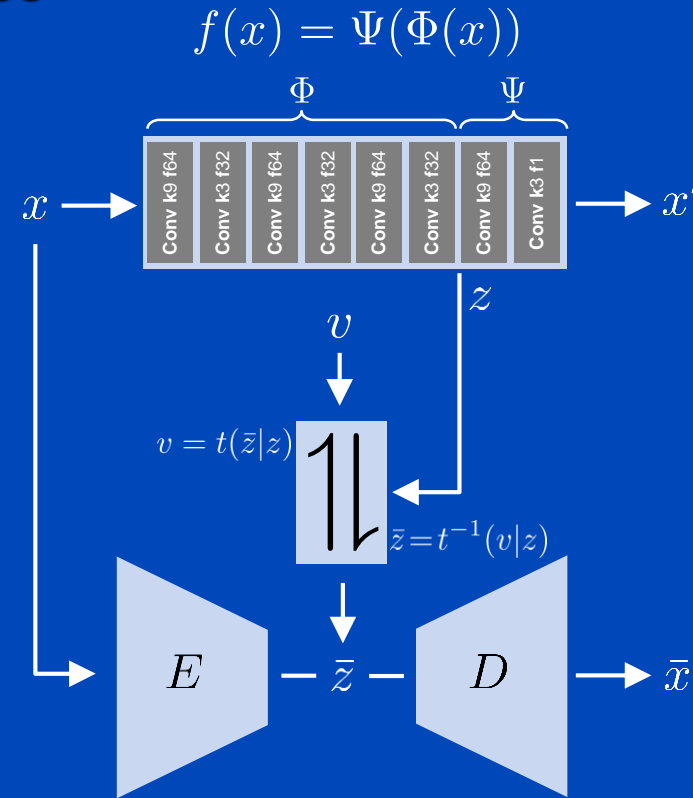
# Method

## Recovering Invariances

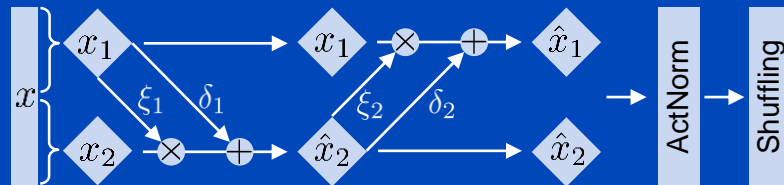
1. Our work is based on Rombach et al.<sup>1</sup>
2. **Train denoising methods** Chen et al. & Yang et al.
3. Train VAE to learn a complete data representation of the **low dose** images  $x$ .
4. For each denoising method and layer in the network we wish to evaluate, train a **clNN to recover the invariances**.
5. For a given test image, sample 250 invariances  $v$ , apply the inverse mapping  $t^{-1}$  and apply the pretrained decoder  $D$ .

$t^{-1}$  maps  $\mathcal{N}(0, 1)$  onto  $p(\bar{z}|z)$ .

Thus it produces only images that are likely under the training distribution of the AE.



**Alternative: Use VAE in high dose domain, i.e. VAE<sub>y</sub>, to visualize the invariances.**



Building block of INN: Invertible block,  $\xi_{12}$  and  $\delta_{12}$  are CNNs or NNs

$$x_1 \exp(\xi_2(\hat{x}_2)) + \delta_2(\hat{x}_2) = \hat{x}_1$$

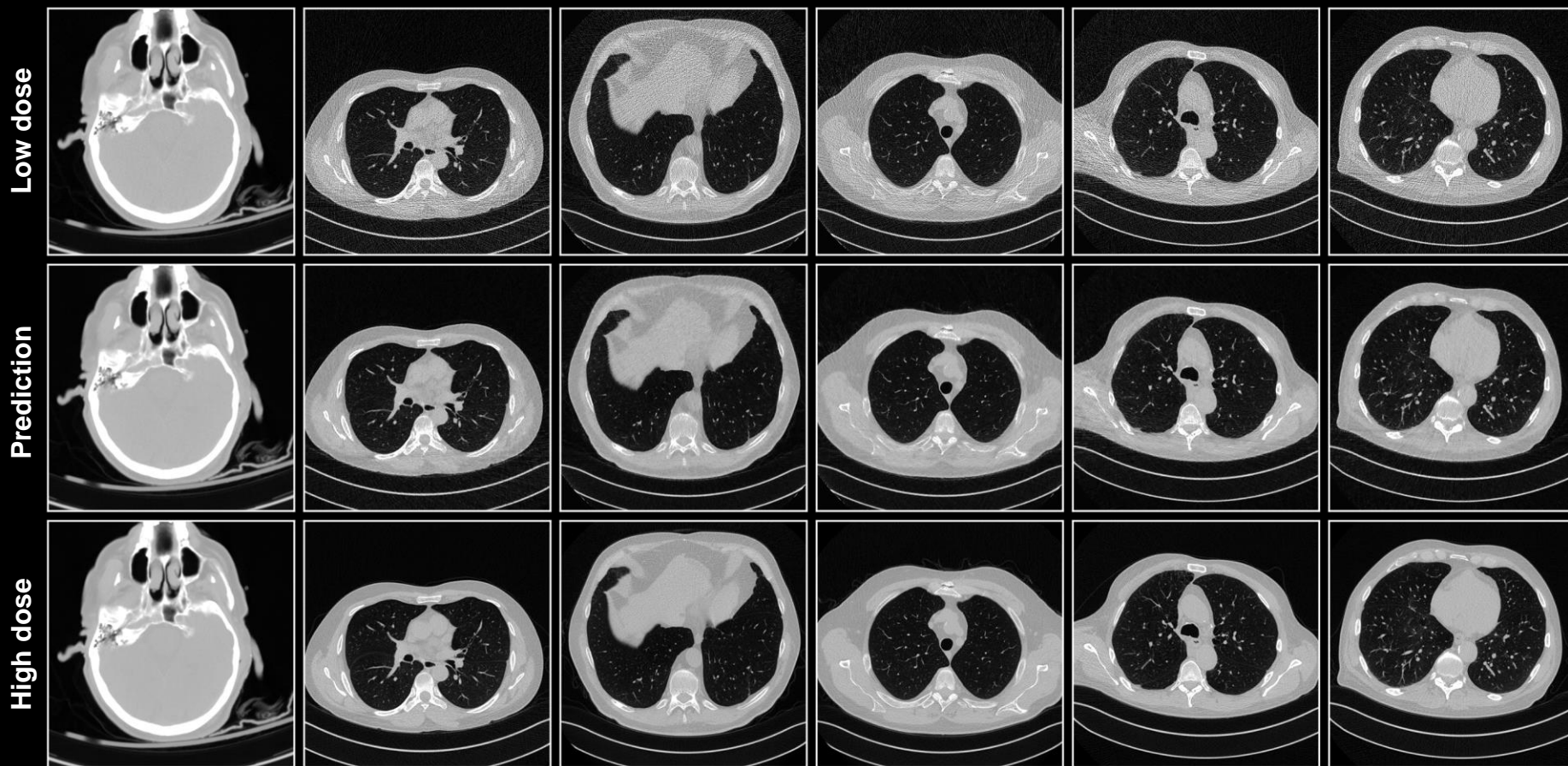
$$x_2 \exp(\xi_1(x_2)) + \delta_1(x_1) = \hat{x}_2$$

<sup>1</sup>Rombach et al. "Making sense of CNNs: Interpreting deep representations and their invariances with INNs", ECCV 2020.



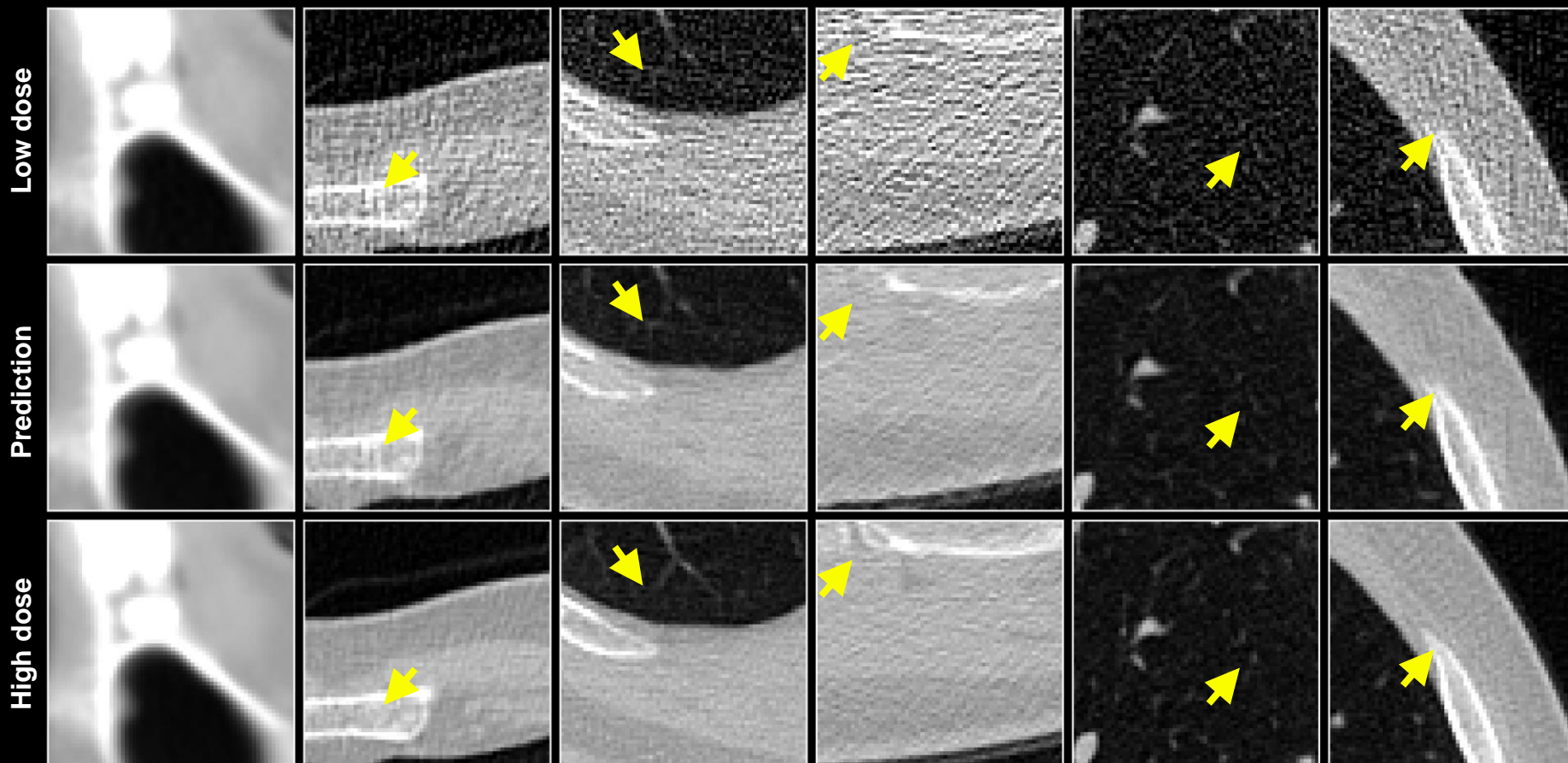
# Results

Denoising (Yang et al.)  $f = \Psi \circ \Phi$



# Results

Denoising (Yang et al.)  $f = \Psi \circ \Phi$

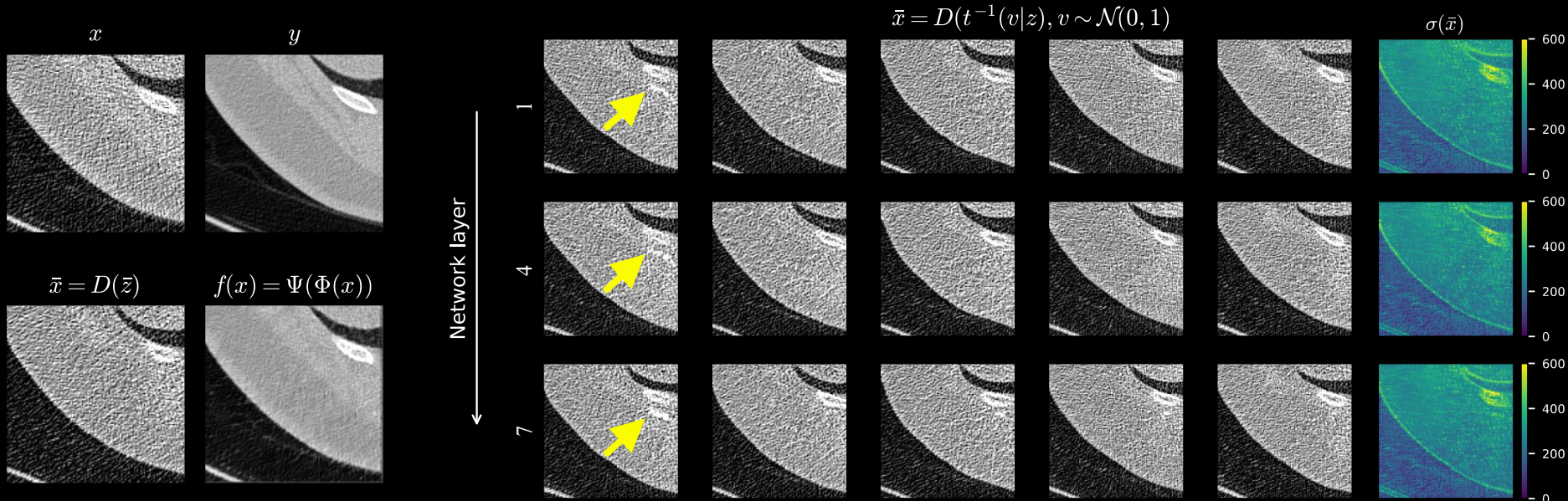


Arrows point at selected differences between prediction and ground truth.



# Results

## Sampling Invariances in Yang et al.'s Net

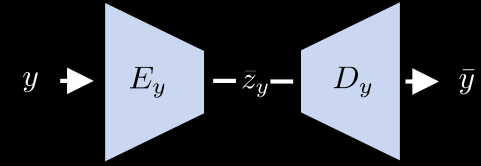


$$\Phi(x) = \Phi(\bar{x}) \quad \forall \bar{x}$$

$$x' = f(x) = f(\bar{x}) \quad \forall \bar{x}$$

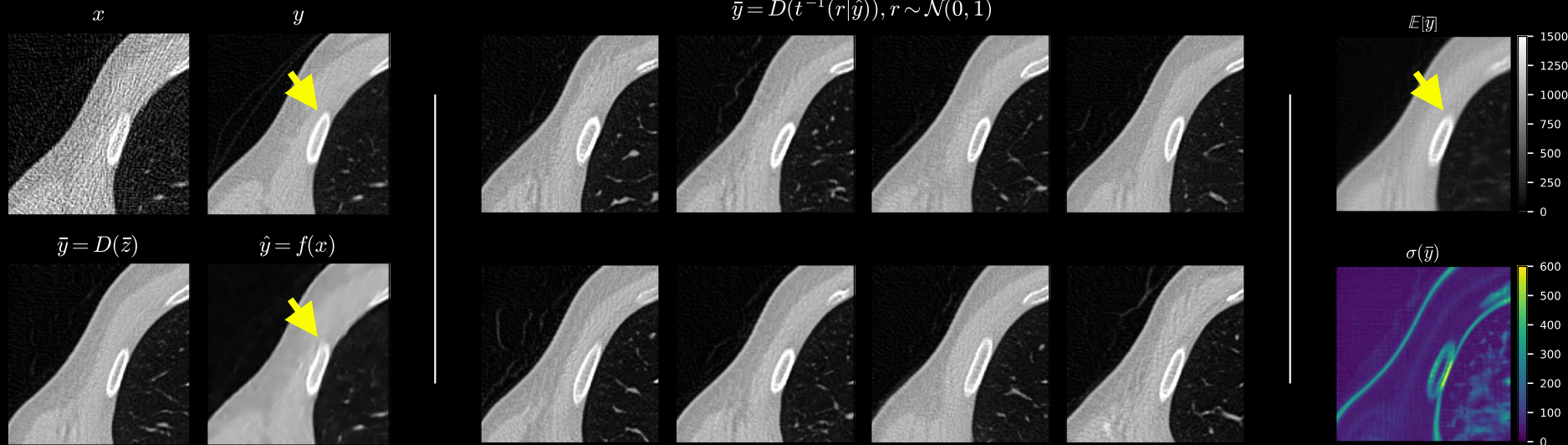
Same samples of  $v$  used for the rows corresponding to wiretapping after layers 1, 4 and 7.

1 Conv k9 f64  
3 Conv k3 f32  
5 Conv k3 f1

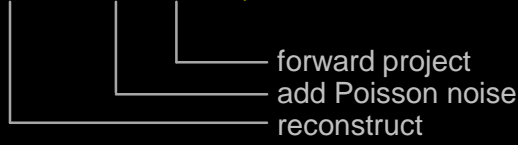


# Results

↑ Sampling Invariances in Target Domain in Chen et al.'s Net



$$x' = f(x) = f(\mathcal{R}^{-1} \mathcal{P} \mathcal{R} \bar{y}) \quad \forall \bar{y}$$



Wiretapping after last layer.

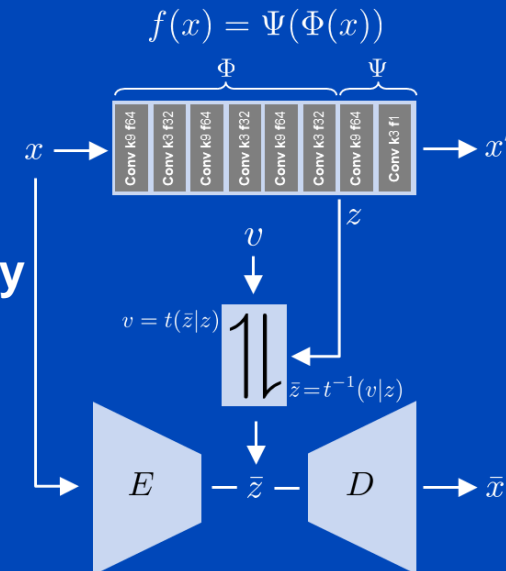
# Conclusions & Outlook

## Conclusions

- Designed a method to highlight invariances of a given network.
- Algorithm agnostic, not restricted to denoising .
- Architecture agnostic, not restricted to CT.
- Both denoising methods are invariant to some anatomical features to some extent.

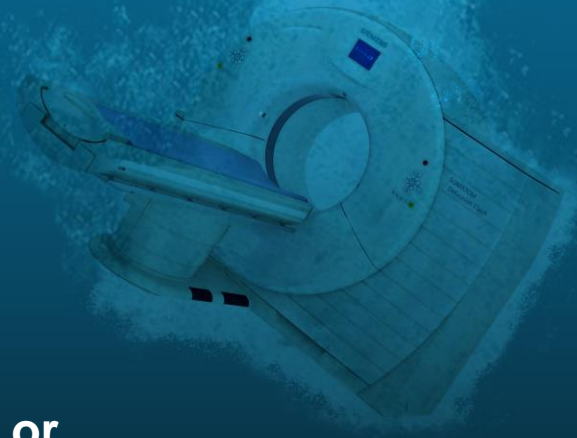
## Outlook

- Improve interpretability by
  - improving the embedding of the VAEs,
  - mapping sampled invariance images to semantically meaningful space (disentangled representations of e.g. tumors).
- One could use the undesired invariances to finetune the denoising methods.



# Conclusions on Deep CT

- Machine learning plays and will play a significant role in CT image formation.
- High potential for
  - Artifact correction
  - Noise and dose reduction
  - Real-time dose assessment (also for RT)
  - ...
- Care has to be taken
  - Underdetermined acquisition, e.g. sparse view or limited angle CT, require the net to make up information!
  - Nice looking images do not necessarily represent the ground truth.
  - Data consistency layers and variational networks with rawdata access may ensure that the information that is made up is consistent with the measured data.
  - ...





# Thank You!

Job opportunities through DKFZ's international PhD or Postdoctoral Fellowship programs ([marc.kachelriess@dkfz.de](mailto:marc.kachelriess@dkfz.de)).

Parts of the reconstruction software were provided by RayConStruct<sup>®</sup> GmbH, Nürnberg, Germany.